

Mediating Between Modeled and Observed Behavior: The Quest for the "Right" Process

prof.dr.ir. Wil van der Aalst



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Where innovation starts

Outline

**Introduction
to Process
Mining (short)**

**The 4+
dimensions of
conformance**

**Importance of
alignments to relate
observed and
modeled behavior**

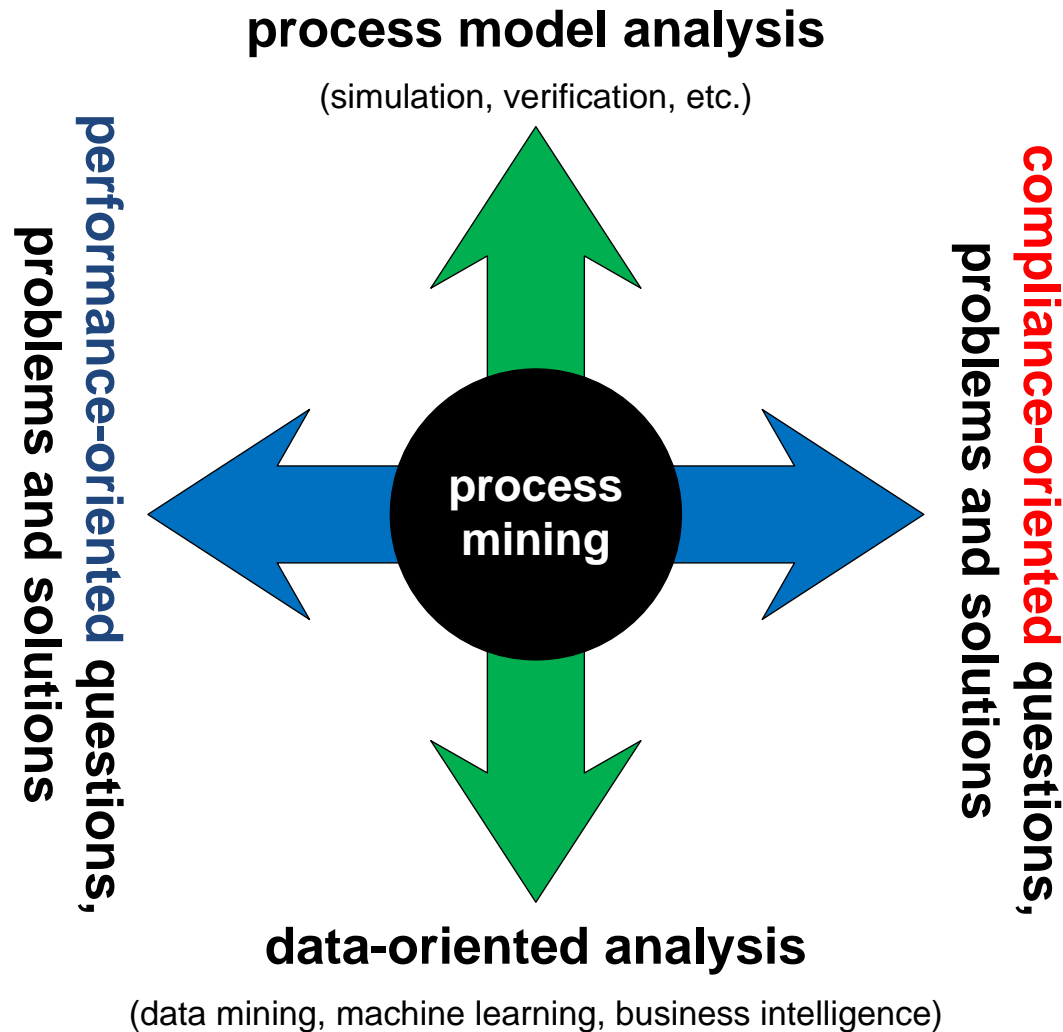
**Representational
bias**

**Mediating between
a reference model
and observed
behavior (model
repair)**

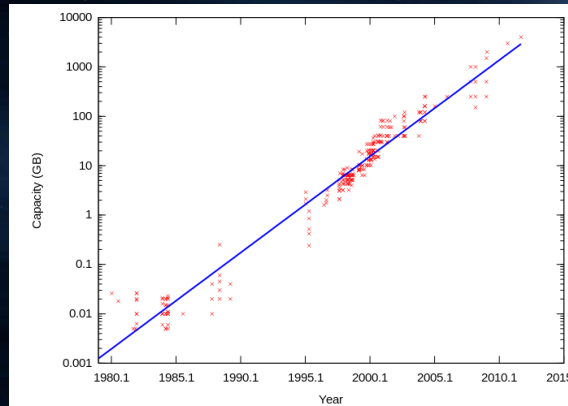
**Discovering
configurable
process models**

**Decomposing process
mining problems to
deal with Big Data**

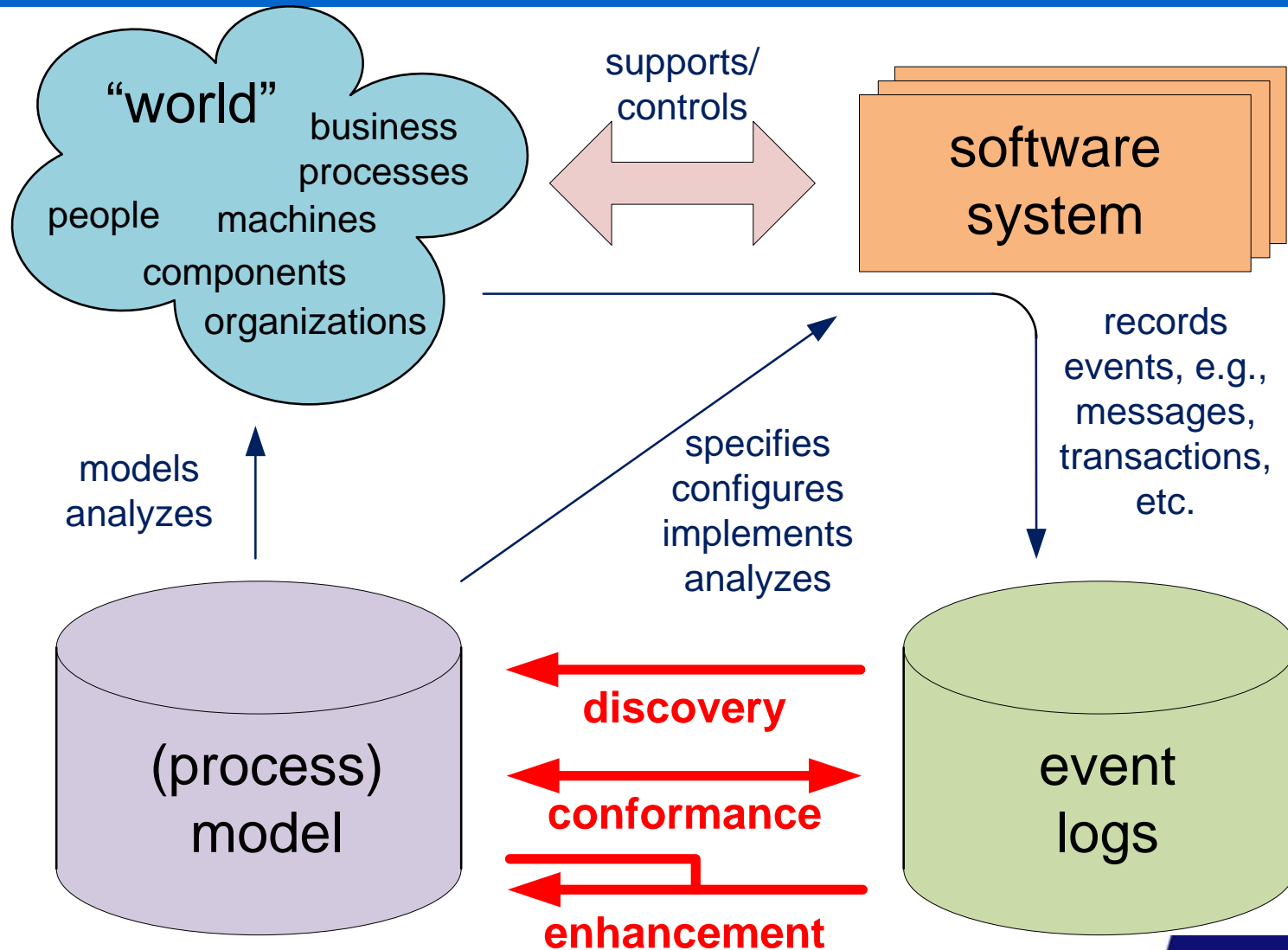
Positioning Process Mining



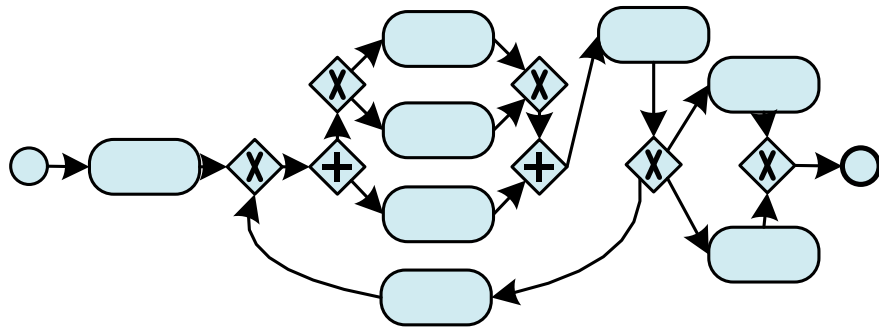
2013



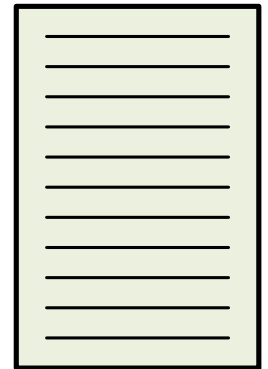
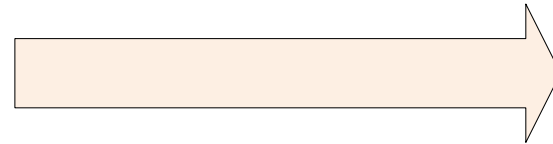
Three Types of Process Mining



Play-Out

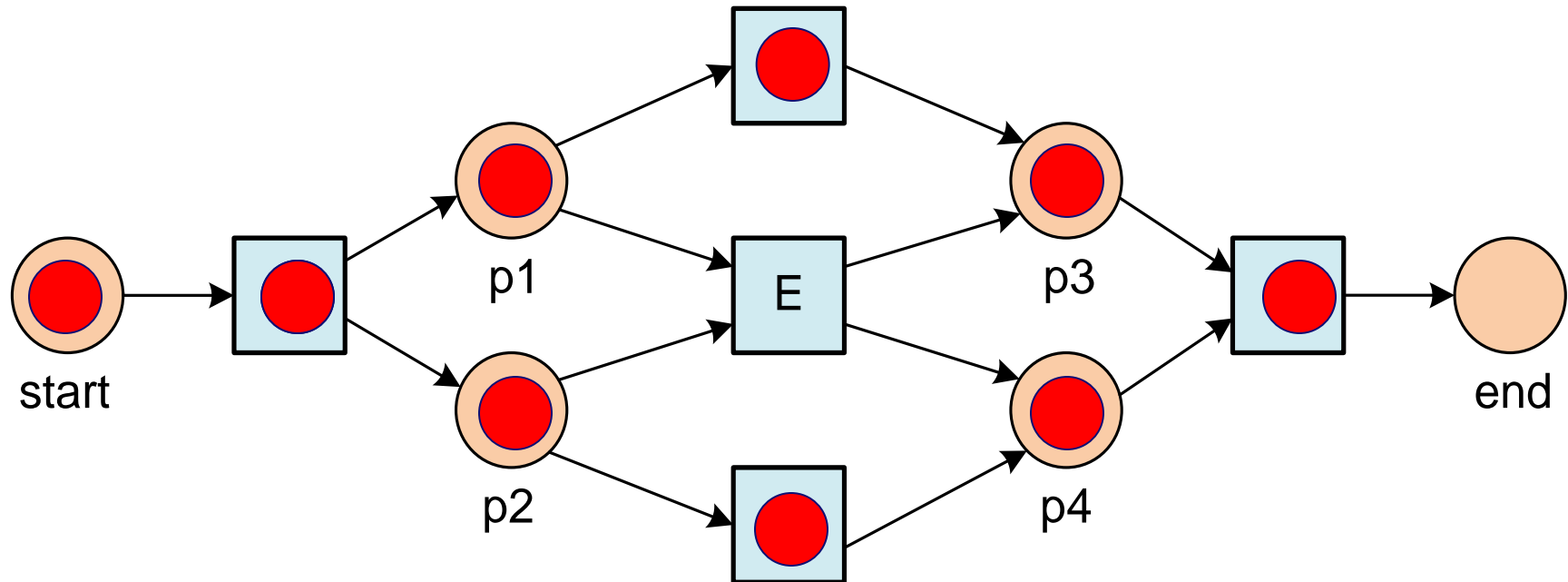


process model



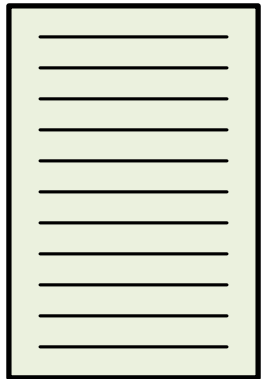
event log

Play-Out (Classical use of models)

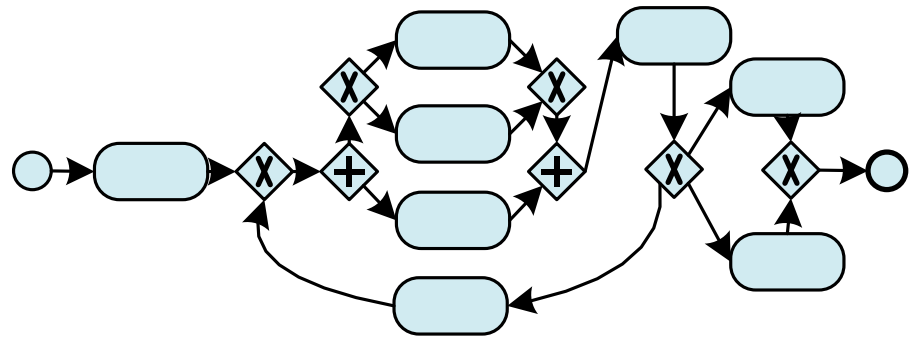
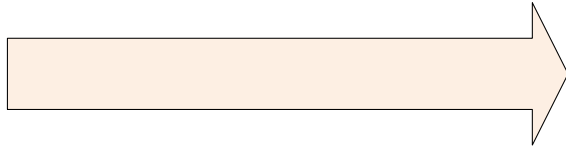


A B C D **A E D** **A E D**
 A B C D **A C B D**
A C B D **A E D** **A C B D**

Play-In



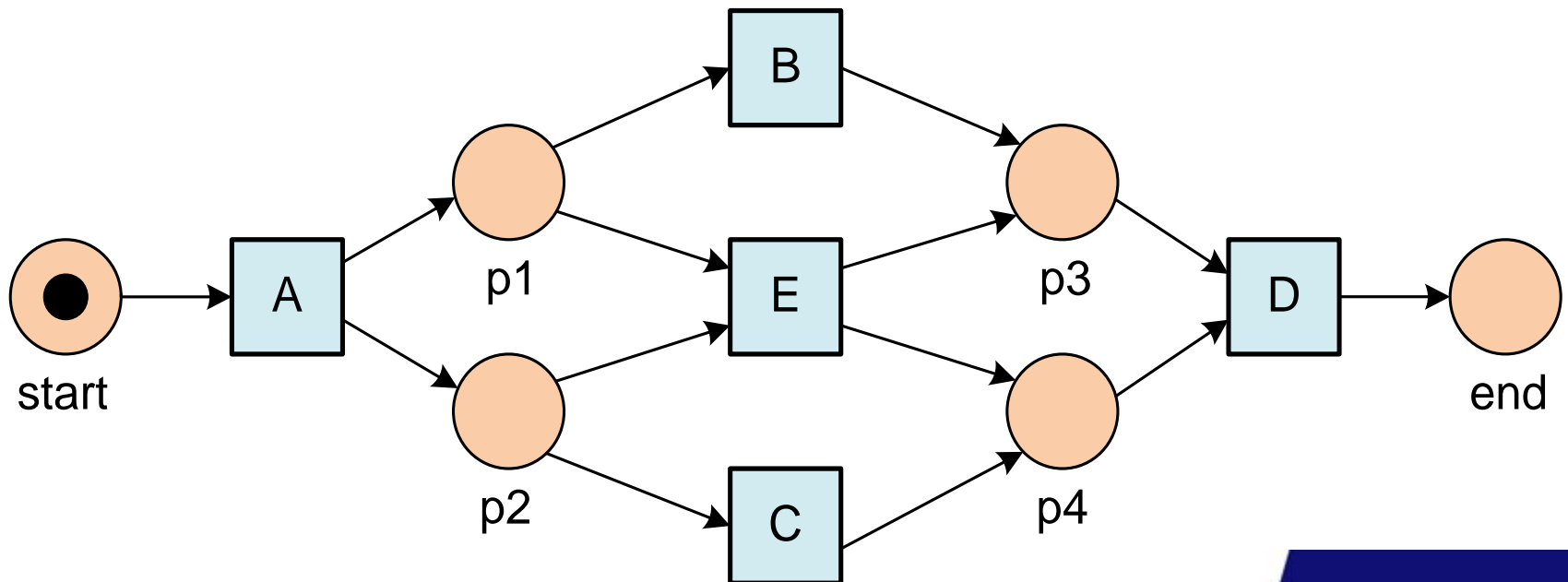
event log



process model

Play-In

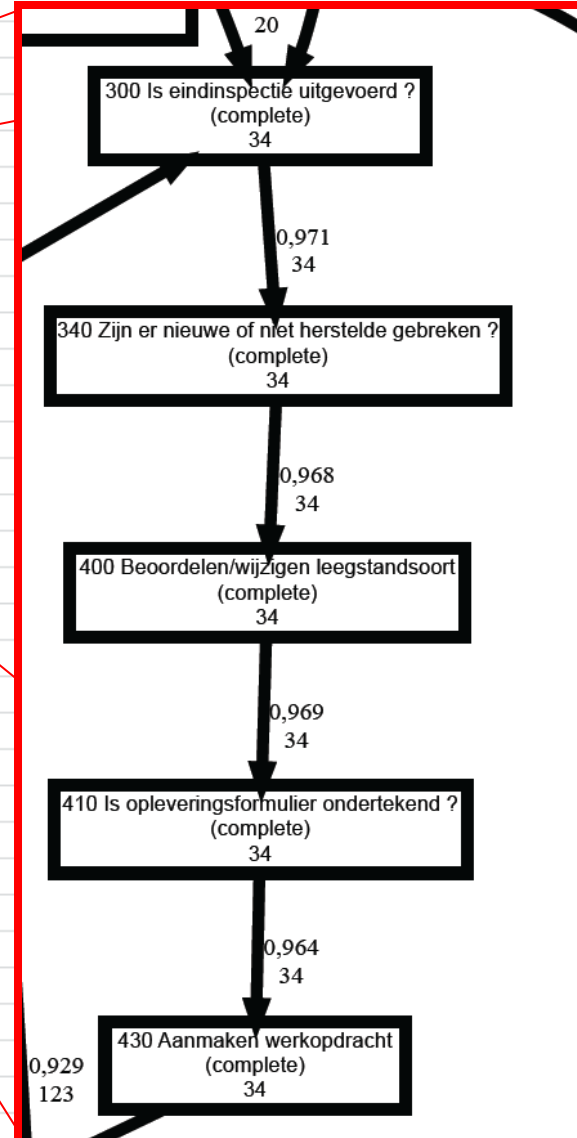
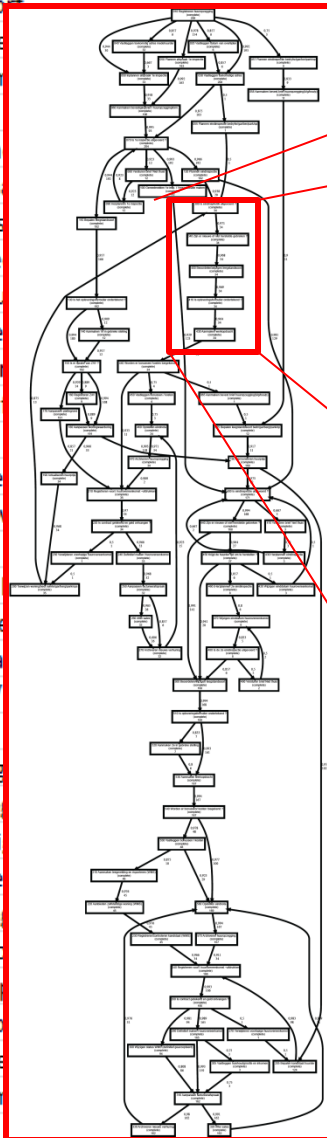
A B C D A E D A E D
A C B D A B C D A C B D
A C B D A E D A C B D



Example Process Discovery

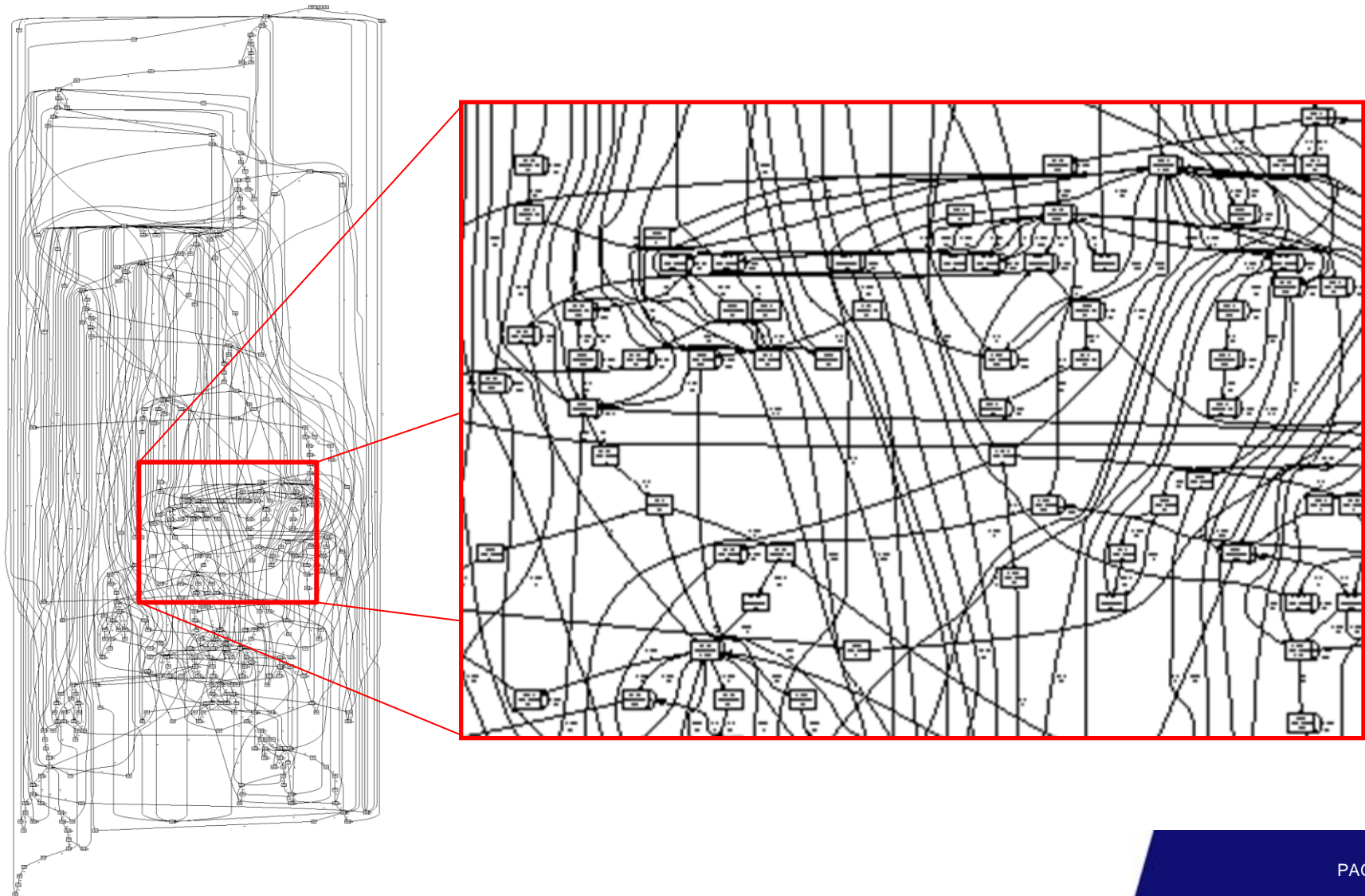
(Vestia, Dutch housing agency, 208 cases, 5987 events)

117315	110 Bepalen leegstandsoort	16.05.2007 14:06:23
117315	120 Plannen eindinspectie	16.05.2007 14:36:01
117315	130 Is het opleveringsform	23.05.2007 09:41:40
117315	150 Is er sprake van ZAV ?	23.05.2007 09:41:51
117315	170 Aanpassen plattegron	23.05.2007 11:57:18
117315	180 Aanpassen woningwa	23.05.2007 09:42:37
117315	190 Actualiseren huurprijs	23.05.2007 09:48:23
117315	200 Toewijzen woning/be	23.05.2007 09:48:29
117315	210 Registreren voorl. hu	10.09.2007 16:24:36
117315	220 Is contract getekend e	11.09.2007 14:56:18
117315	240 Definitief maken Huu	31.03.2008 16:17:12
117315	250 Aanpassen factureera	09.09.2008 15:39:59
117315	260 After sales	09.09.2008 16:51:24
117315	270 Archiveren nieuwe ve	10.09.2008 07:52:08
117315	300 Is eindinspectie uitgev	07.06.2007 14:47:04
117315	340 Zijn er nieuwe of niet	07.06.2007 14:47:06
117315	400 Beoordelen/wijzigen	07.06.2007 14:51:16
117315	410 Is opleveringsformulie	07.06.2007 14:51:26
117315	430 Aanmaken werkopdra	11.06.2007 09:21:39
117315	440 Worden er bonussen/	11.06.2007 09:21:49
117315	460 Opstellen eindnota	08.08.2007 16:18:26
117315	470 Archiveren huuropzeg	09.08.2007 14:42:23
119763	010 Registreren huuropze	09.05.2007 11:19:14
119763	030 Vastleggen toekomst	09.05.2007 12:25:01
119763	050 Inplannen afspraak 1e	09.05.2007 11:59:52
119763	060 Aanmaken bevestigin	09.05.2007 12:31:57
119763	070 Is 1e inspectie uitgev	16.05.2007 13:04:26
119763	100 Gereedmelden 1e ins	16.05.2007 13:43:39
119763	110 Bepalen leegstandsoo	16.05.2007 13:43:28
119763	120 Plannen eindinspectie	16.05.2007 13:42:58
119763	130 Is het opleveringsform	16.05.2007 13:34:49
119763	150 Is er sprake van ZAV ?	16.05.2007 13:34:56



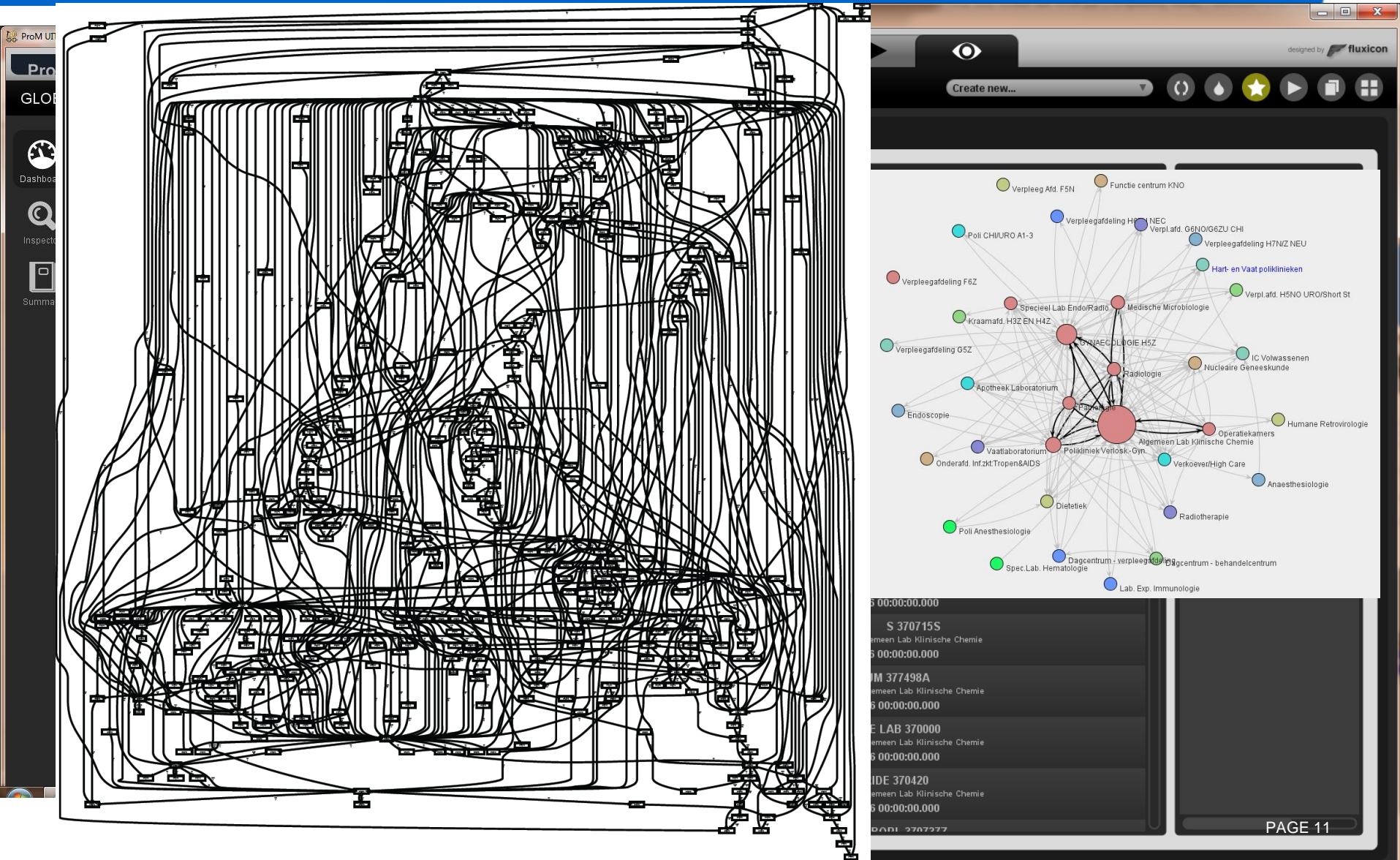
Example Process Discovery

(ASML, test process lithography systems, 154966 events)

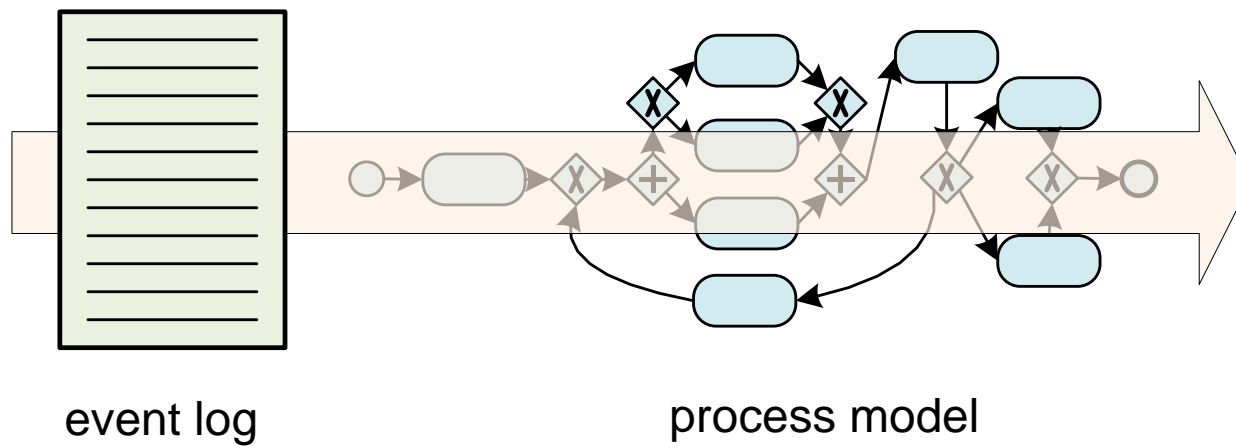


Example Process Discovery

(AMC, 627 gynecological oncology patients, 24331 events)



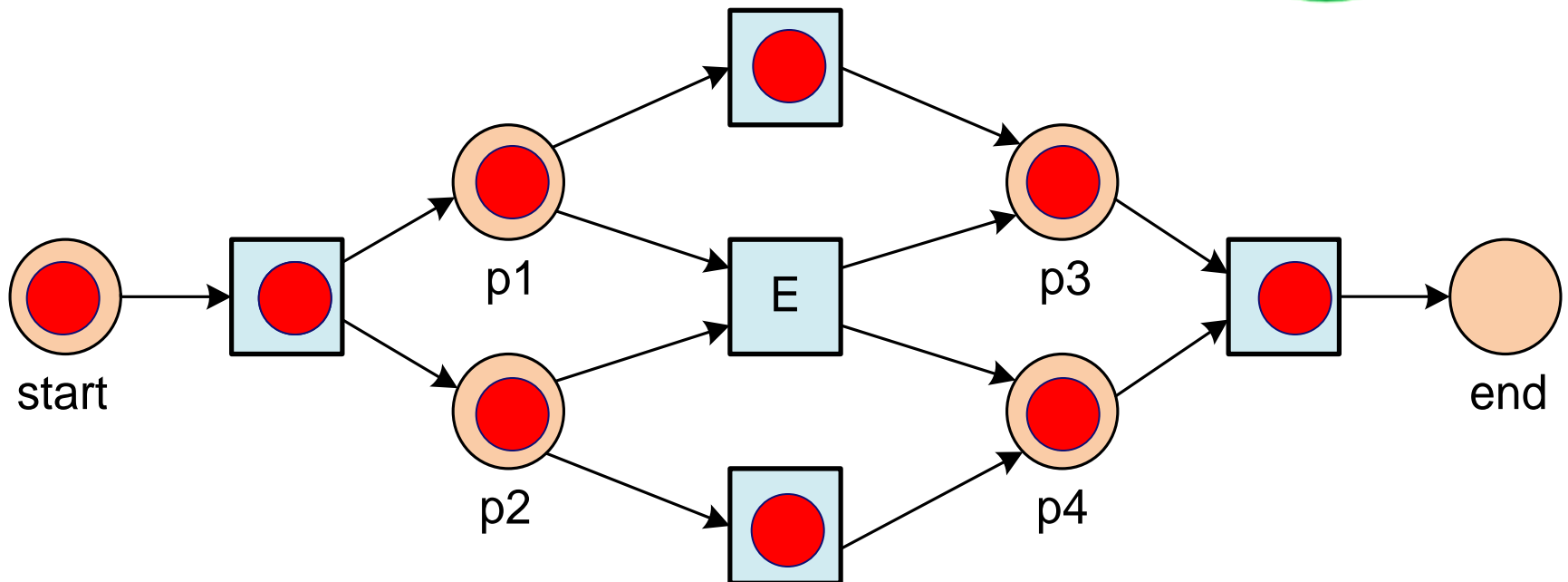
Replay



- extended model showing times, frequencies, etc.
- diagnostics
- predictions
- recommendations

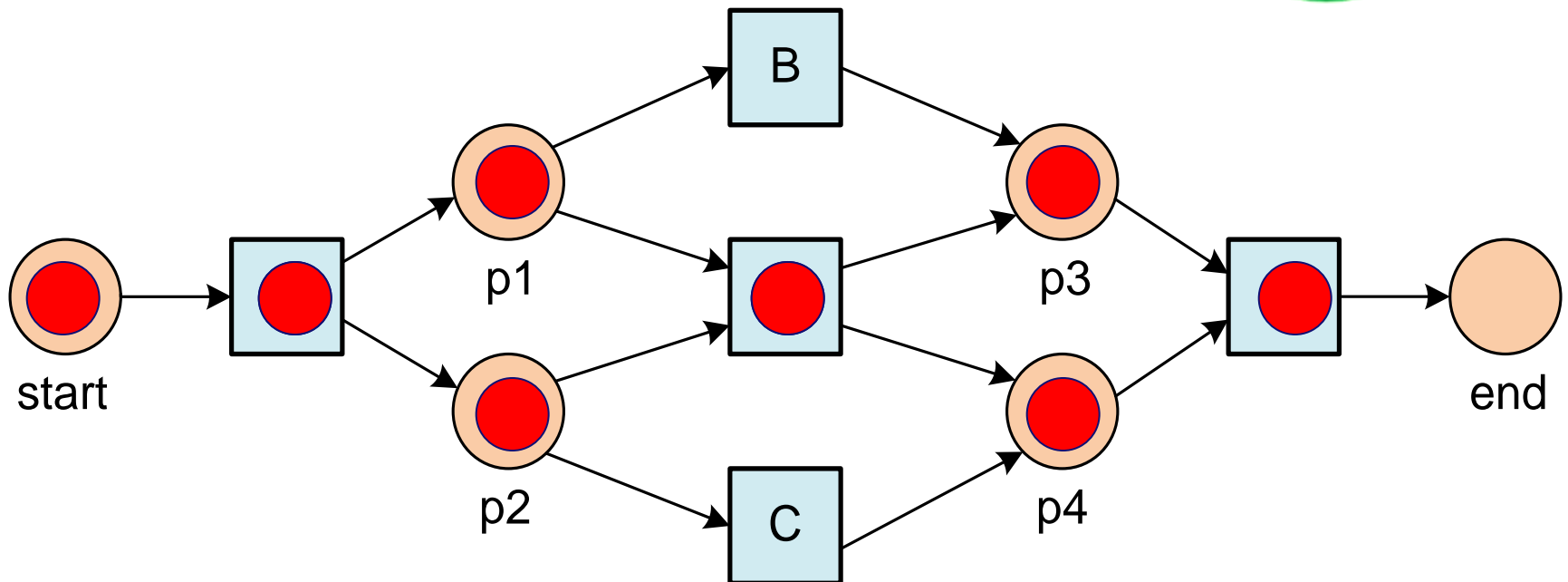
Replay

A B C D



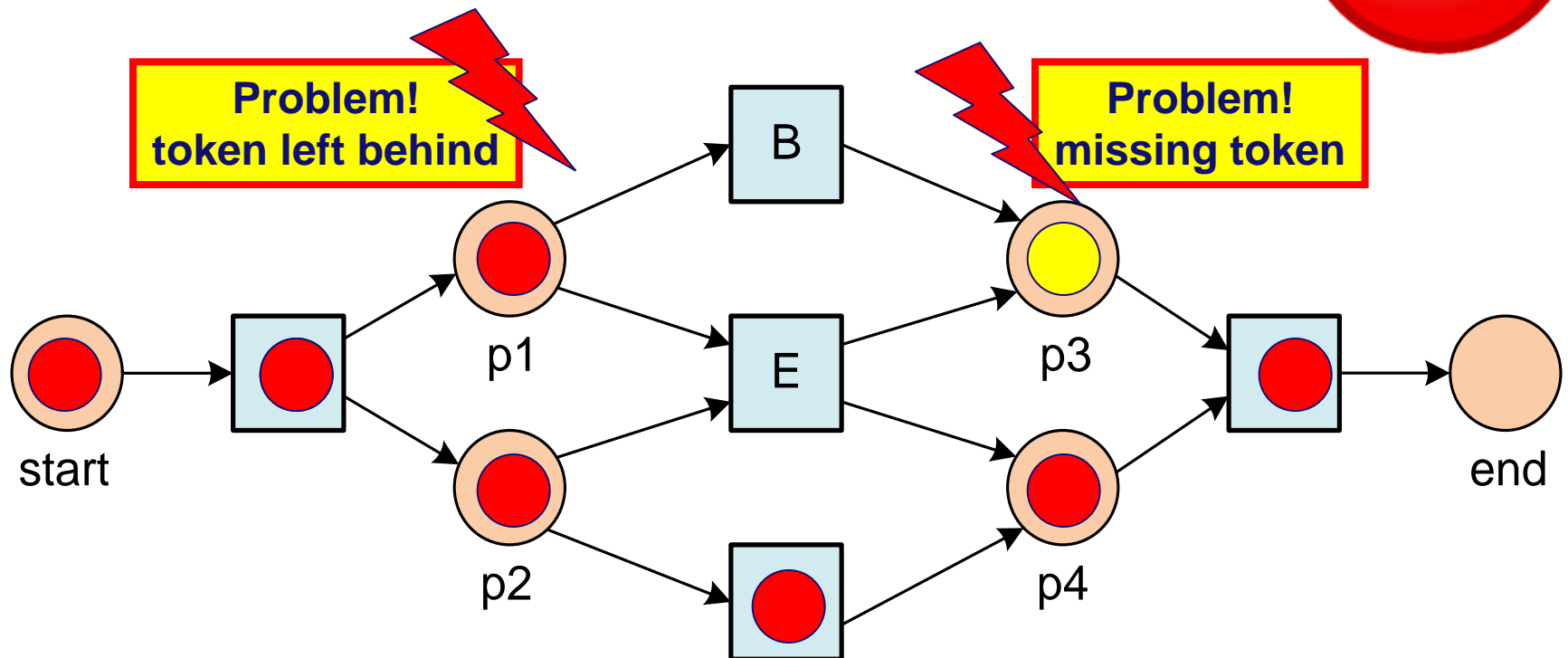
Replay

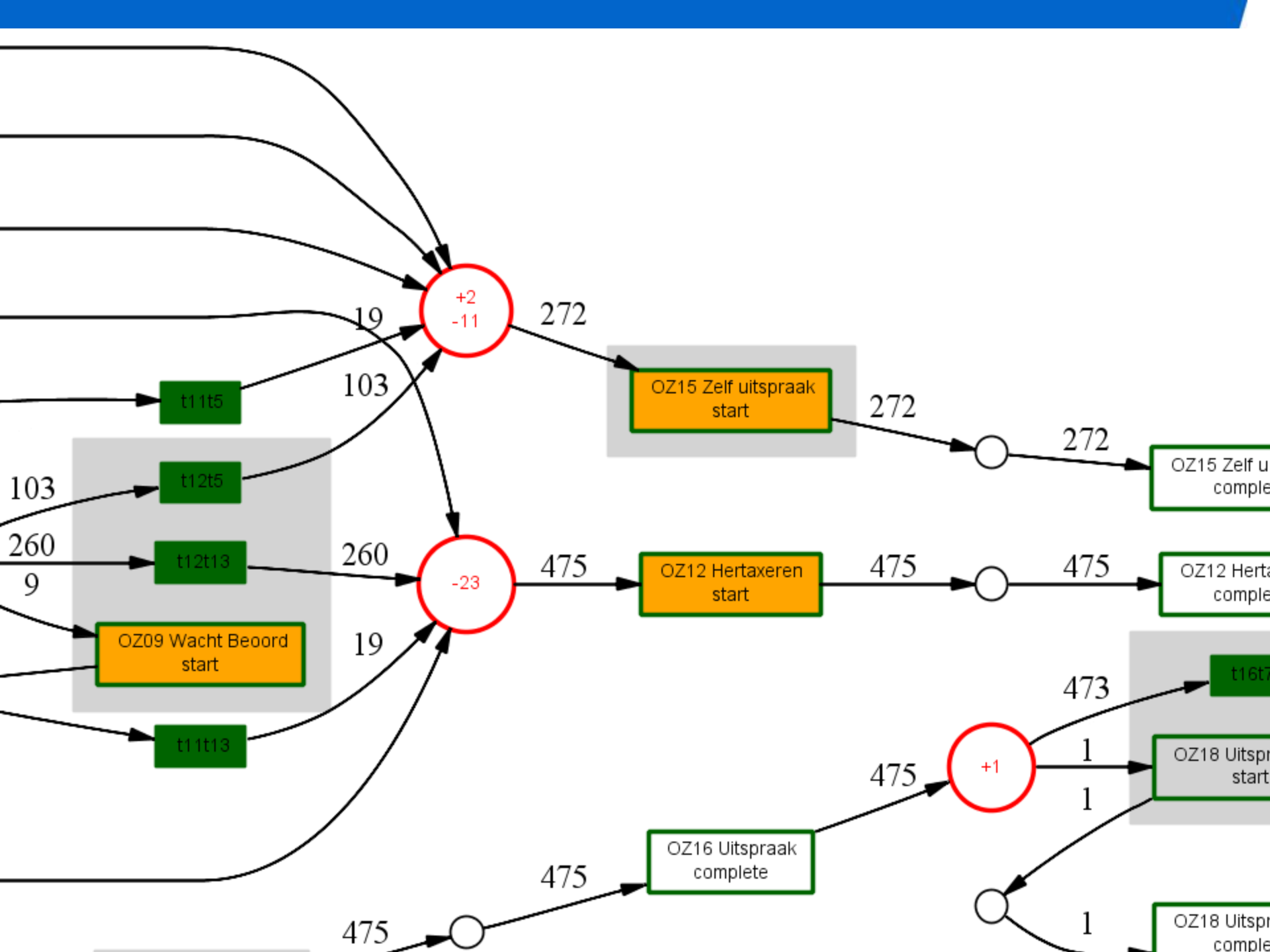
A E D



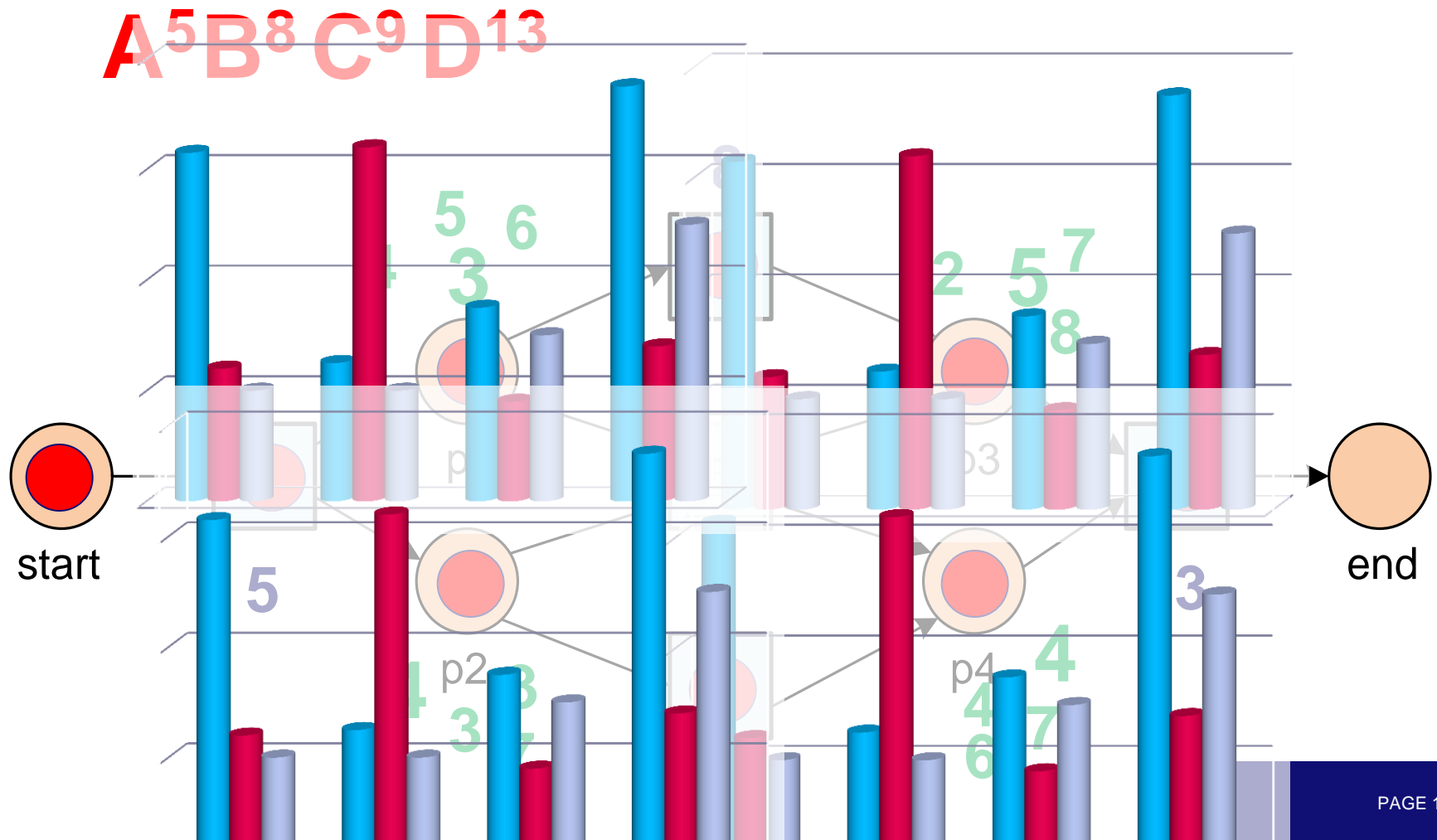
Replay can detect problems

A C D



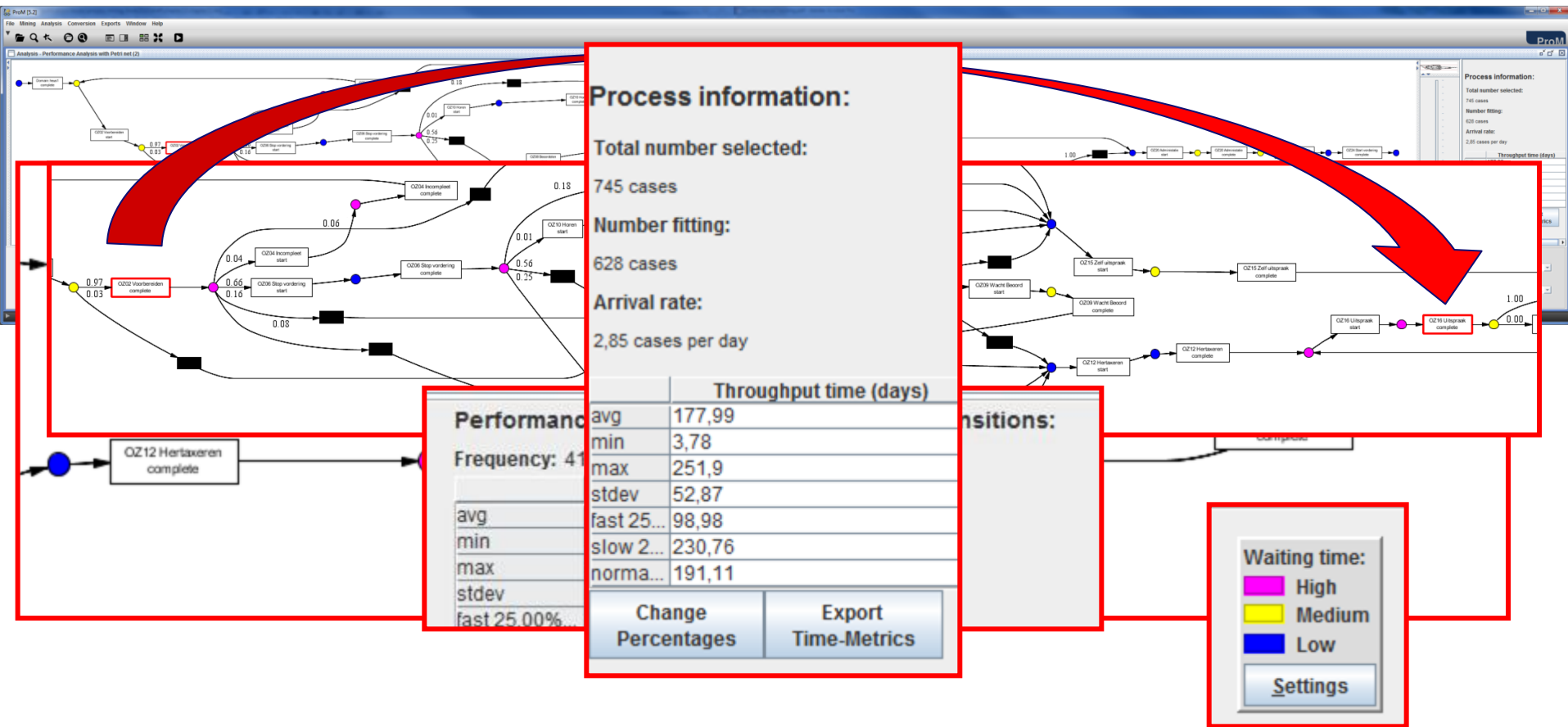


Replay can extract timing information



Performance Analysis Using Replay

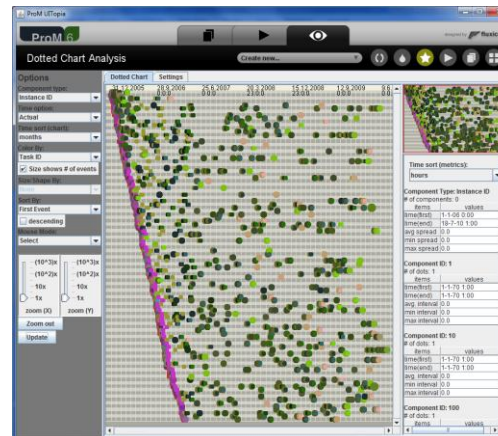
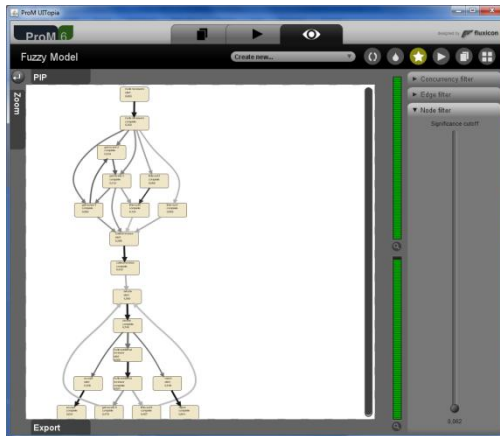
(WOZ objections Dutch municipality, 745 objections, 9583 event, $f=0.988$)



Hundreds of plug-ins available covering the whole process mining spectrum



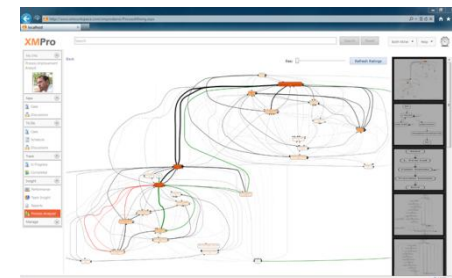
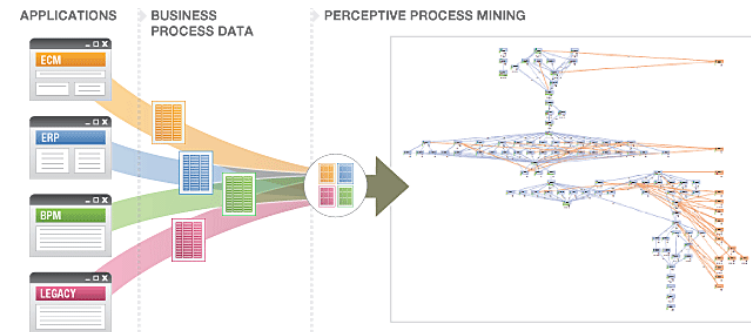
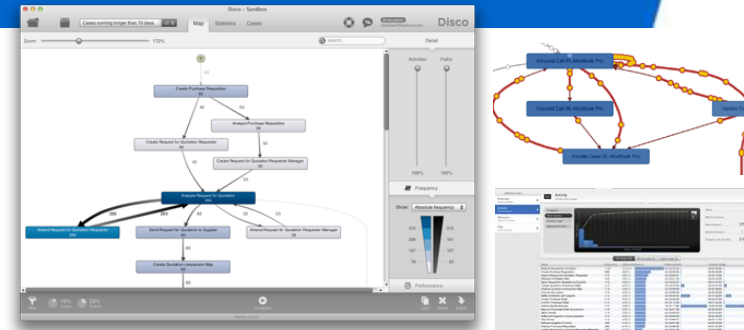
open-source (L-GPL)



Download from: www.processmining.org

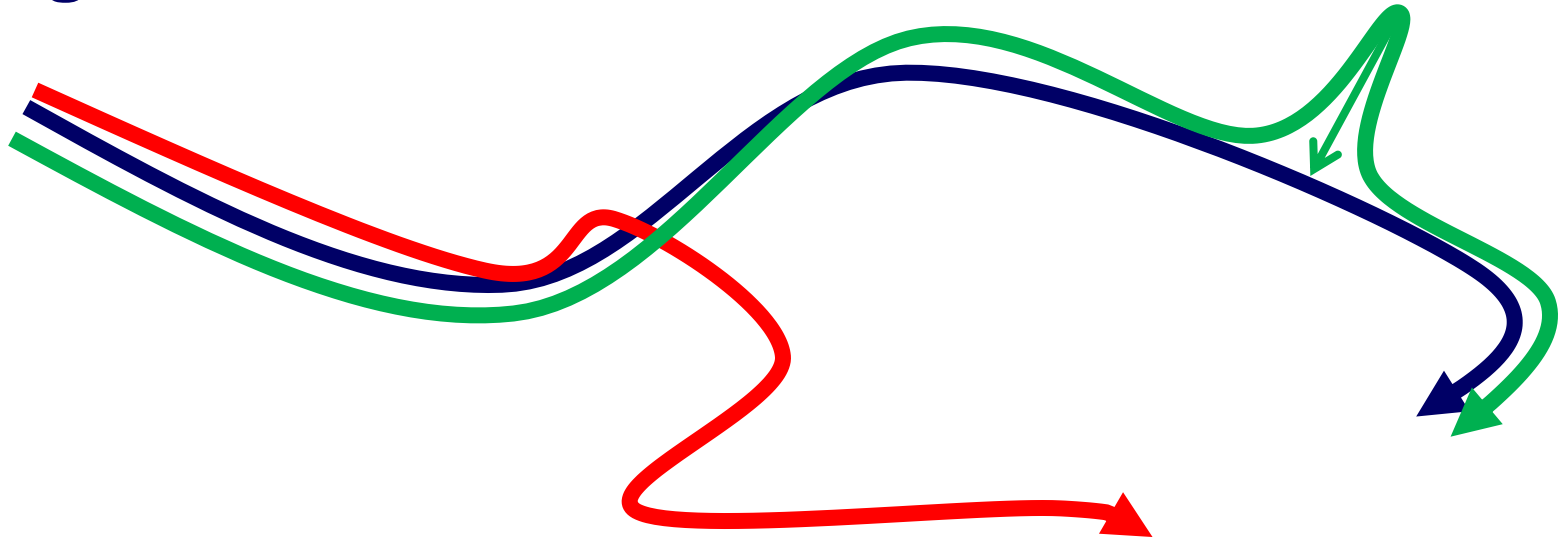
Commercial Alternatives

- **Disco (Fluxicon)**
- **Perceptive Process Mining**
(before Futura Reflect and BPM|one)
- **ARIS Process Performance Manager**
- **QPR ProcessAnalyzer**
- **Interstage Process Discovery (Fujitsu)**
- **Discovery Analyst (StereoLOGIC)**
- **XMAalyzer (XMPro)**
- ...

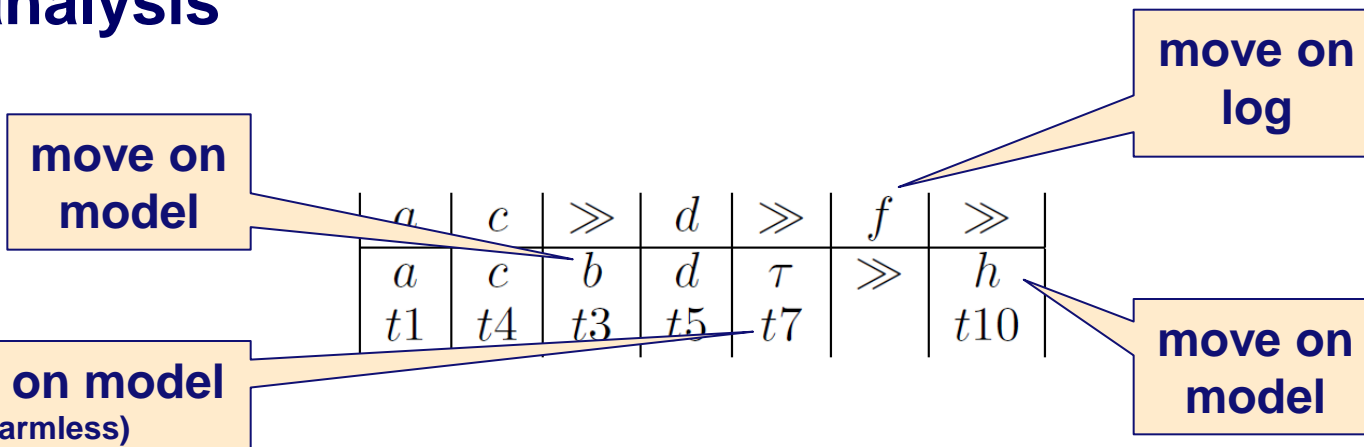


Three Key Observations

#1 Alignments are essential!

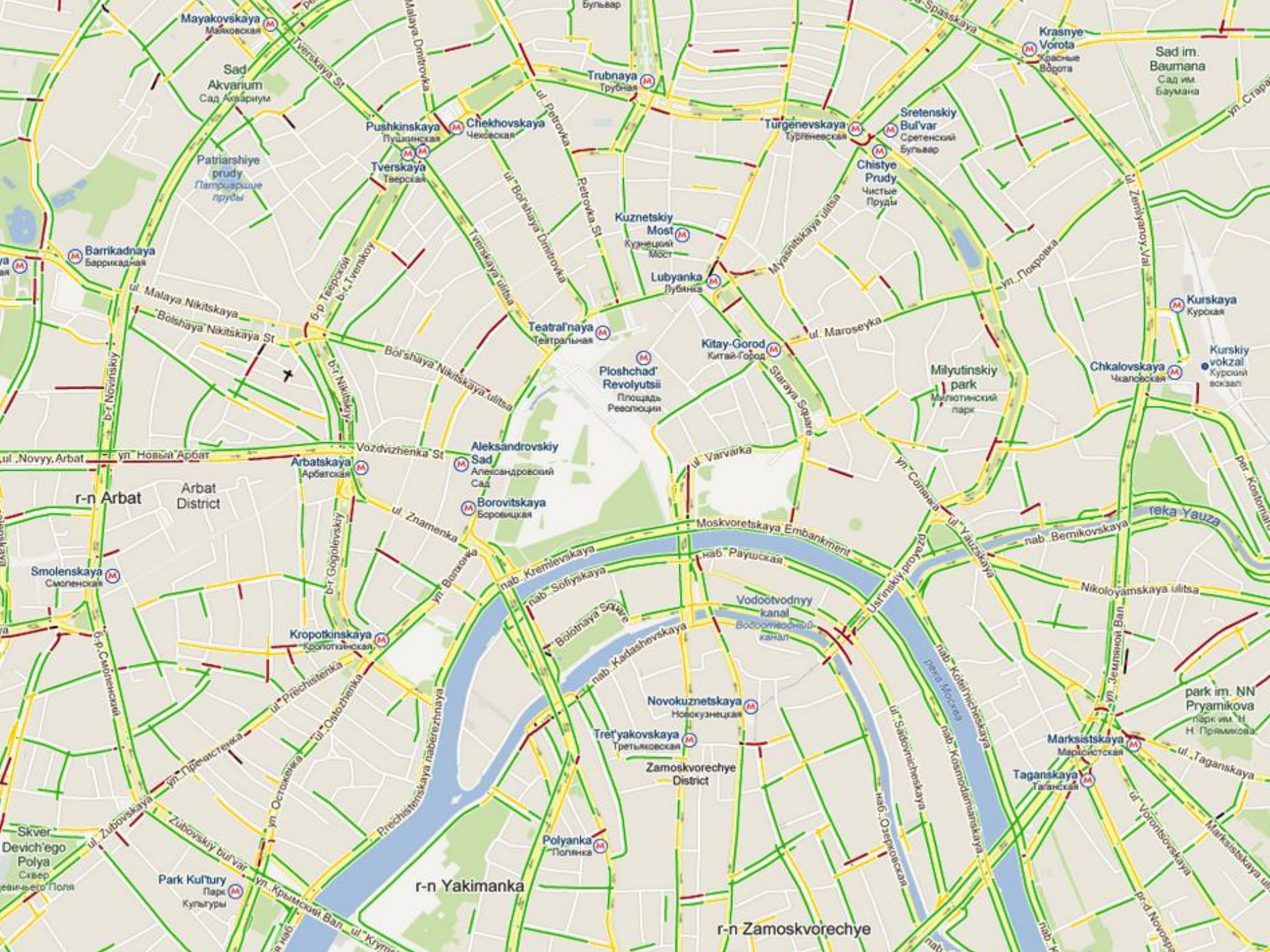


- conformance checking to diagnose deviations
- squeezing reality into the model to do model-based analysis



#2 Models are like the glasses required to see and understand event data!



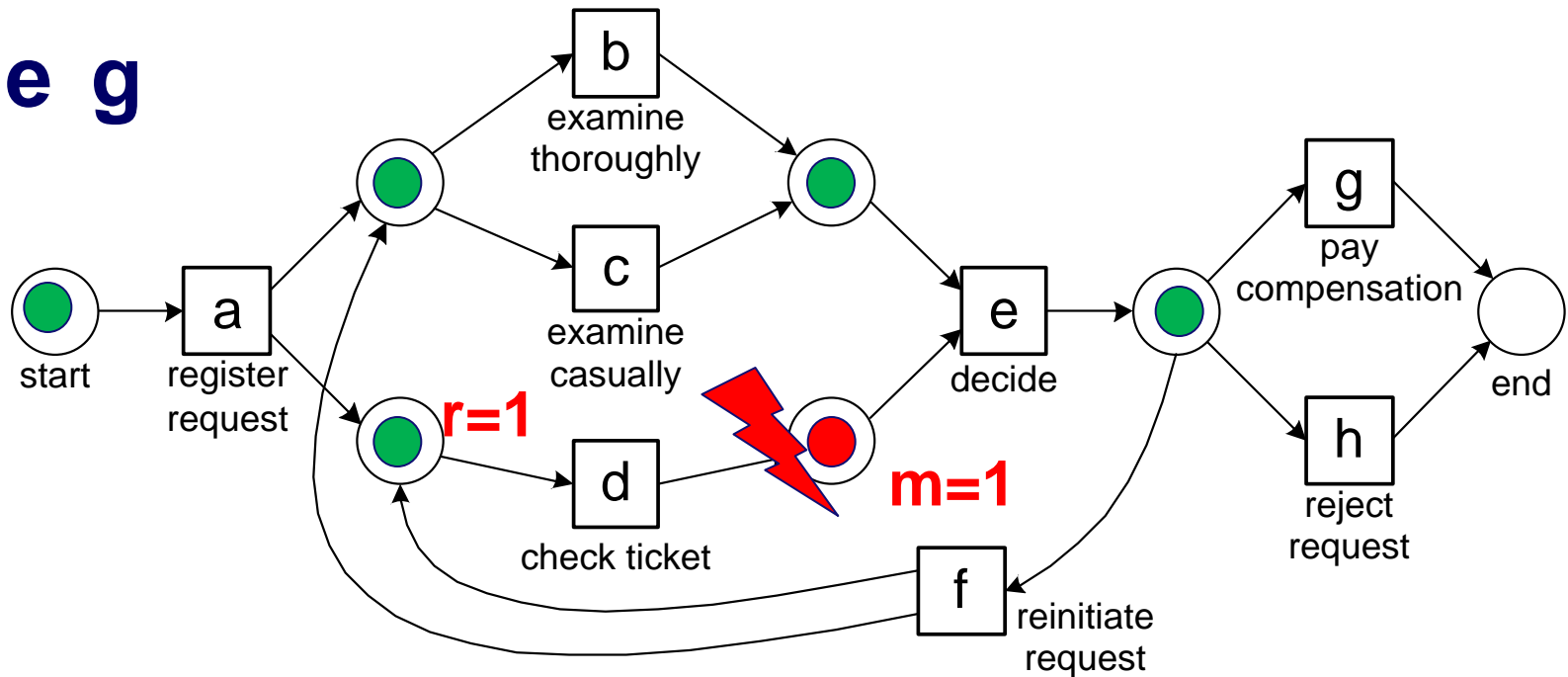


Alignments

Joint work with Arya Adriansyah, Boudewijn van Dongen, Elham Ramezani, Dirk Fahland, Massimiliano de Leoni, et al.

Replaying trace “abeg”

a b e g



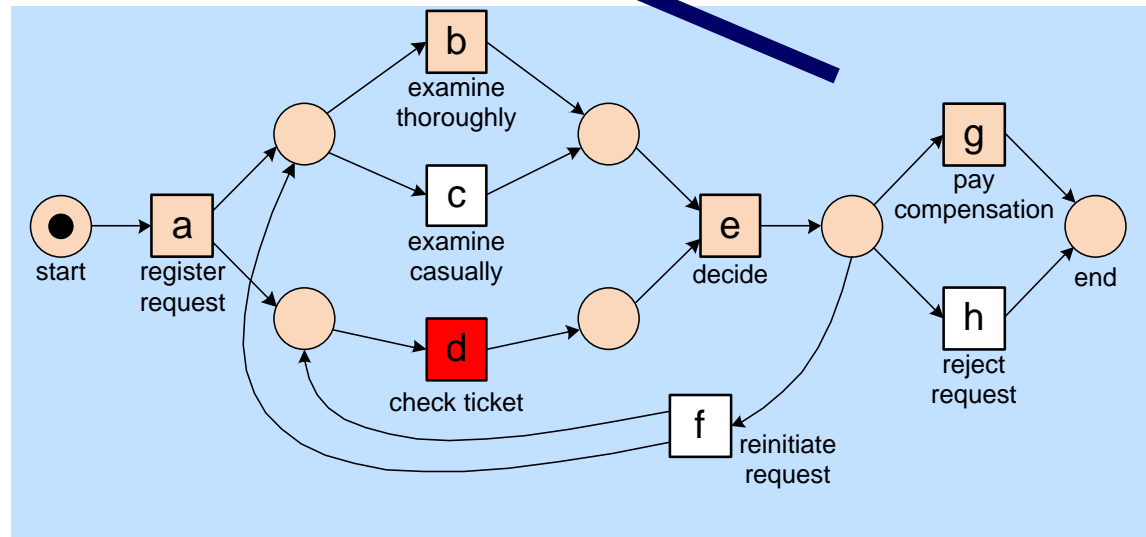
$$fitness(\sigma, N) = \frac{1}{2} \left(1 - \frac{1}{6} \right) + \frac{1}{2} \left(1 - \frac{1}{6} \right) = 0.83333$$

From “playing the token game” to optimal alignments ...

observed trace: “abeg”

a	b	»	e	g
a	b	d	e	g

move in
model only

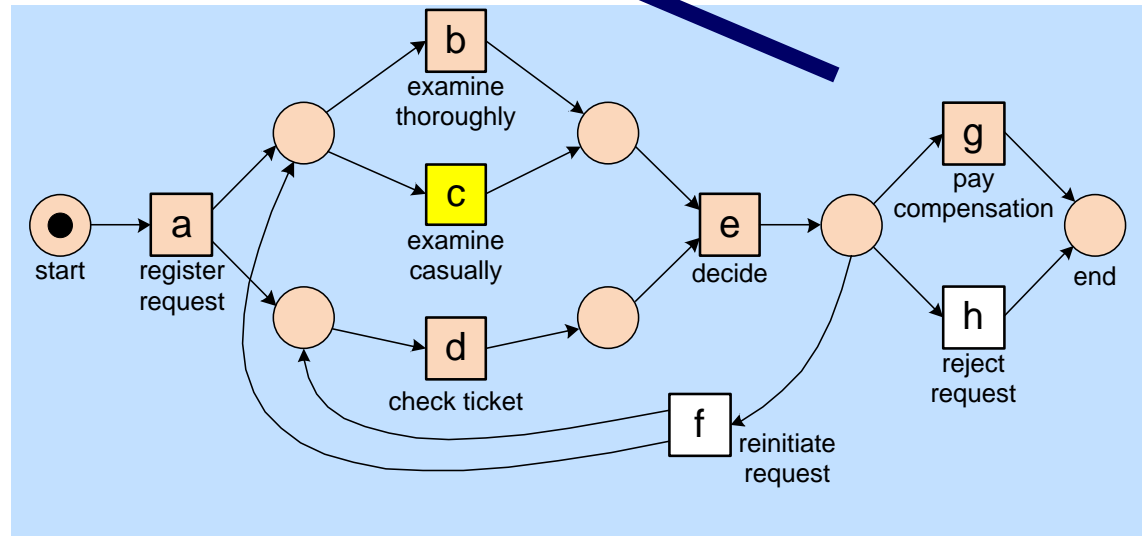


Another alignment

observed trace: “abcdeg”

a	b	c	d	e	g
a	b	»	d	e	g

move in
log only



Moves have costs

...	a	...
...	»	...

...	»	...
...	a	...

...	a	...
...	a	...

...	a	...
...	b	...

- Standard cost function:
 - $c(x, \text{»}) = 1$
 - $c(\text{»}, y) = 1$
 - $c(x, y) = 0$, if $x=y$
 - $c(x, y) = \infty$, if $x \neq y$

Any cost structure is possible

...	send-letter(John,2 weeks, \$400)	...
...	send-email(Sue,3 weeks,\$500)	...

- **Similar activities** (more similarity implies lower costs).
- **Resource conformance** (done by someone that does not have the specified role).
- **Data conformance** (path is not possible for this customer).
- **Time conformance** (missed the legal deadline)

Using Alignments

- An **optimal alignment** has the lowest possible costs.
- If multiple alignments are optimal, pick one or use all.
- Like an "**oracle**" revealing paths in the model.
- These paths can be used for further analysis!



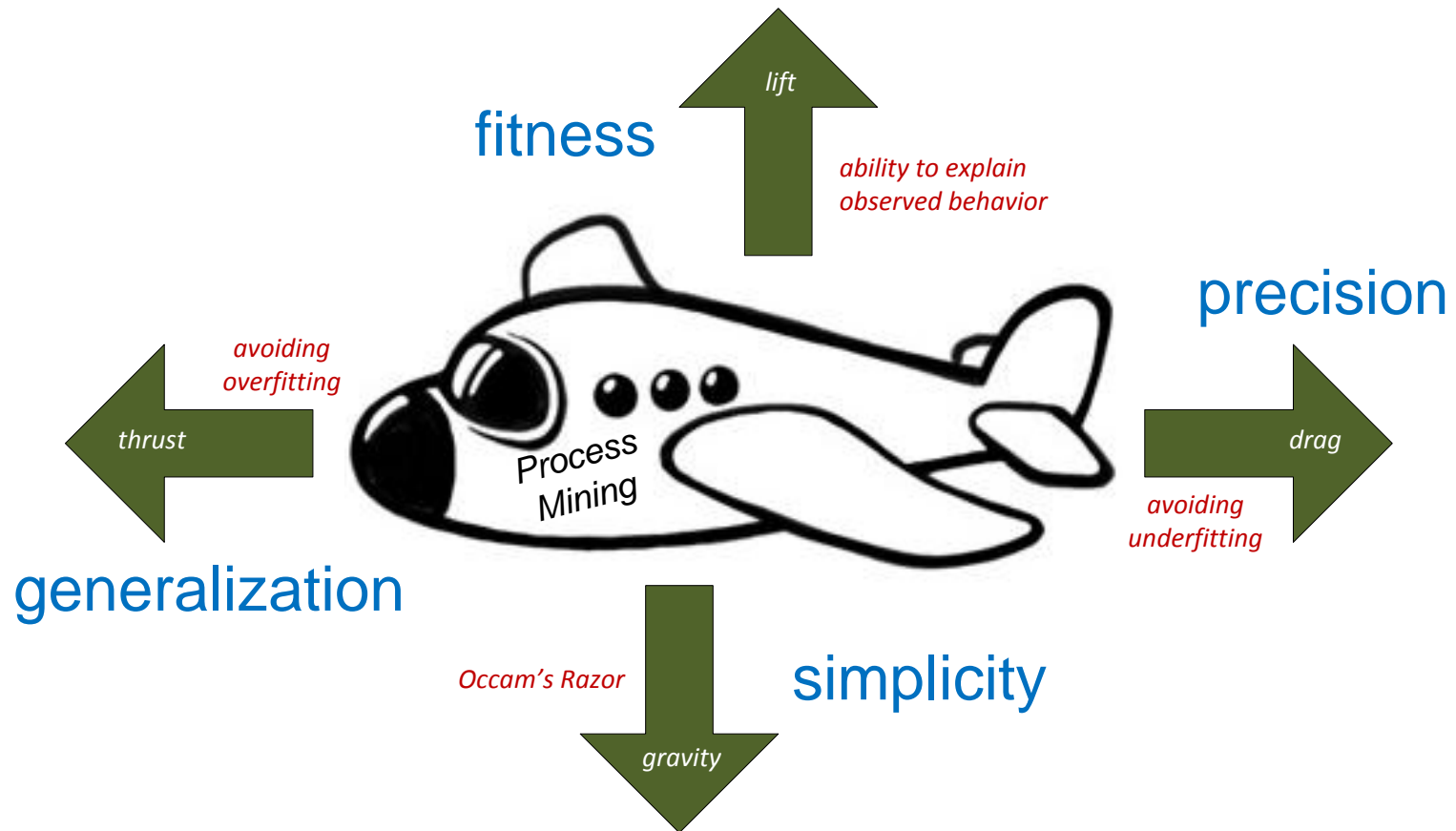
- Can be used for **quantifying various types conformance** (possibly using a different cost function).

Some pointers

- Wil M. P. van der Aalst, Arya Adriansyah, Boudewijn F. van Dongen: Replaying history on process models for conformance checking and performance analysis. Wiley Interdisc. Rew.: Data Mining and Knowledge Discovery 2(2): 182-192 (2012)
- Arya Adriansyah, Jorge Munoz-Gama, Josep Carmona, Boudewijn F. van Dongen, Wil M. P. van der Aalst: Alignment Based Precision Checking. Business Process Management Workshops 2012: 137-149
- Arya Adriansyah, Boudewijn F. van Dongen, Wil M. P. van der Aalst: Conformance Checking Using Cost-Based Fitness Analysis. EDOC 2011: 55-64
- Massimiliano de Leoni, Wil M. P. van der Aalst, Boudewijn F. van Dongen: Data- and Resource-Aware Conformance Checking of Business Processes. BIS 2012: 48-59
- Joos C. A. M. Buijs, Boudewijn F. van Dongen, Wil M. P. van der Aalst: On the Role of Fitness, Precision, Generalization and Simplicity in Process Discovery. OTM Conferences (1) 2012: 305-322
- Elham Ramezani, Dirk Fahland, Wil M. P. van der Aalst: Where Did I Misbehave? Diagnostic Information in Compliance Checking. BPM 2012: 262-278
- A. Adriansyah, B.F. van Dongen, W.M.P. van der Aalst. Memory-Efficient Alignment of Observed and Modeled Behavior. BPM Center Report BPM-13-03, BPMcenter.org, 2013

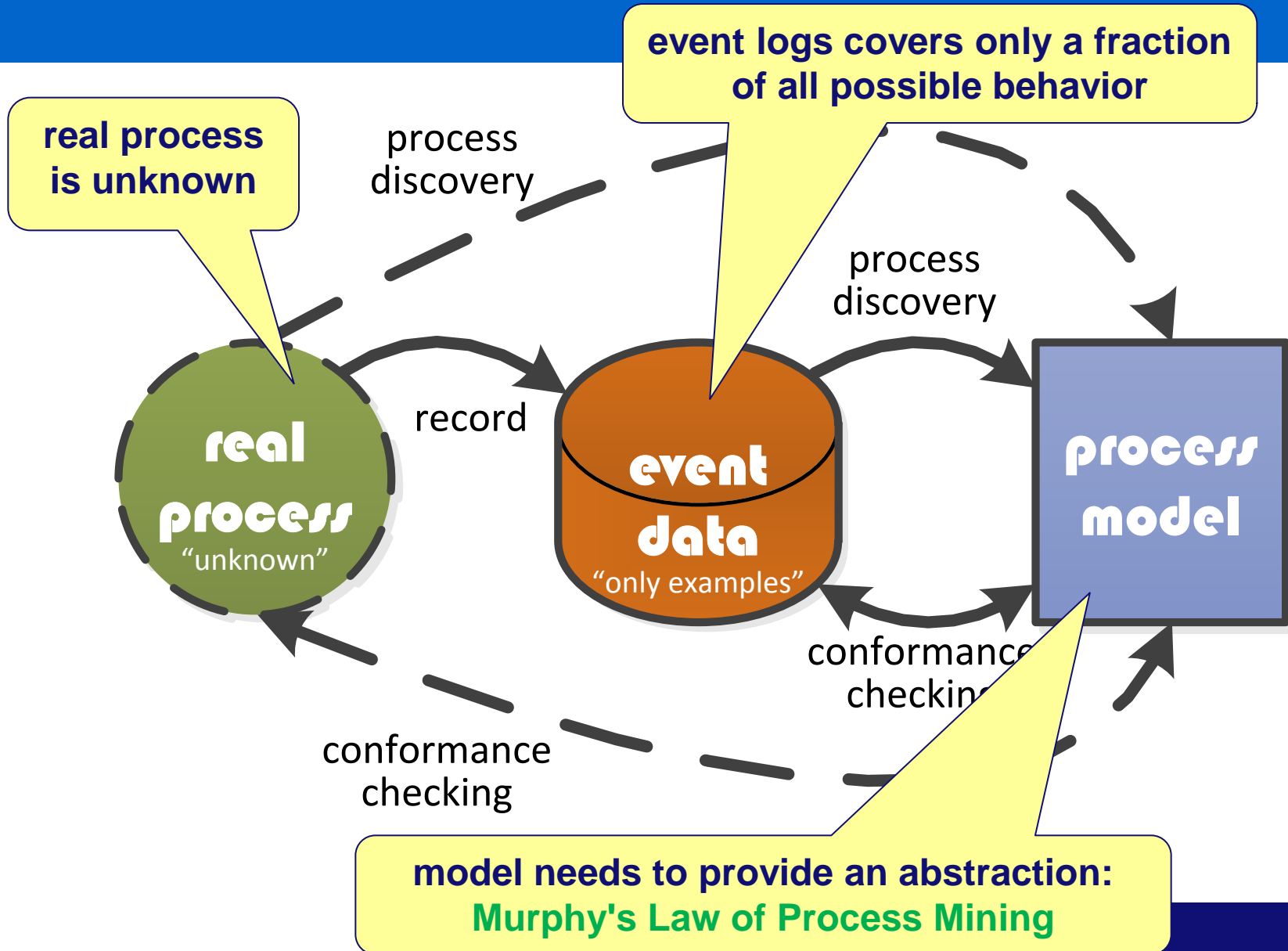
Conformance: Taking a Step Back

Conventional Conformance Notions

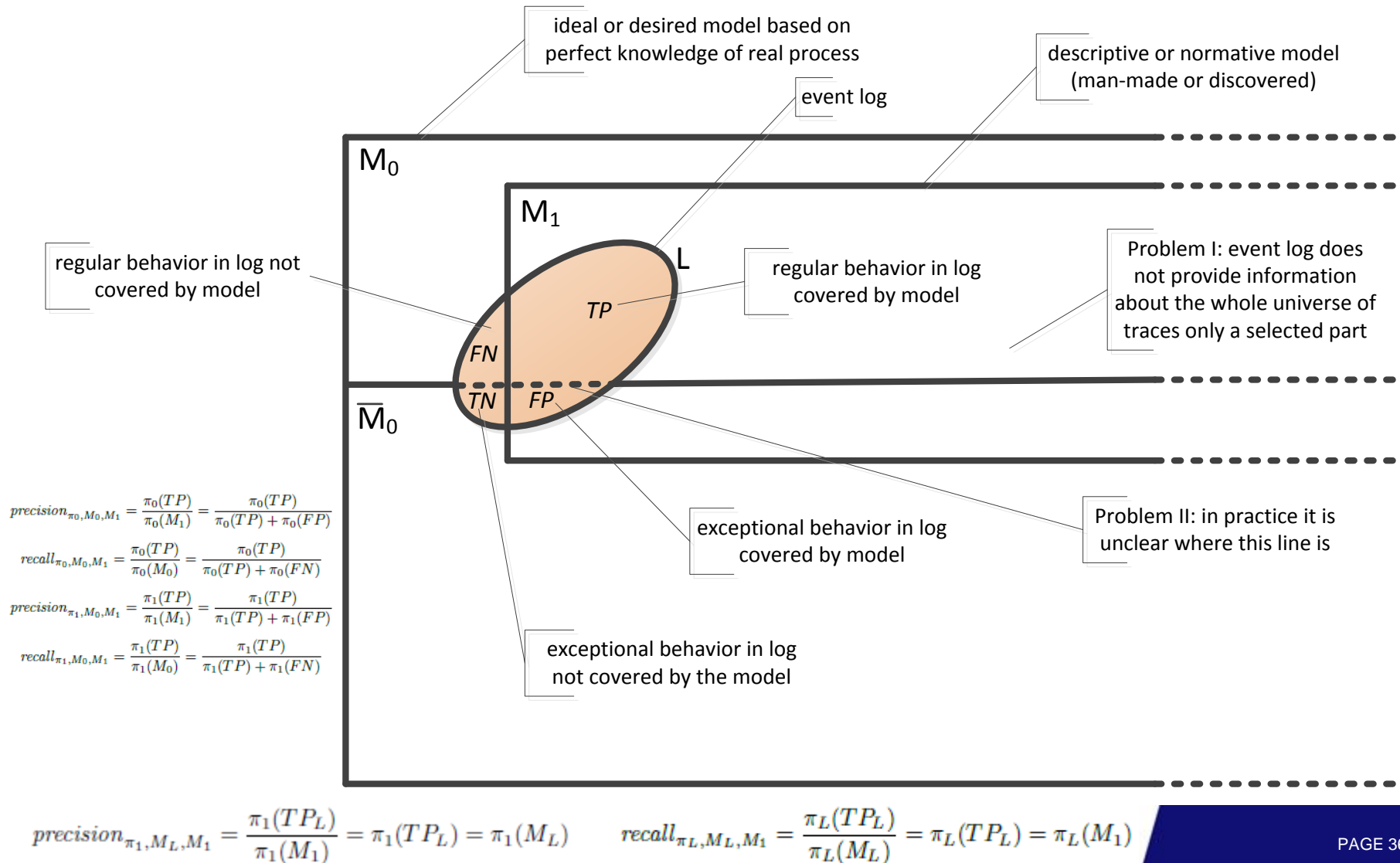


Leaving out one of these dimensions during discovery will lead to degenerate cases!

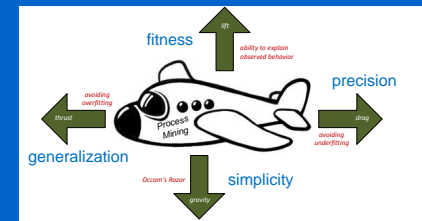
Problem



Traditional Notions such as Precision and Recall do NOT Apply



Operationalizing the Four Conformance dimensions



- **Fitness** (fraction of observed behavior possible according to the model).
 - Measure at the case or event level.
 - How to continue after a deviation (where to put the "blame"), cf. duplicate and silent activities.
- **Precision** (avoiding underfitting; fraction of allowed behavior never observed).
 - Log only contains examples.
 - Metrics are e.g. based on escaping edges.
- **Generalization** (avoiding overfitting; probability that the next unseen case will not fit).
 - Reasoning about unseen behavior, strongly related to log completeness.
- **Simplicity** (Occam's Razor: the simplest of two or more competing theories is preferable)
 - Easy to operationalize (e.g., number of nodes or arcs).
 - Often subjective (valuation of AND/XOR/OR-split/joins).

Some pointers

- **Wil M. P. van der Aalst: Mediating Between Modeled and Observed Behavior: The Quest for the “Right” Process. Seventh IEEE International Conference on Research Challenges in Information Science (RCIS 2013), (2013)**
- **Wil M. P. van der Aalst, Arya Adriansyah, Boudewijn F. van Dongen: Replaying history on process models for conformance checking and performance analysis. Wiley Interdisc. Rev.: Data Mining and Knowledge Discovery 2(2): 182-192 (2012)**
- **Joos C. A. M. Buijs, Boudewijn F. van Dongen, Wil M. P. van der Aalst: On the Role of Fitness, Precision, Generalization and Simplicity in Process Discovery. OTM Conferences (1) 2012: 305-322**
- **Wil M. P. van der Aalst: Process Mining - Discovery, Conformance and Enhancement of Business Processes. Springer 2011, isbn 978-3-642-19344-6, pp. I-XVI, 1-352**

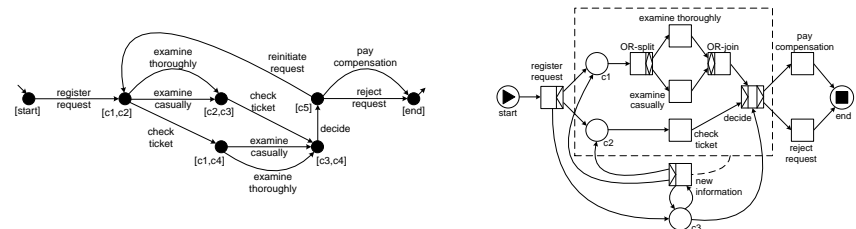
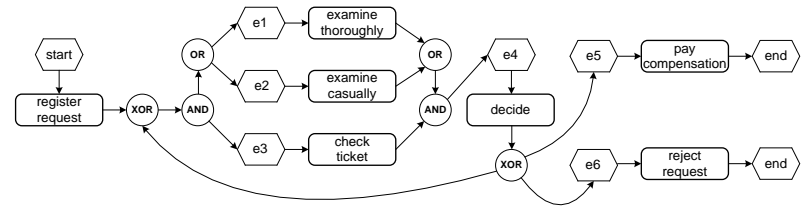
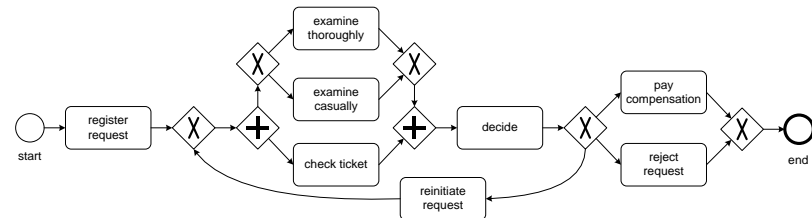
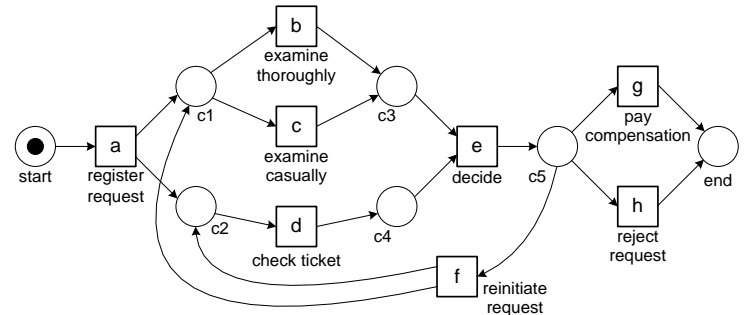
Representational Bias in Process Mining

(not about visualization)

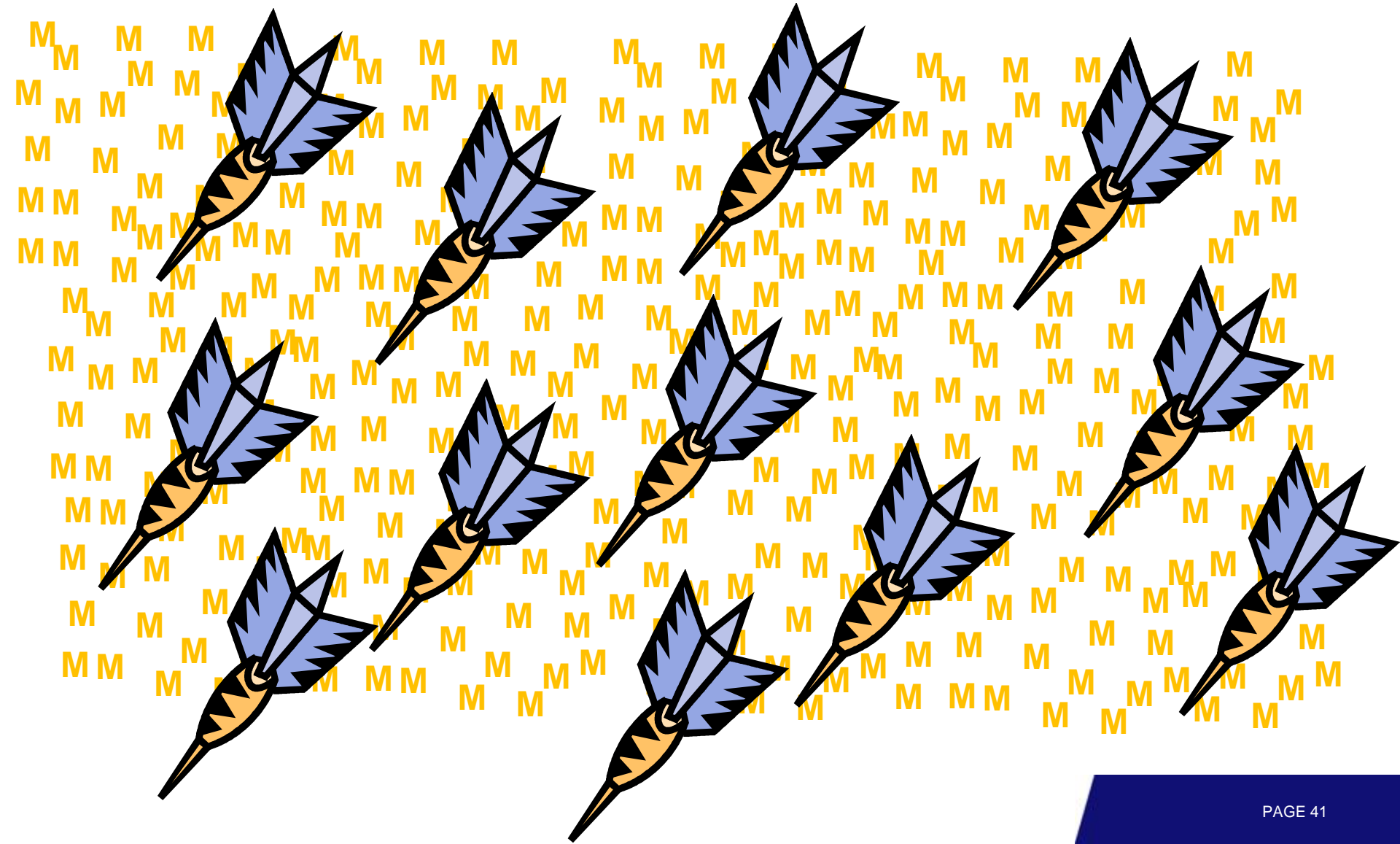
Joint work with Joos Buijs, Sander Leemans, and Boudewijn van Dongen.

Typical Representational Bias

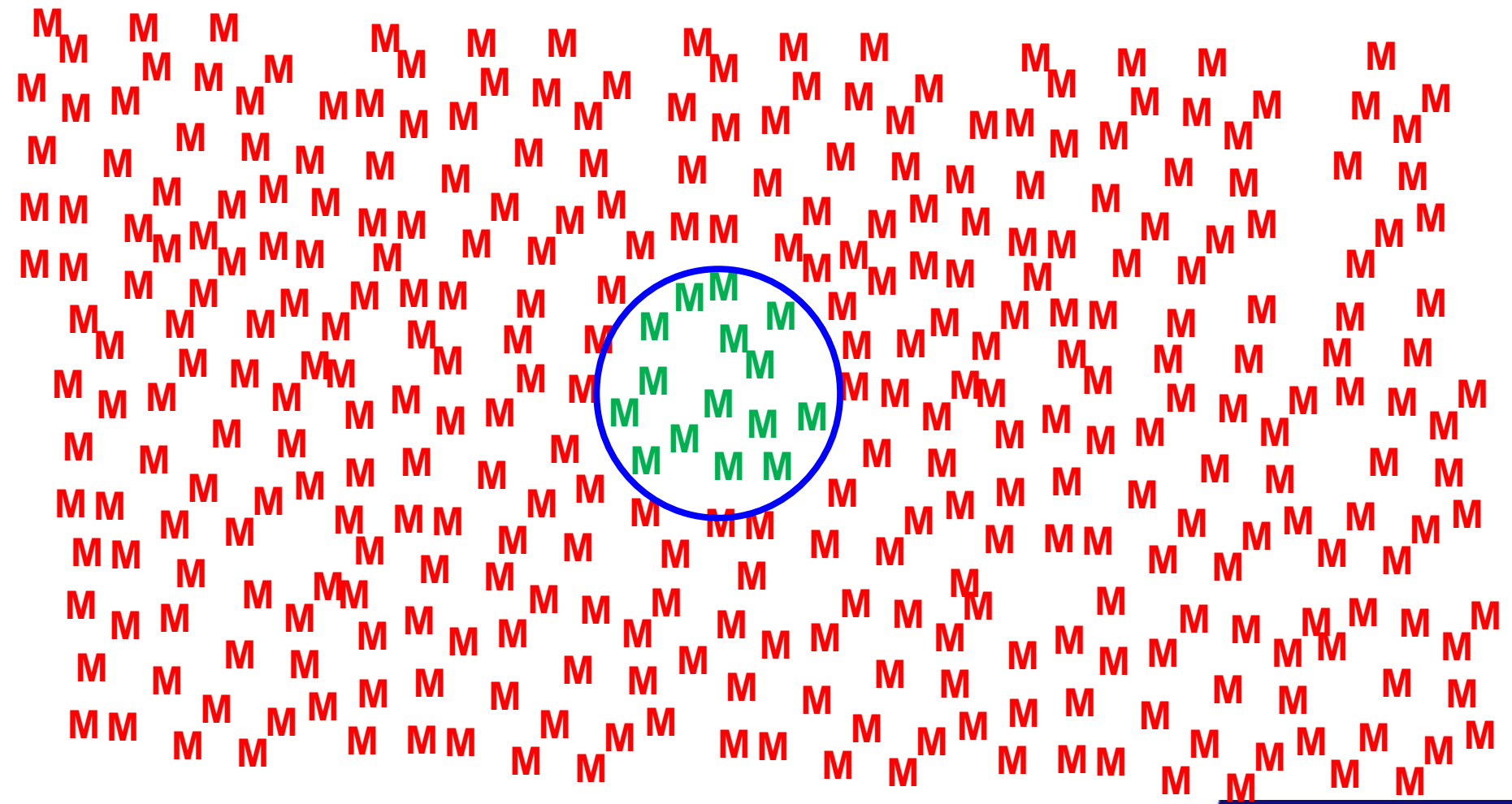
- (Labeled) Petri Nets, WF-nets, etc.
- Subsets of
 - BPMN diagrams,
 - UML Activity Diagrams,
 - Event-Driven Process Chains (EPCs),
 - YAWL,
 - etc.
- Transition Systems
- (Hidden) Markov Models
- ...



Huge Search Space When Discovering a Petri Net, BPMN model, and the like ...

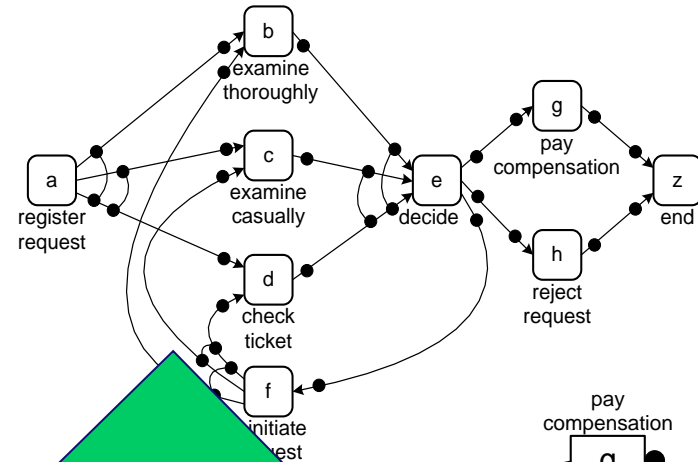


... with just a few interesting candidates

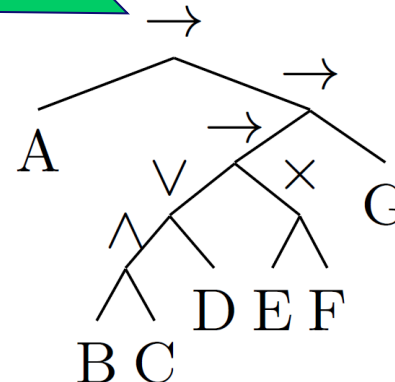
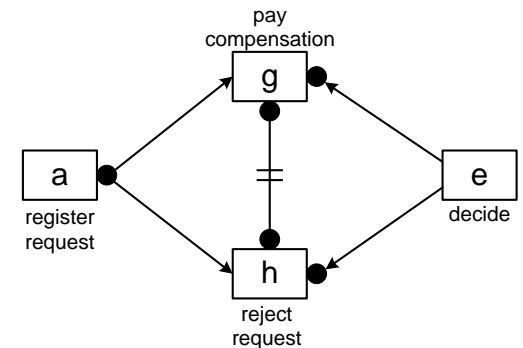


Alternative Representational Bias

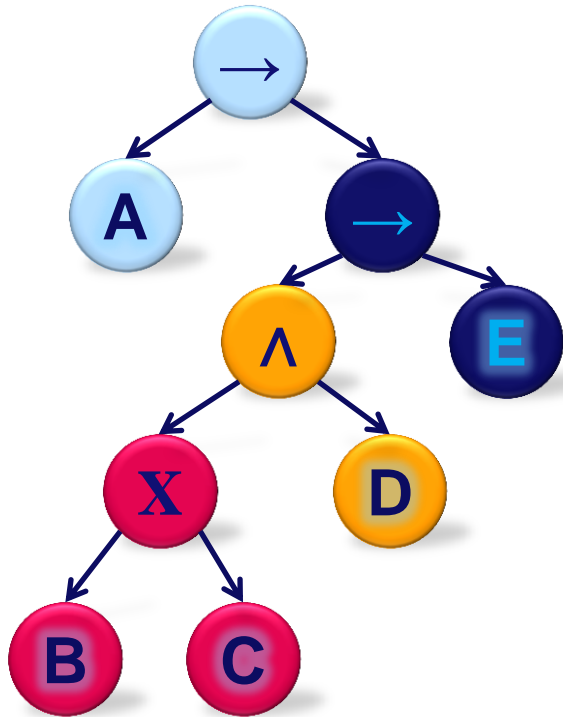
1. **C-nets** (XOR/AND/OR-split/join graphs; more likely to be sound due to declarative semantics).
2. **Declare models** (constraint based, grounded in LTL; anything is possible unless forbidden)
3. **Process Trees** (similar to subsets of various process algebras; sound by structure)



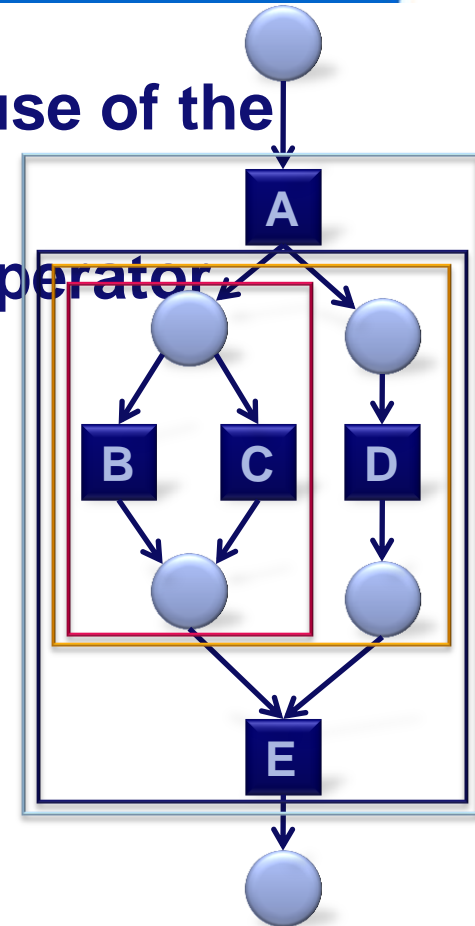
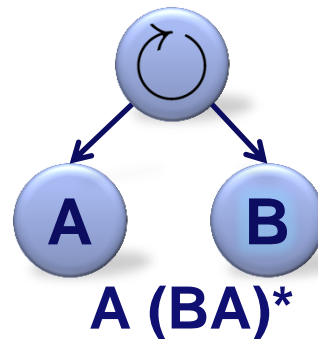
today's
focus



Another Representational Bias: Process Trees

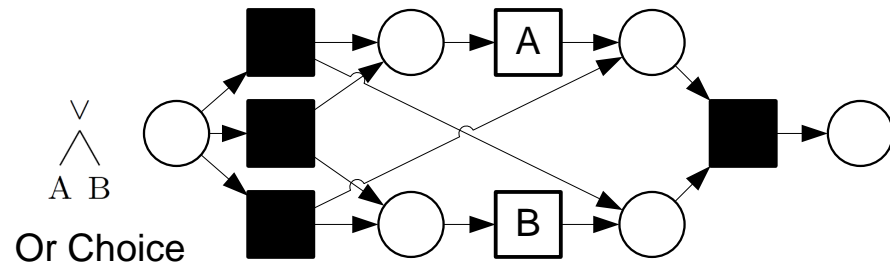
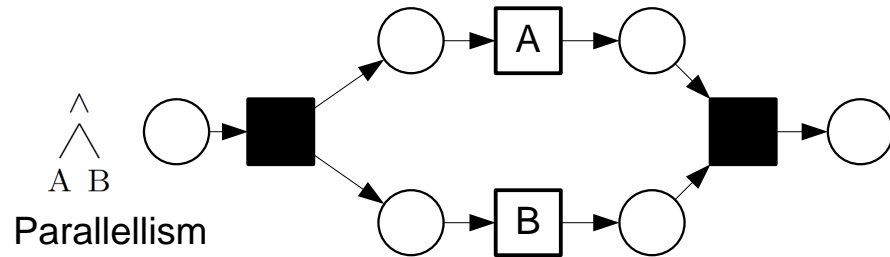
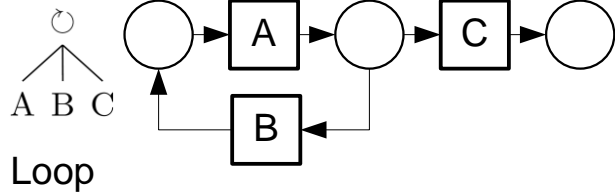
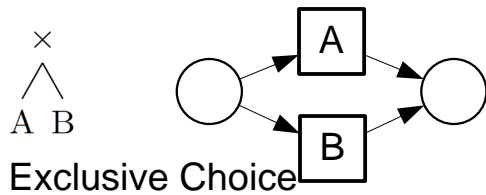
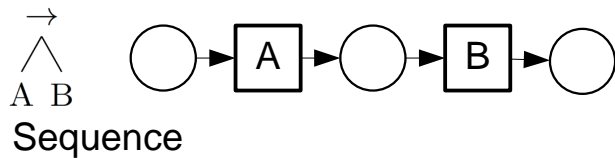


- Always sound because of the block structure
- Also Loop and OR operator

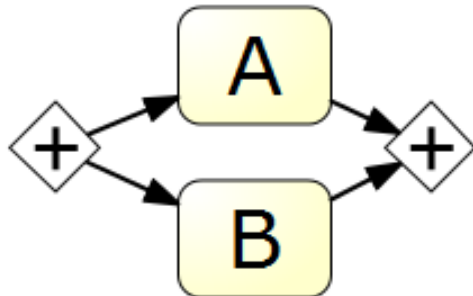
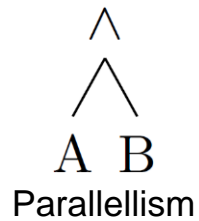
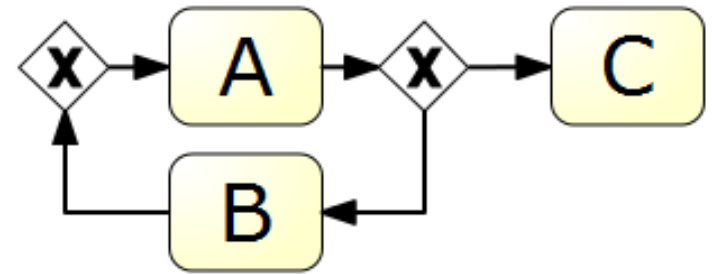
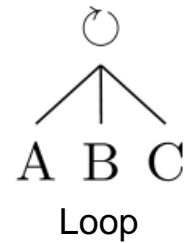
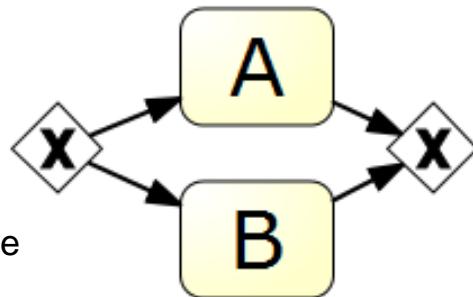
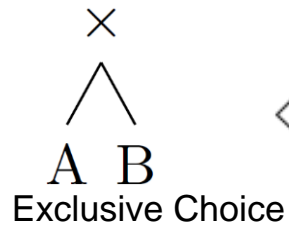
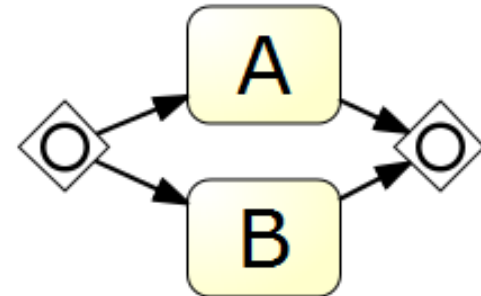
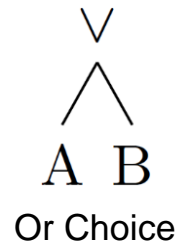
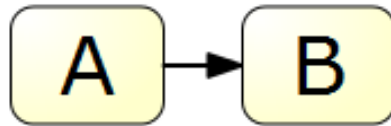
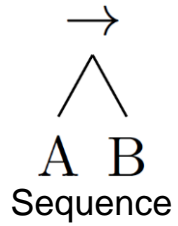


Petri Net Semantics

(used for comparison and conformance checking only)

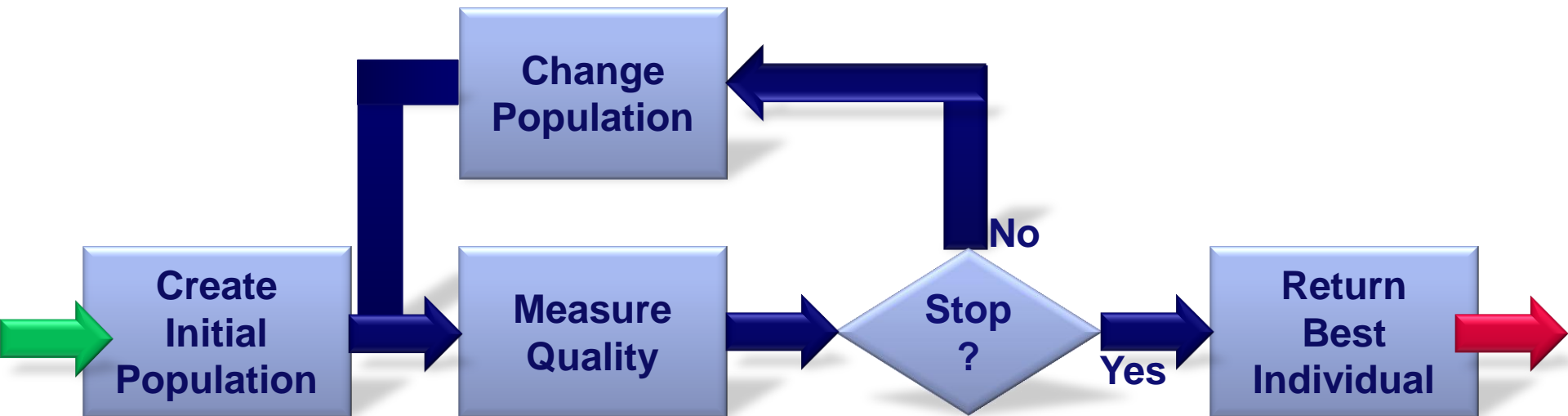


... and BPMN.

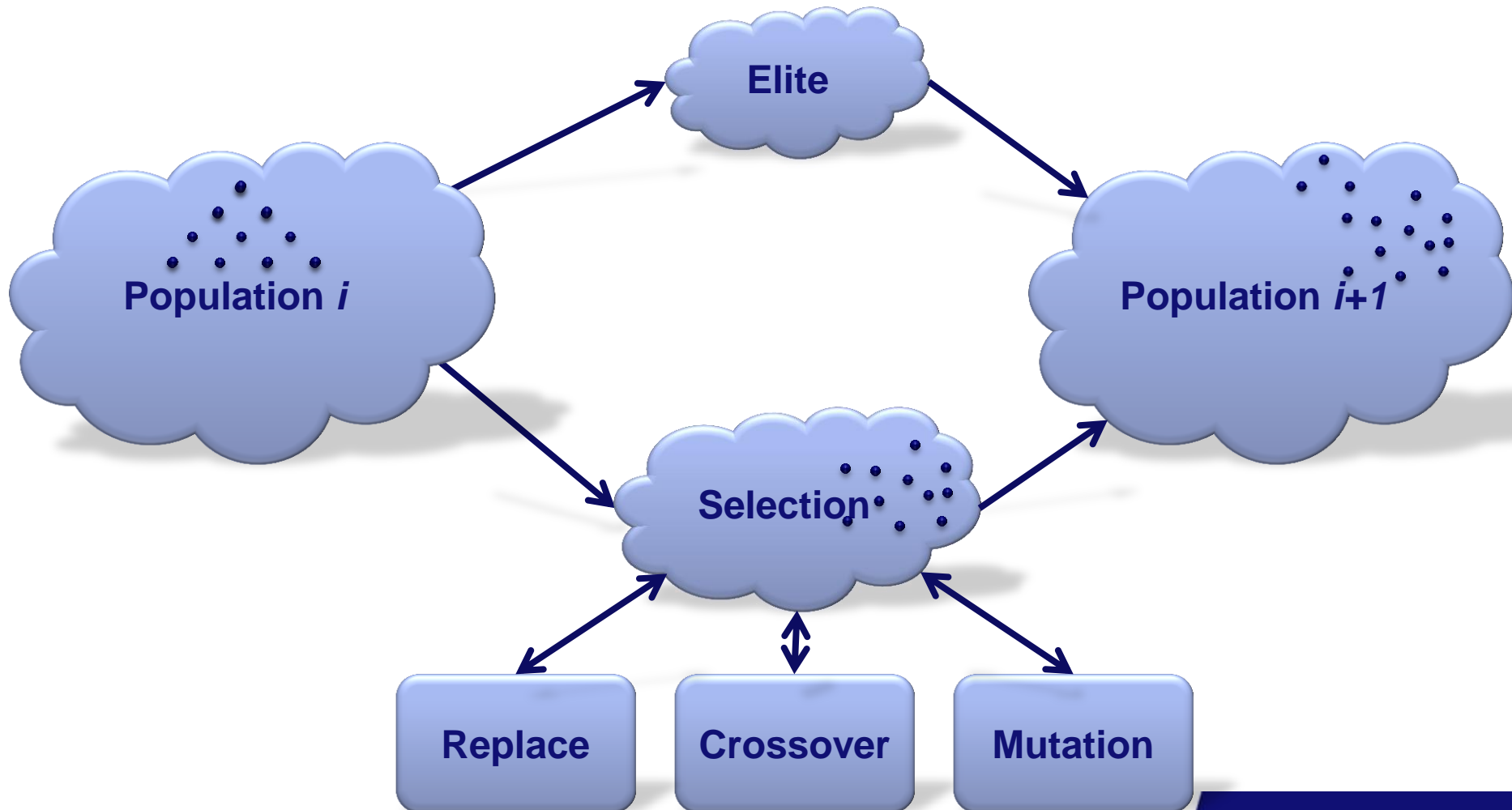


A Discovery Algorithm Using Process Trees: Evolutionary Tree Miner (ETM)

- **Process trees** as representation (= limit search space to "good" models).
- **Genetic** approach (= very flexible)
- Fitness function uses all **four criteria** (= seamlessly balance the different "forces")

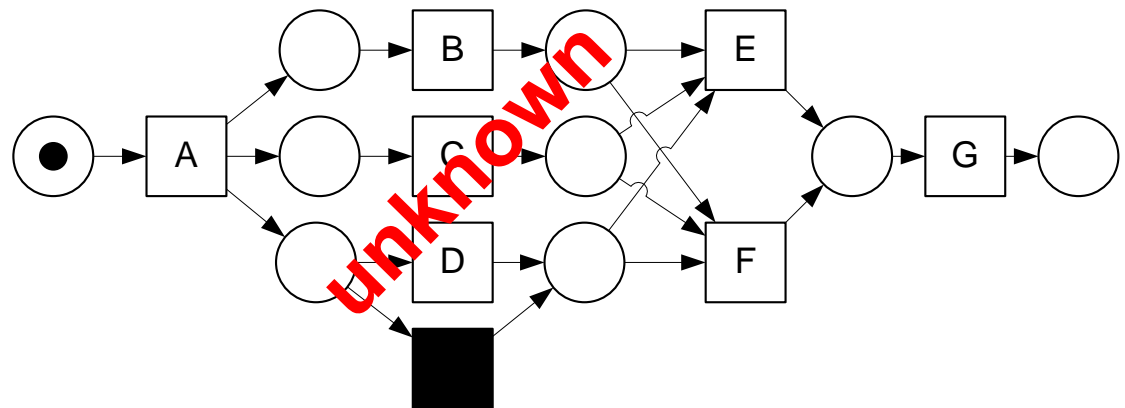


Population Change



Example

Trace	#
A B C D E G	6
A B C D F G	38
A B D C E G	12
A B D C F G	26
A B C F G	8
A C B E G	1
A D B C F G	1
A D B C E G	1
A D C B F G	4
A C D B F G	2
A C B F G	1

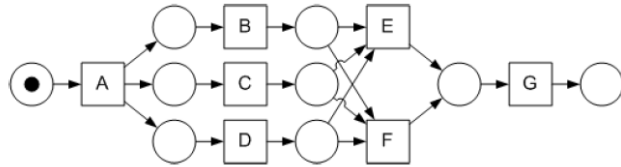


A = send e-mail, B = check credit,
 C = calculate capacity, D = check system,
 E = accept, F = reject, G = send e-mail

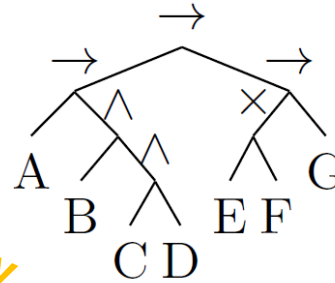
Conventional Algorithms (1/3)

("best effort" mapping to process trees to allow for comparison)

alpha miner



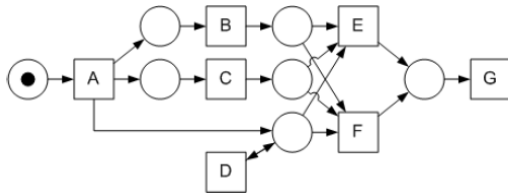
sound
... lucky



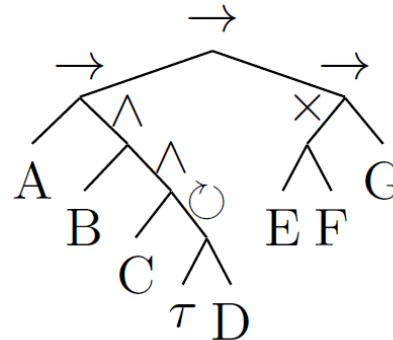
f: 0,992	p: 0,995
s: 1,000	g: 0,889

low fitness

ILP miner



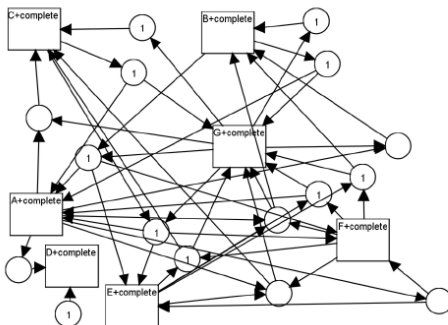
sound



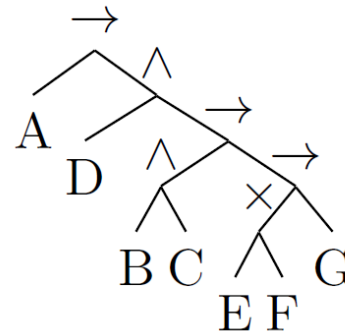
f: 1,000	p: 0,784
s: 0,933	g: 0,830

low precision

language-based region miner



sound

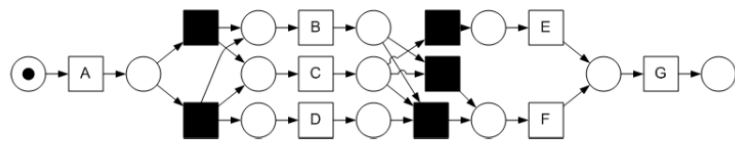


f: 0,992	p: 0,957
s: 1,000	g: 0,889

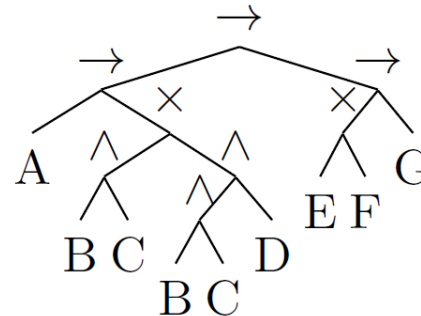
low fitness

Conventional Algorithms (2/3)

heuristic miner

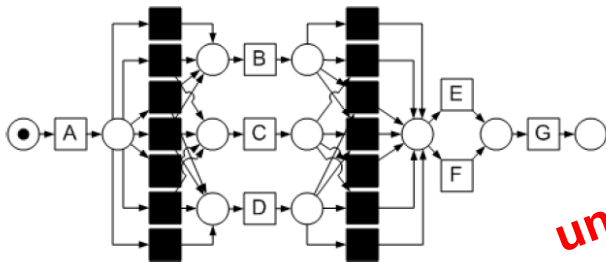


unsound

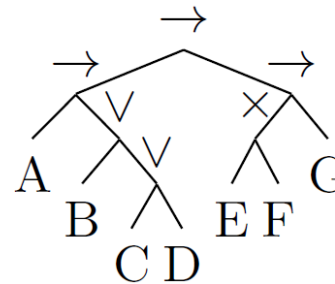


f: 1,000	p: 0,986
s: 0,875	g: 0,852

multi-phase miner



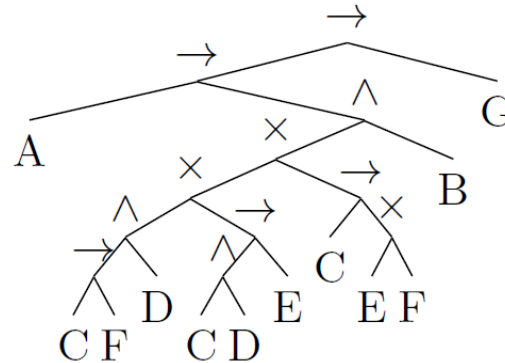
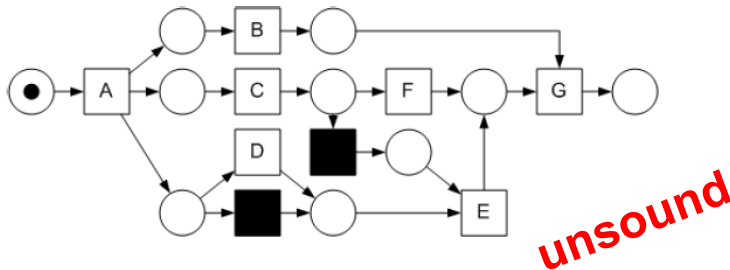
unsound
(relaxed
sound)



f: 1,000	p: 0,830
s: 1,000	g: 0,889

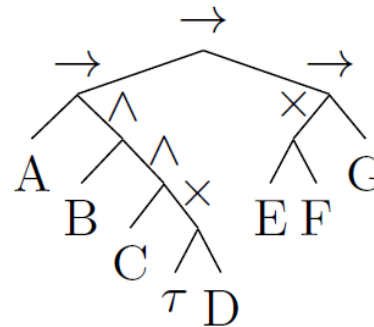
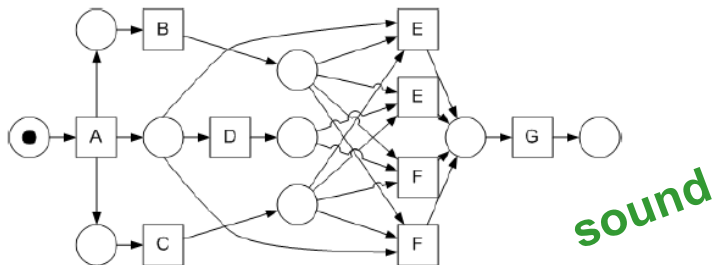
Conventional Algorithms (3/3)

genetic miner



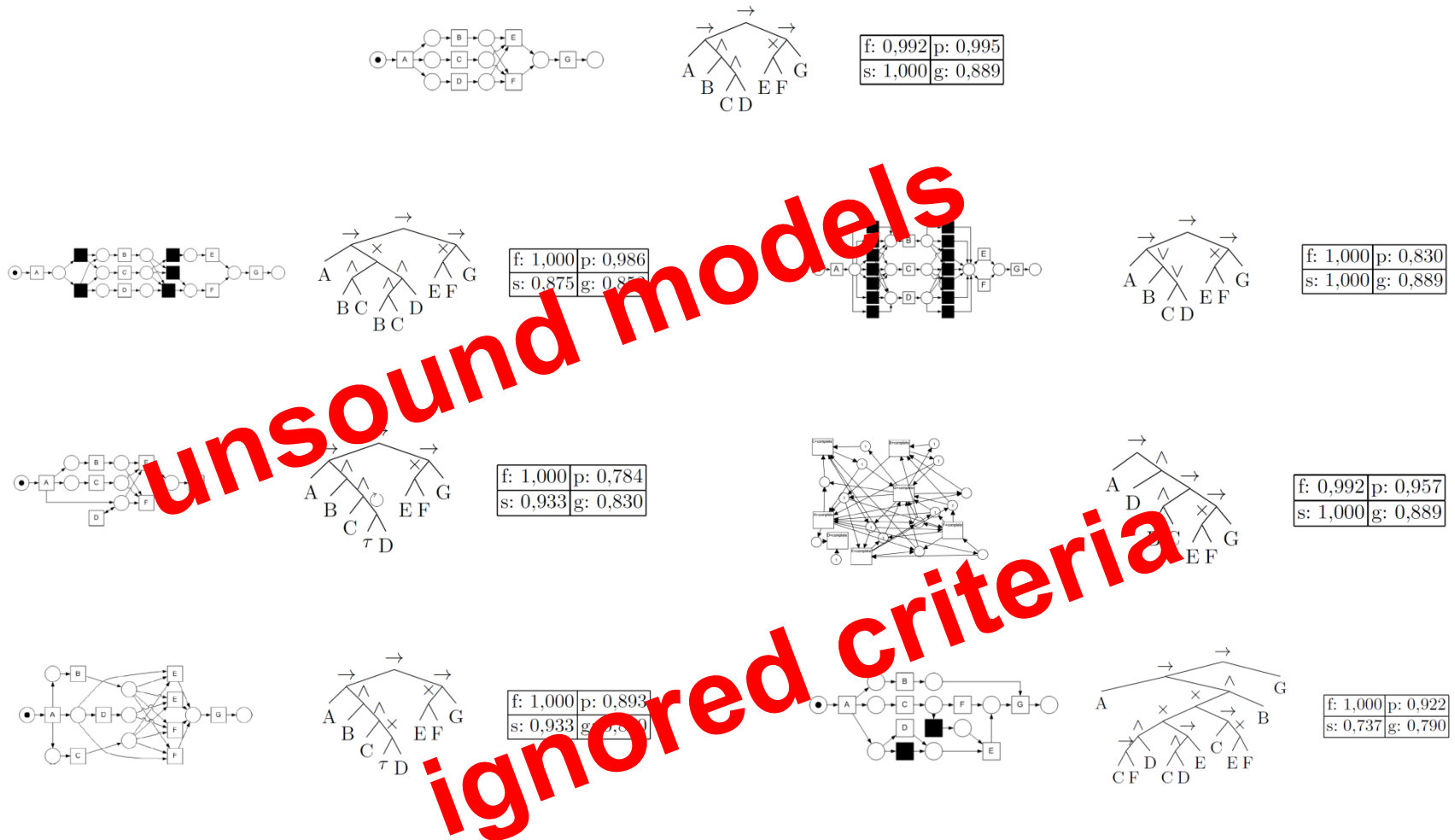
f: 1,000	p: 0,922
s: 0,737	g: 0,790

state-based region miner

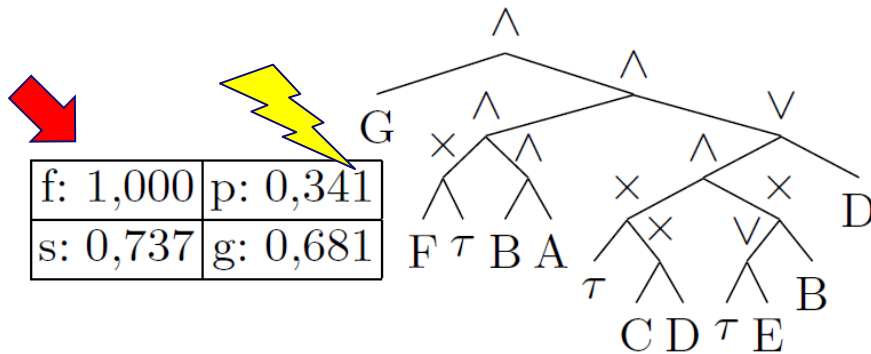


f: 1,000	p: 0,893
s: 0,933	g: 0,830

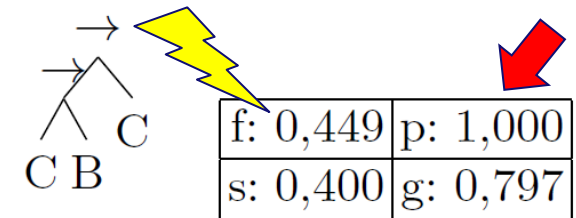
Often unsound result and no mechanism to seamlessly balance the four criteria



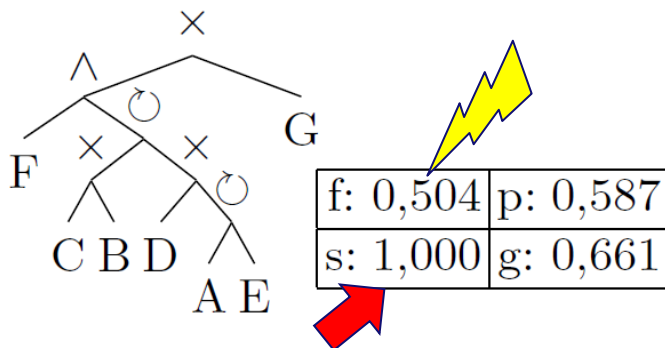
Genetic Mining (ETM) While Considering Only One Criterion



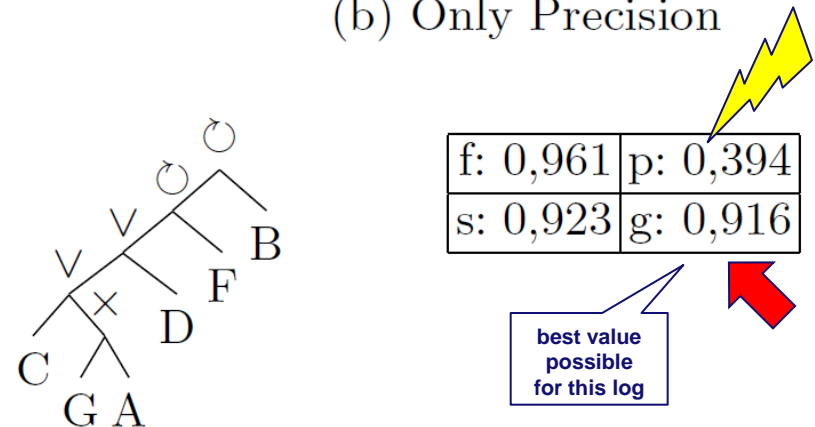
(a) Only replay fitness



(b) Only Precision

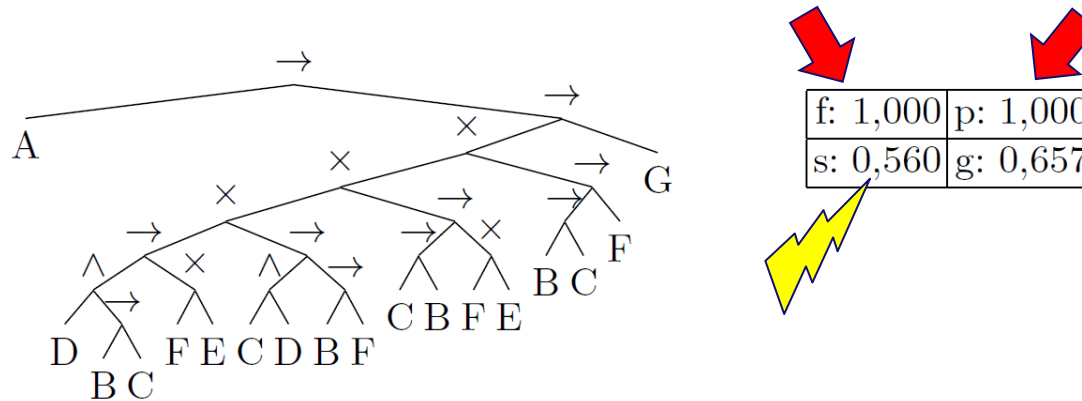


(c) Only Simplicity

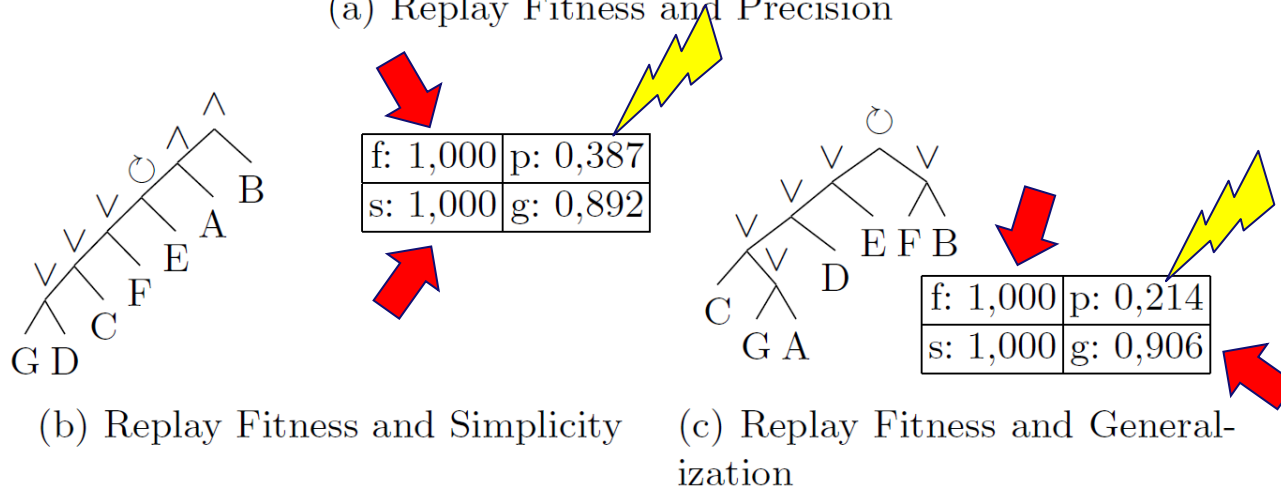


(d) Only Generalization

Considering Replay Fitness and One Other Criterion



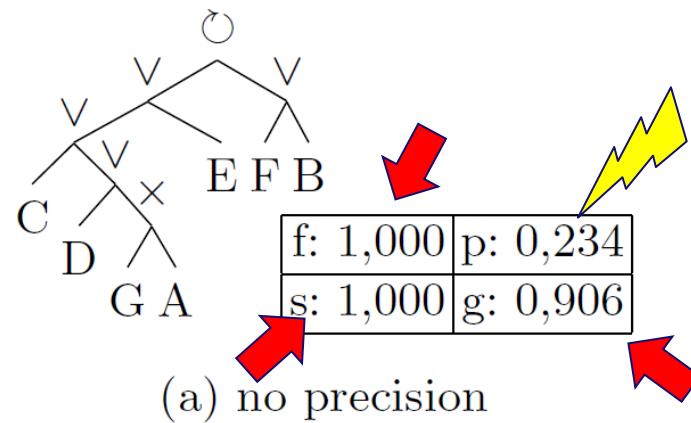
(a) Replay Fitness and Precision



(b) Replay Fitness and Simplicity

(c) Replay Fitness and Generalization

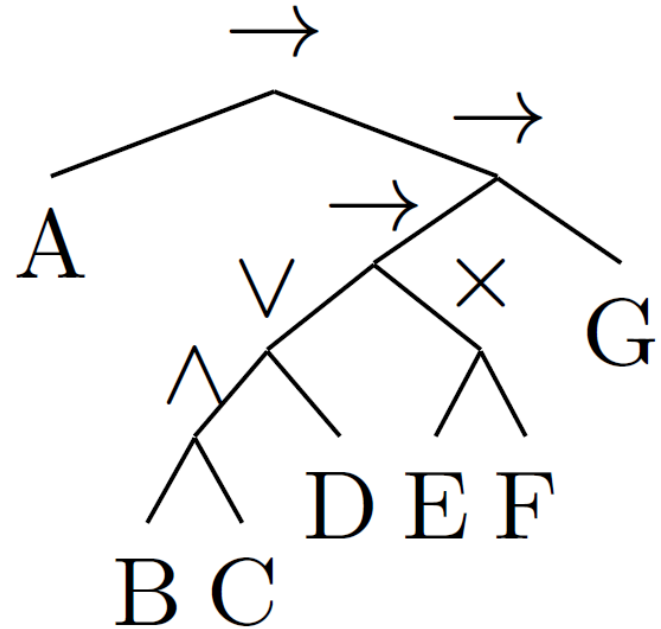
Considering 3 of 4 Criteria



replay fitness needs to have a larger weight

Considering All Four Criteria with Emphasis on Fitness

f: 1,000	p: 0,923
s: 1,000	g: 0,889



fitness has weight 10

Initial Model Versus Discovered Model

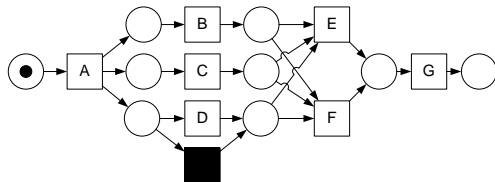
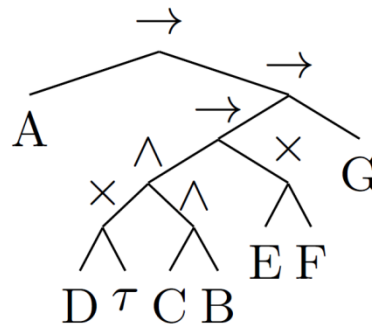
Better than existing algorithms (but patience is needed)!

Trace	#
A B C D E G	6
A B C D F G	38
A B D C E G	12
A B D C F G	26
A B C F G	8
A C B E G	1
A D B C F G	1
A D B C E G	1
A D C B F G	4
A C D B F G	2
A C B F G	1

Discovered model outperforms initial model with respect to all criteria!

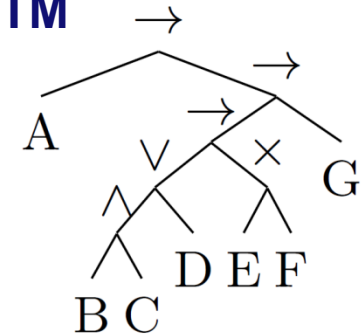
simulated

f: 1,000	p: 0,893
s: 0,933	g: 0,830



discovered by ETM

f: 1,000	p: 0,923
s: 1,000	g: 0,889



1) Carefully choose your representational bias during discovery: Unrelated to presentation/visualization!

Lessons
Learned

2) Consider all conformance dimensions (replay fitness, precision, generalization, and simplicity)!

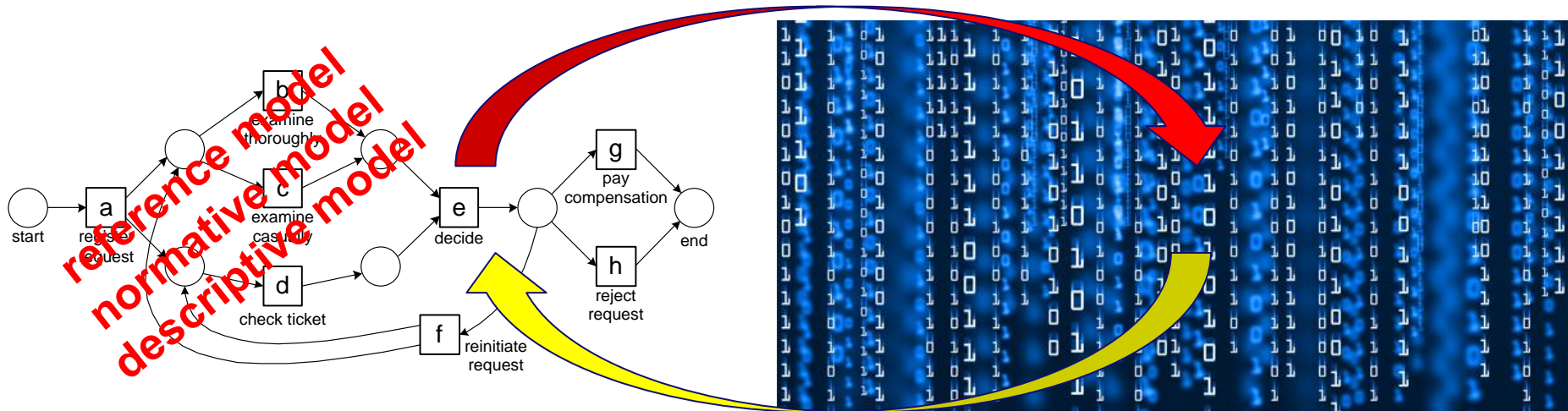
Some pointers

- **Wil M. P. van der Aalst, Arya Adriansyah, Boudewijn F. van Dongen: Causal Nets: A Modeling Language Tailored towards Process Discovery. CONCUR 2011: 28-42**
- **Joos C. A. M. Buijs, Boudewijn F. van Dongen, Wil M. P. van der Aalst: On the Role of Fitness, Precision, Generalization and Simplicity in Process Discovery. OTM Conferences (1) 2012: 305-322**
- **Joos C. A. M. Buijs, Boudewijn F. van Dongen, Wil M. P. van der Aalst: A genetic algorithm for discovering process trees. IEEE Congress on Evolutionary Computation 2012: 1-8**
- **S.J.J. Leemans, D. Fahland, W.M.P. van der Aalst. Discovering Block-Structured Process Models From Event Logs – A Constructive Approach. BPM Center Report BPM-13-06, BPMcenter.org, 2013**

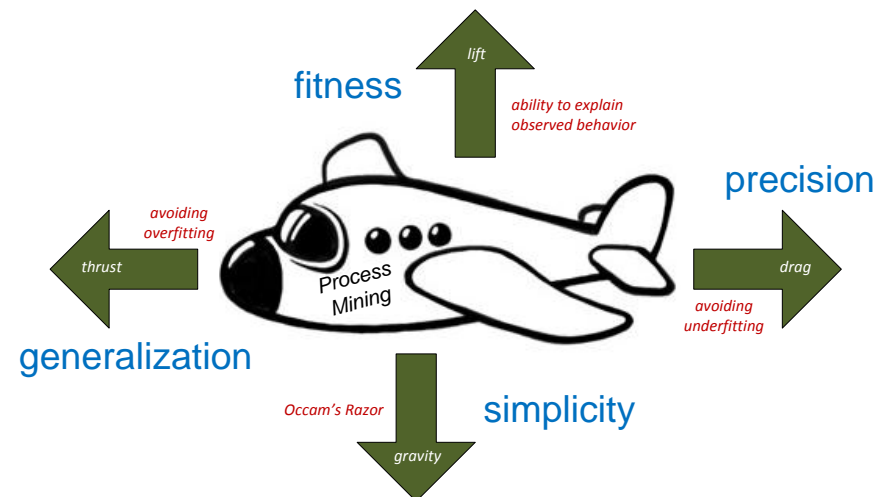
Mediating Between a Reference Model and Real Observed Behavior

Joint work with Joos Buijs, Boudewijn van Dongen, and Dirk Fahland.

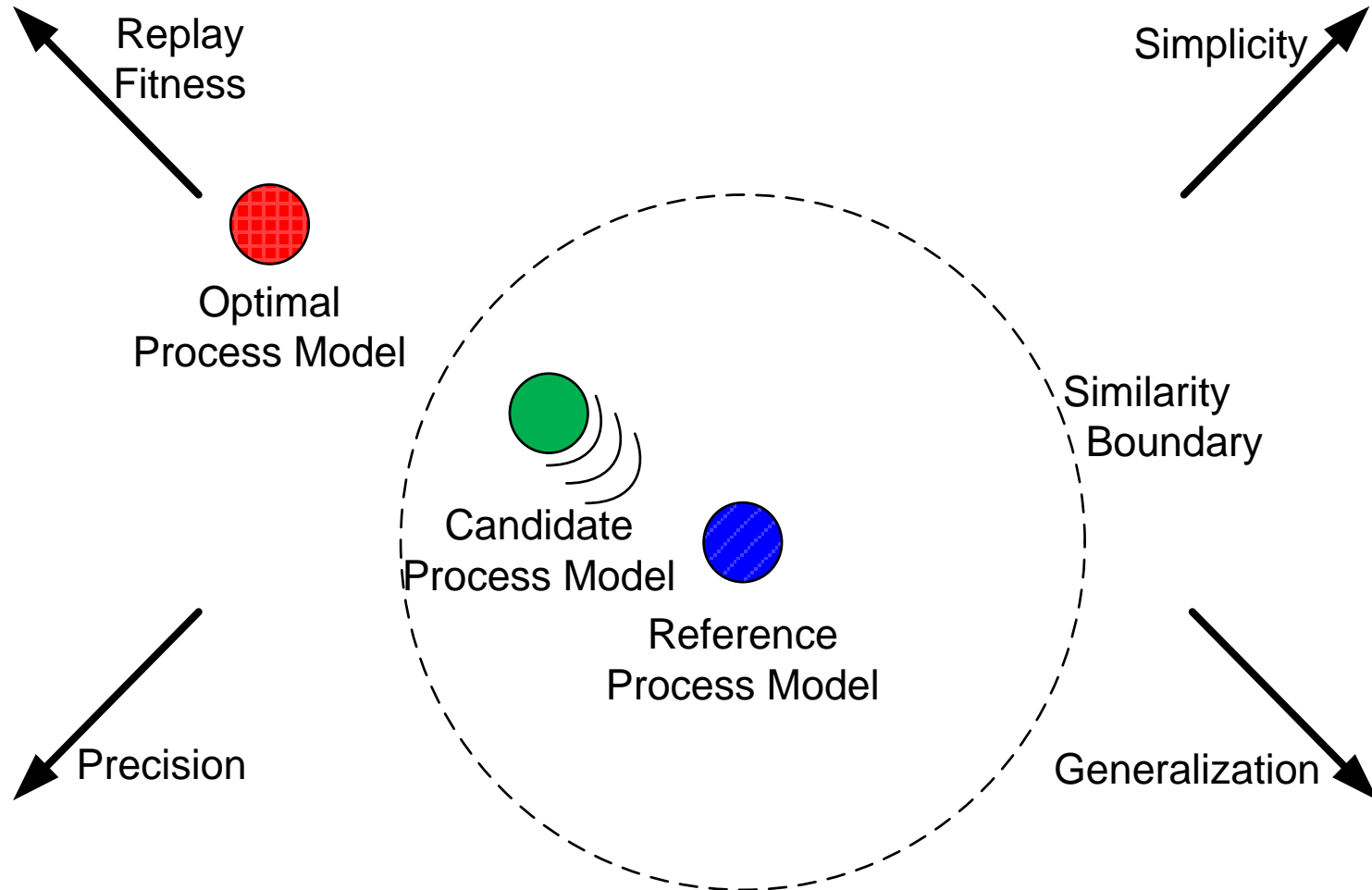
Compromise Based on Two Main Forces



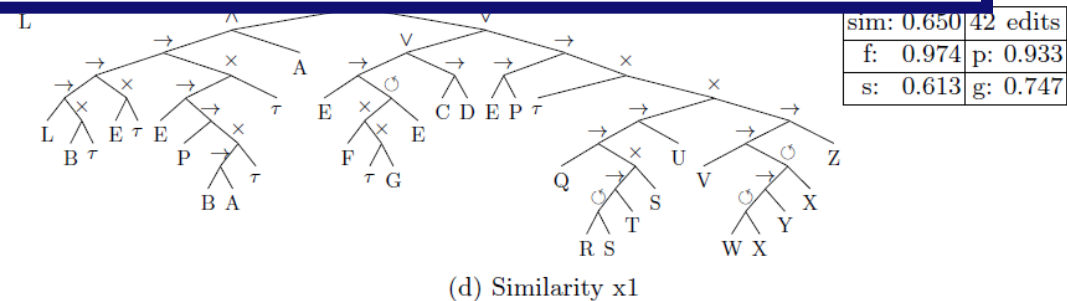
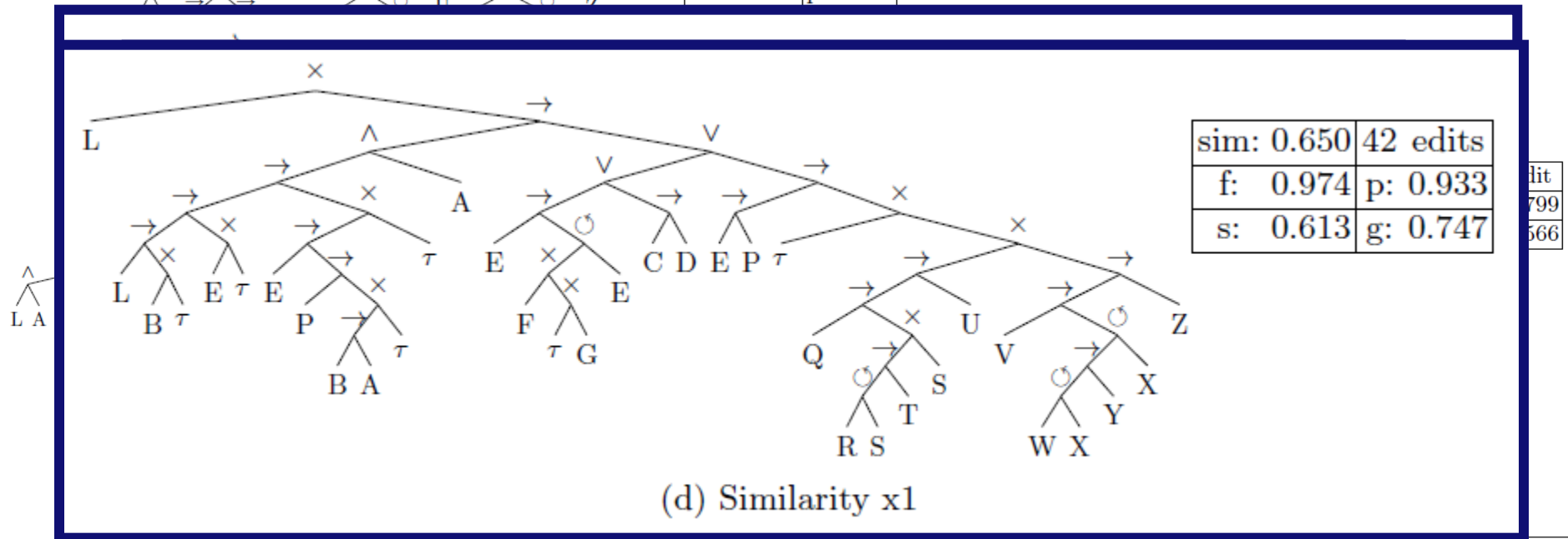
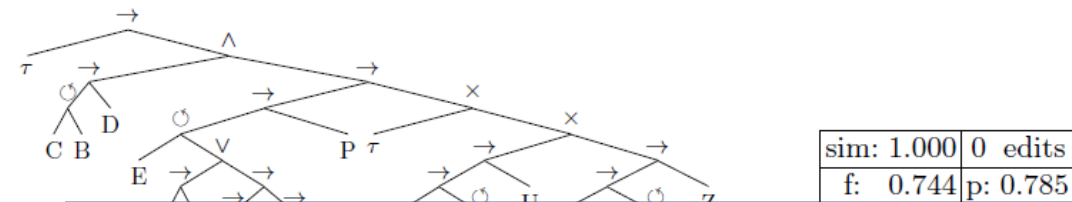
Various techniques to compare graphs, e.g., edit distance notions (add, remove, replace).



Force Between Reference Model and Candidate Model Can be Viewed as a 5th Conformance Notion



Example From CoSeLoG Project



Some pointers

- J.C.A.M. Buijs ,M. La Rosa, H.A. Reijers, B.F. van Dongen, and W.M.P. van der Aalst: Improving Business Process Models using Observed Behavior, SIMPDA 2012 post-proceedings, Lecture Notes in Business Information Processing, 2013.
- Joos C. A. M. Buijs, Boudewijn F. van Dongen, Wil M. P. van der Aalst: On the Role of Fitness, Precision, Generalization and Simplicity in Process Discovery. OTM Conferences (1) 2012: 305-322
- Dirk Fahland, Wil M. P. van der Aalst: Repairing Process Models to Reflect Reality. BPM 2012: 229-245.
- Dirk Fahland, Wil M. P. van der Aalst: Simplifying discovered process models in a controlled manner. Inf. Syst. 38(4): 585-605 (2013).

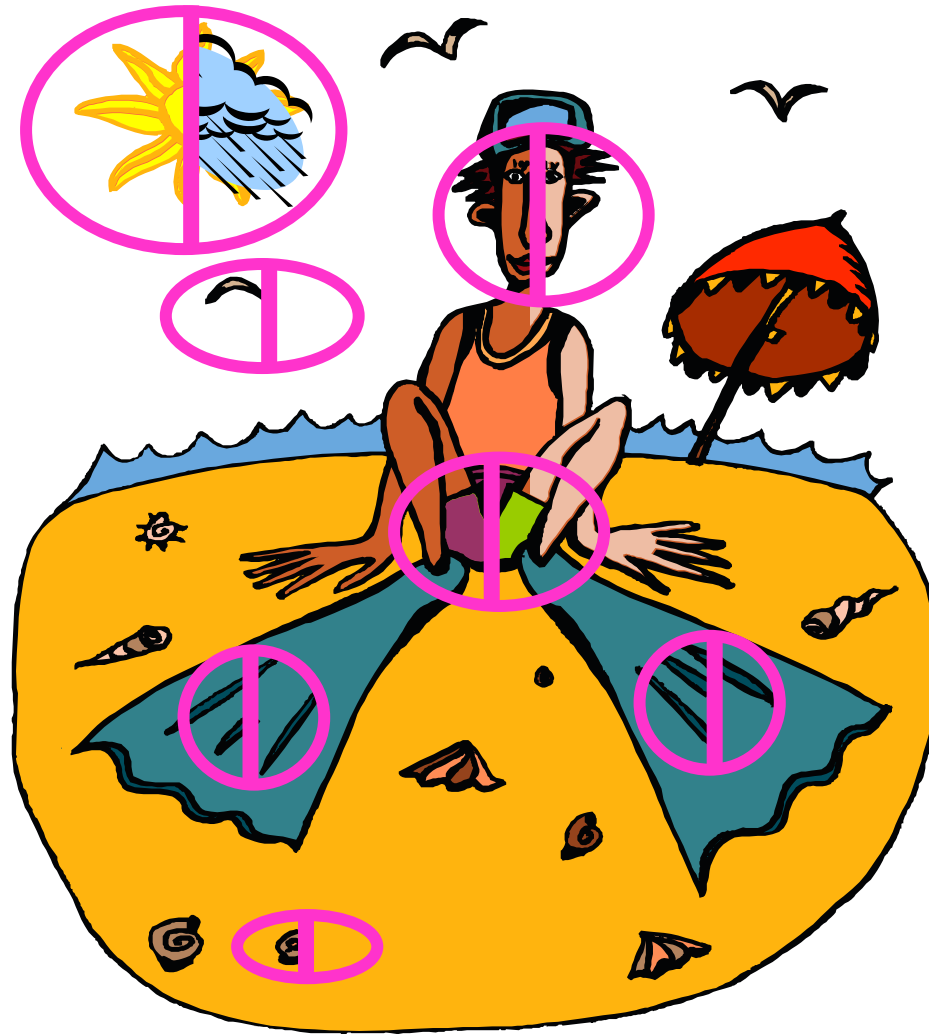
Mining Configurable Process Models

Joint work with Joos Buijs, Boudewijn van Dongen, and Florian Gottschalk.

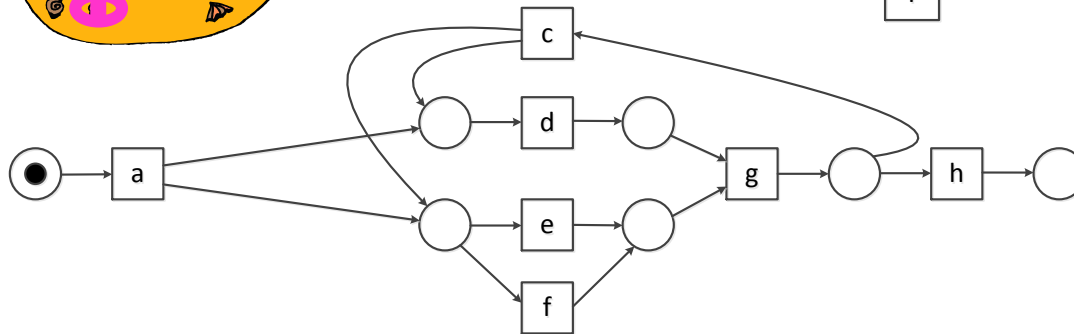
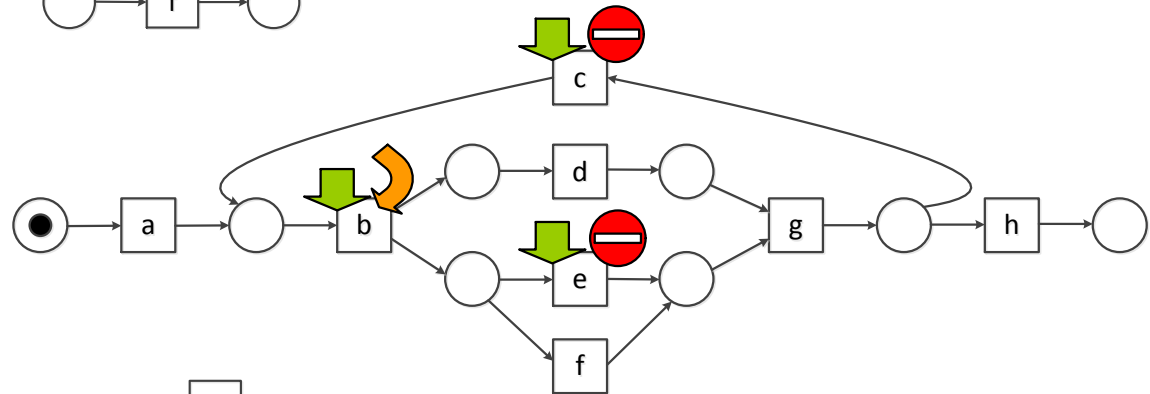
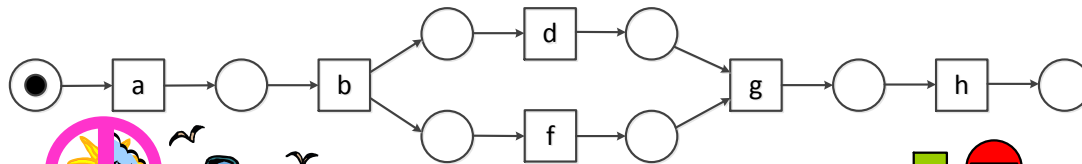
Two variants of the same process ...



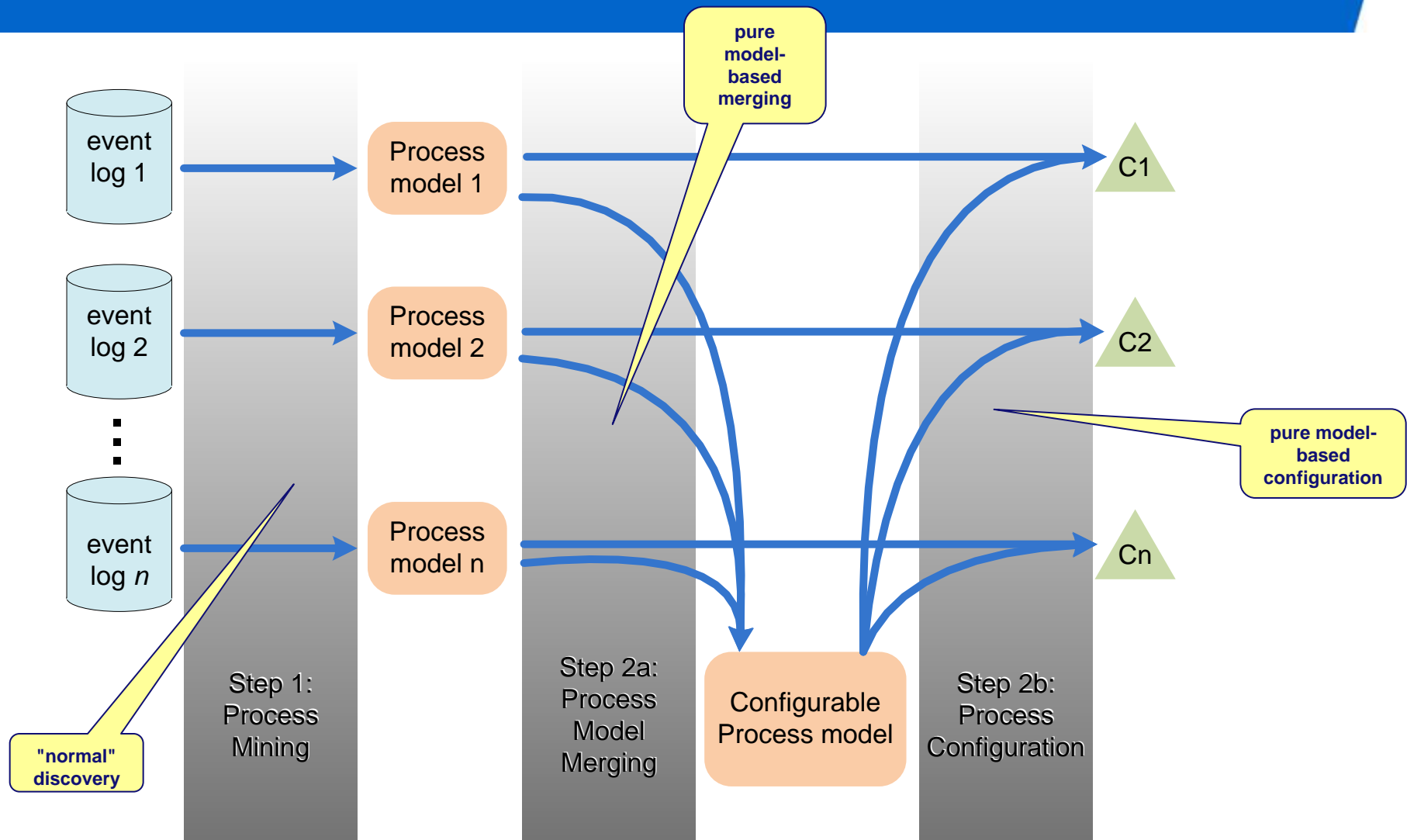
Configurable Process Model



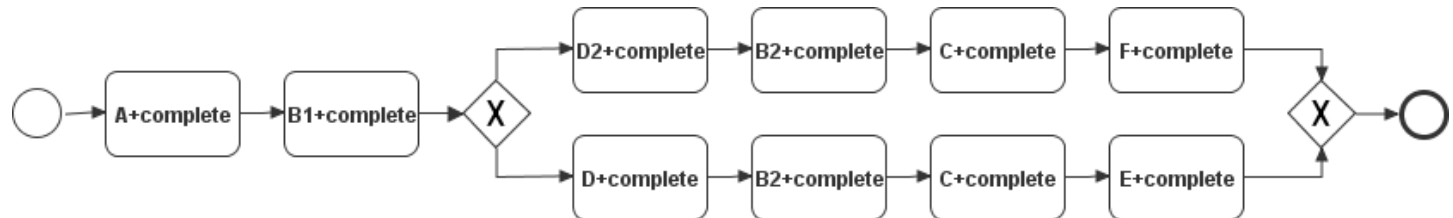
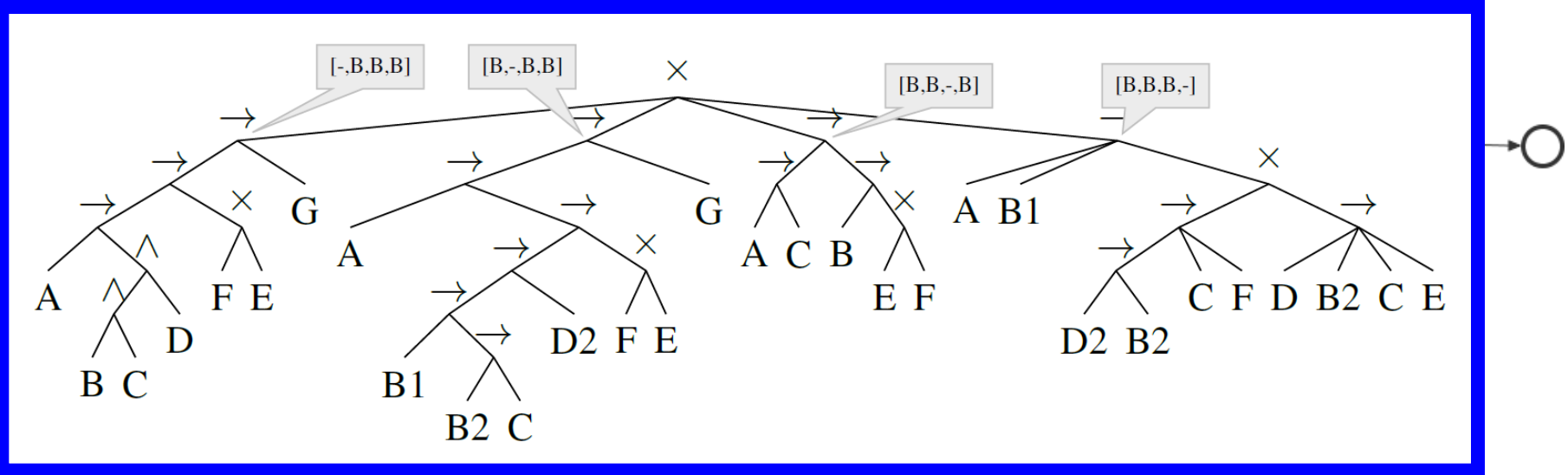
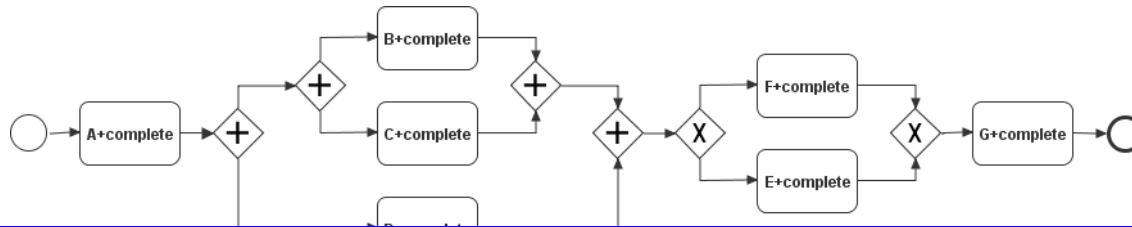
Variants of the same process



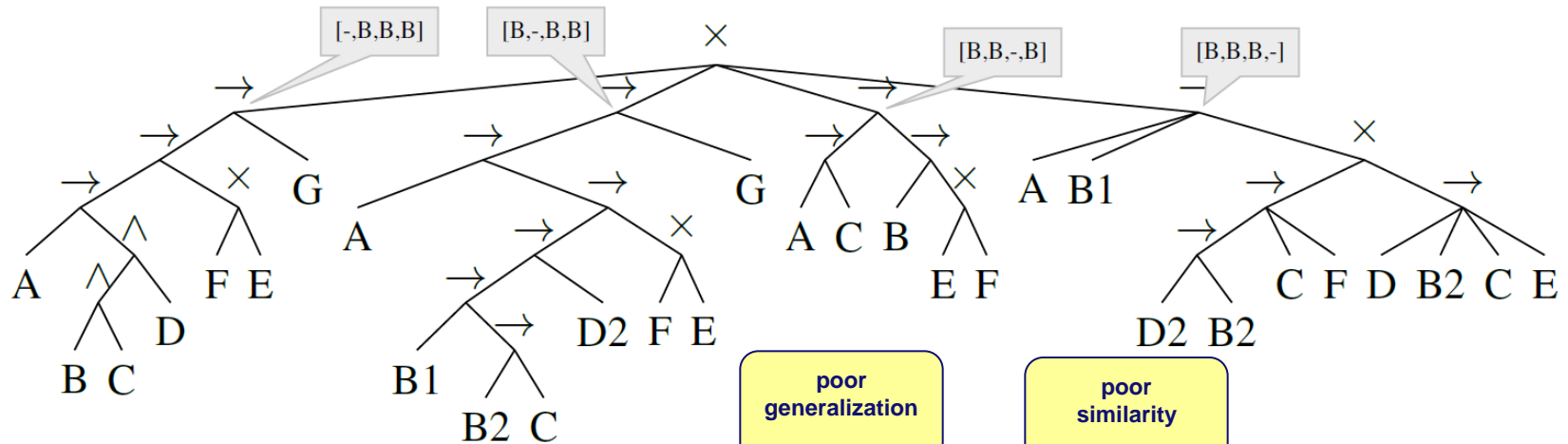
Approach 1: Merge Separately Mined Models



Results Approach 1 for running example

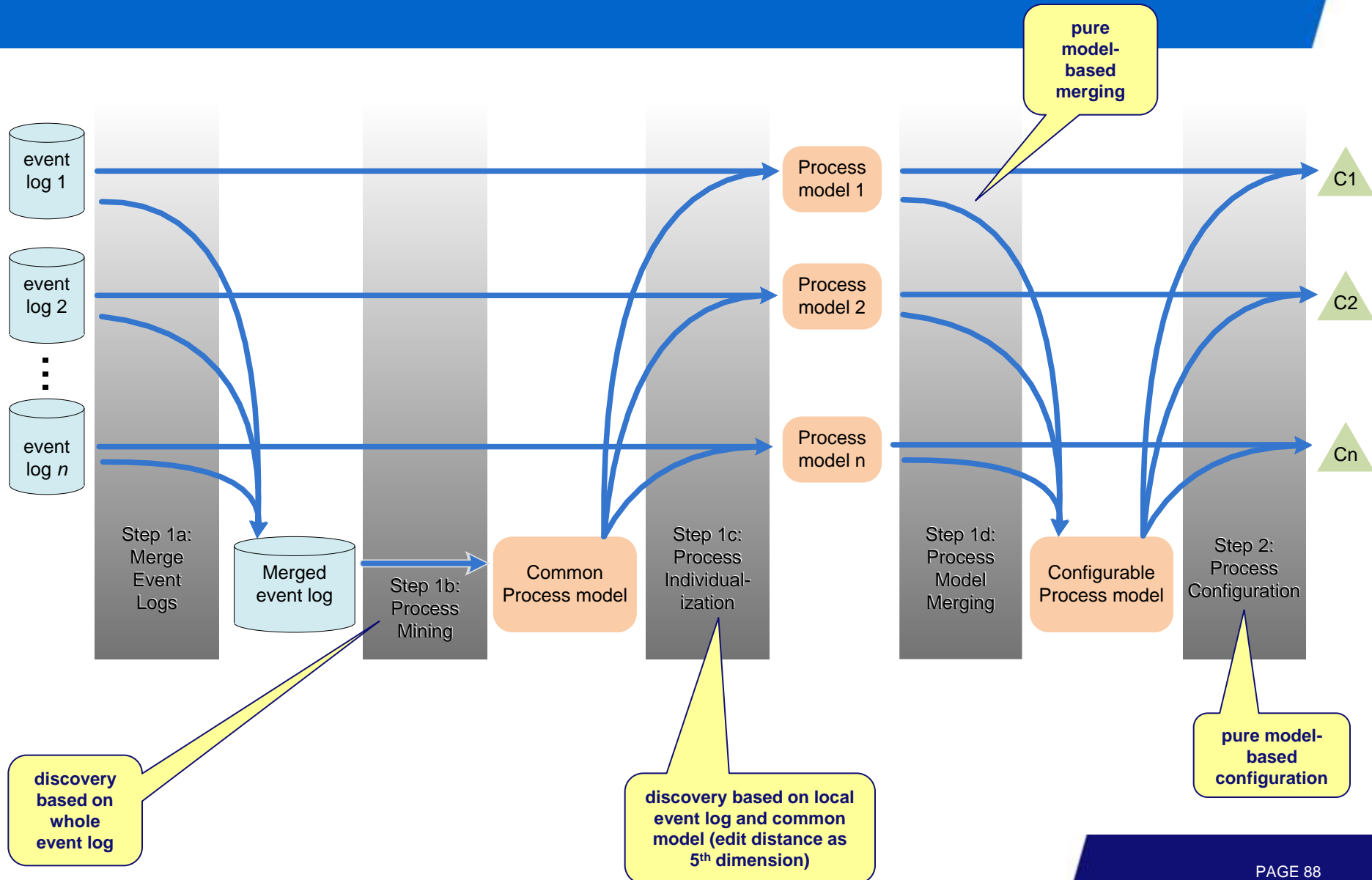


Results Approach 1 for running example

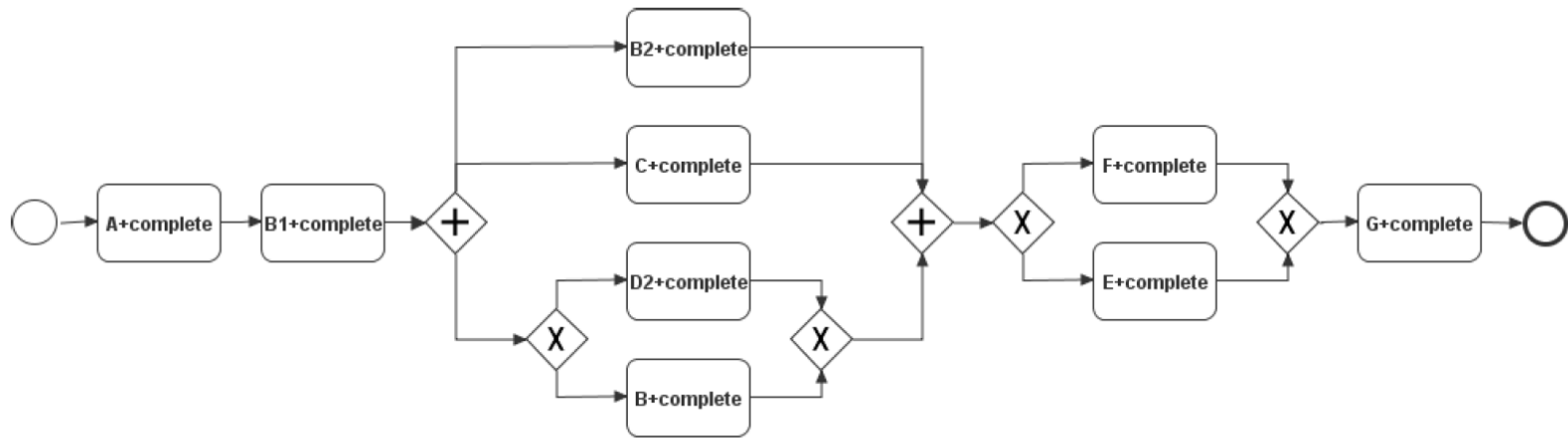


	Overall	Fitness	Precision	Simplicity	Generalization	Size	#C.P.	Similarity
Combined	0.989	0.999	0.999	0.981	0.220	53	4	-
Variant 0	0.986	0.995	0.995	0.981	0.235	14	3	0.418
Variant 1	0.989	1.000	1.000	0.981	0.263	16	3	0.464
Variant 2	0.989	1.000	1.000	0.981	0.174	10	3	0.317
Variant 3	0.989	1.000	1.000	0.981	0.264	16	3	0.464

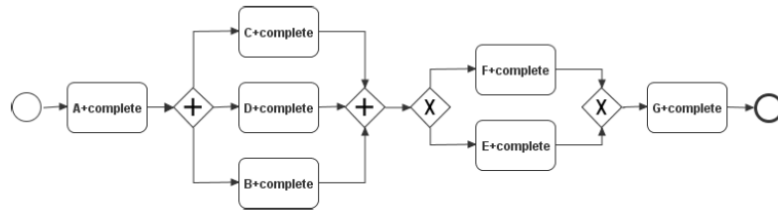
Approach 2



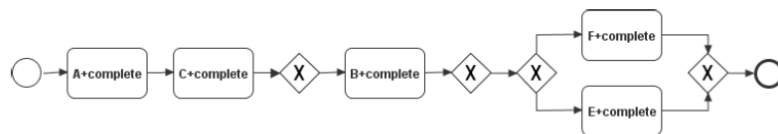
Results Approach 2 for running example



(a) Process model discovered from combined event log

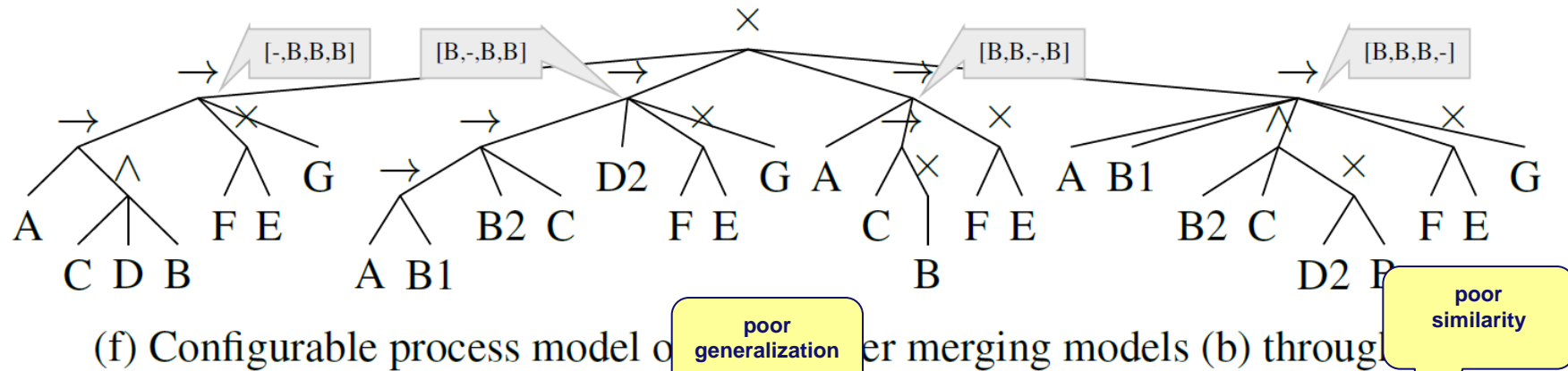


(b) Process model individualized for event log 1 (c) Process model individualized for event log 2



(d) Process model individualized for event log 3 (e) Process model individualized for event log 4

Results Approach 2 for running example

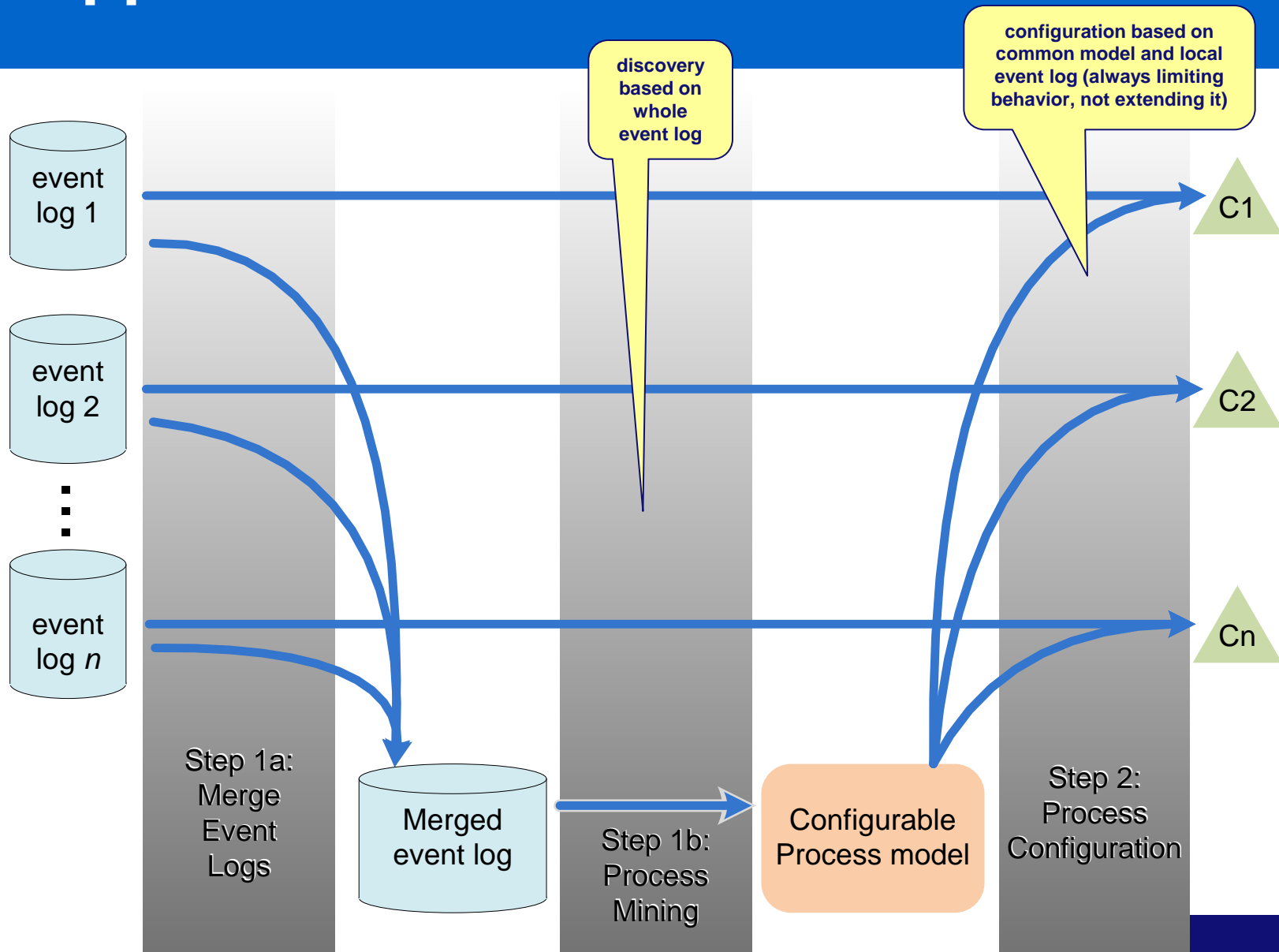


	Overall	Fitness	Precision	Simplicity	Generalization
Combined	0.958	0.974	0.921	0.968	0.212
Variant 0	0.981	0.995	0.995	0.968	0.232
Variant 1	0.984	1.000	1.000	0.968	0.246
Variant 2	0.984	1.000	1.000	0.968	0.180
Variant 3	0.869	0.886	0.649	0.968	0.232

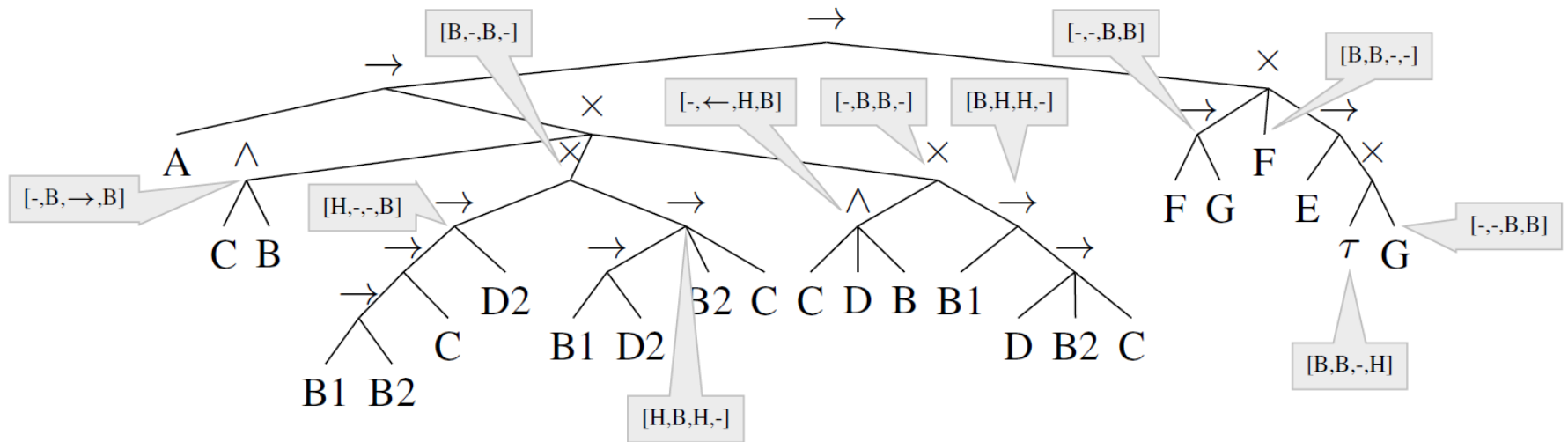
Size	#C.P.	Similarity
46	4	-
12	3	0.414
13	3	0.441
10	3	0.357
14	3	0.467

(g) Quality statistics of the configurable process model of (f)

Approach 3



Results Approach 3 for running example



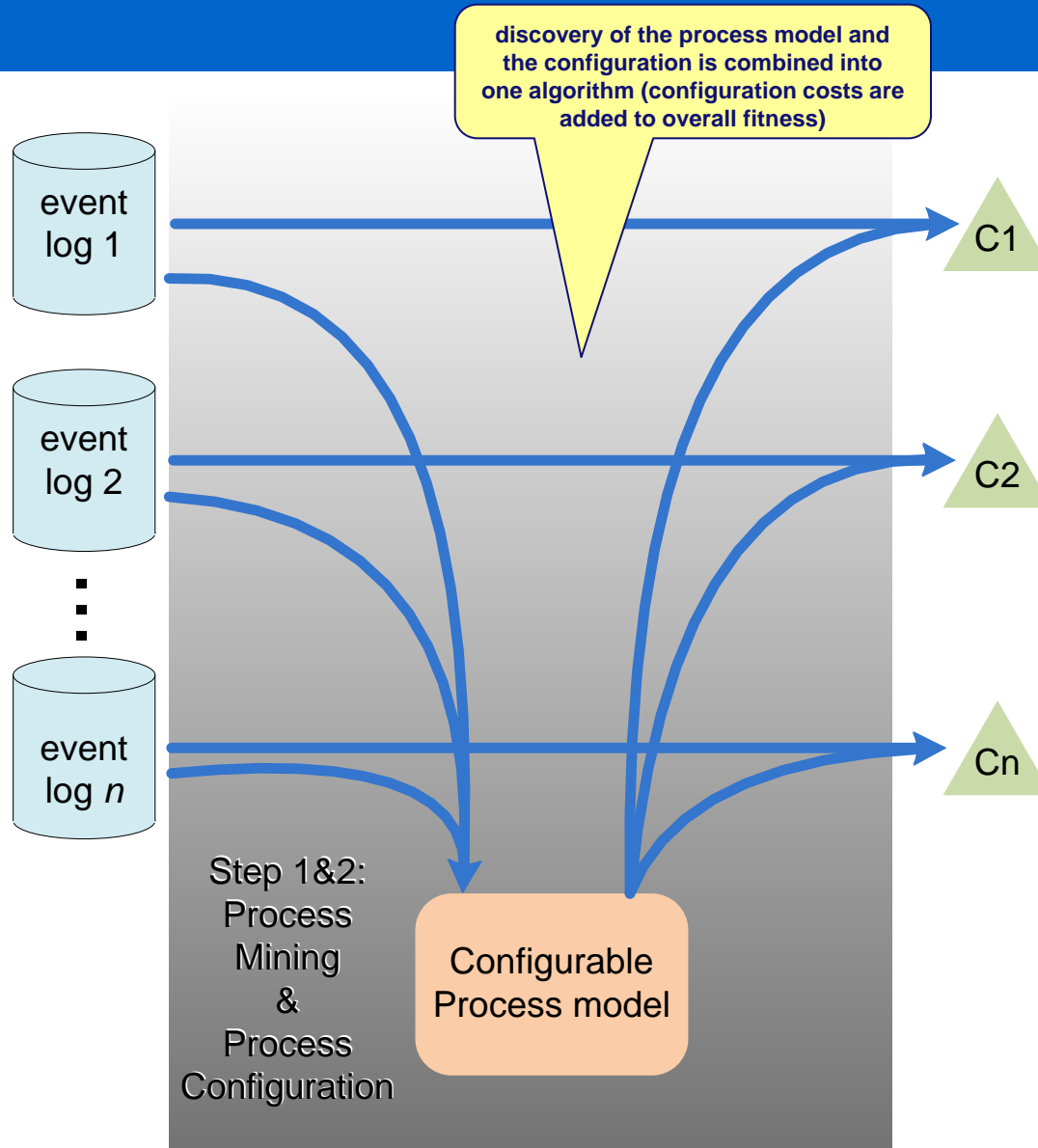
(a) Configurable process model discovered when first discovering the process model and then the configurations

	Overall	Fitness	Precision	Simplicity	Generalization
Combined	0.988	1.000	0.981	0.986	0.374
Variant 0	0.990	1.000	0.990	0.986	0.400
Variant 1	0.992	1.000	1.000	0.986	0.408
Variant 2	0.992	1.000	1.000	0.986	0.285
Variant 3	0.977	1.000	0.922	0.986	0.496

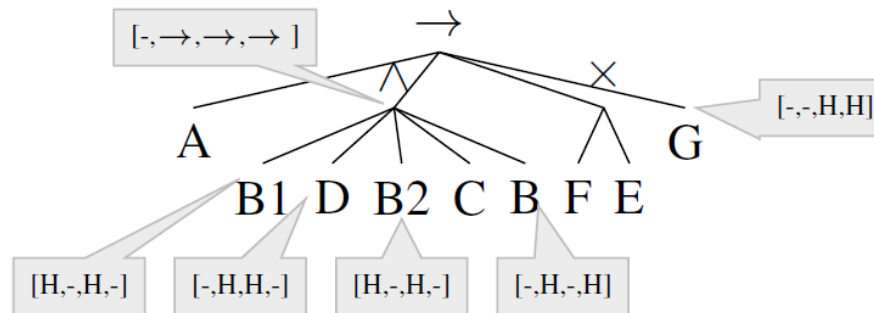
Size	#C.P.	Similarity
42	11	-
20	6	0.645
20	7	0.645
13	8	0.473
24	6	0.727

(b) Quality statistics of the configurable process model of (a)

Approach 4



Results Approach 4 for running example



(a) Configurable model discovery using the integrated approach

even better generalization

even better similarity

	Overall	Fitness	Precision	Simplicity	Generalization
Combined	0.983	0.962	0.999	1.000	0.684
Variant 0	0.996	0.995	0.994	1.000	0.738
Variant 1	0.957	0.894	1.000	1.000	0.723
Variant 2	0.998	1.000	1.000	1.000	0.614
Variant 3	0.961	0.905	1.000	1.000	0.741

Size	#C.P.	Similarity
12	6	-
10	2	0.909
10	3	0.909
8	5	0.800
10	3	0.909

(b) Quality statistics of the configurable process model of (a)

Genetic algorithms are versatile and can consider different forces at the same time



... but often not fast enough



Some pointers

- **J.C.A.M. Buijs, B.F. van Dongen, and W.M.P. van der Aalst: Mining Configurable Process Models from Collections of Event Logs, under review, 2013.**
- **Florian Gottschalk, Teun A. C. Wagemakers, Monique H. Jansen-Vullers, Wil M. P. van der Aalst, Marcello La Rosa: Configurable Process Models: Experiences from a Municipality Case Study. CAiSE 2009: 486-500**
- **Florian Gottschalk, Wil M. P. van der Aalst, Monique H. Jansen-Vullers: Merging Event-Driven Process Chains. OTM Conferences (1) 2008: 418-426**
- **Wil M. P. van der Aalst: Business Process Configuration in the Cloud: How to Support and Analyze Multi-tenant Processes? ECOWS 2011: 3-10**

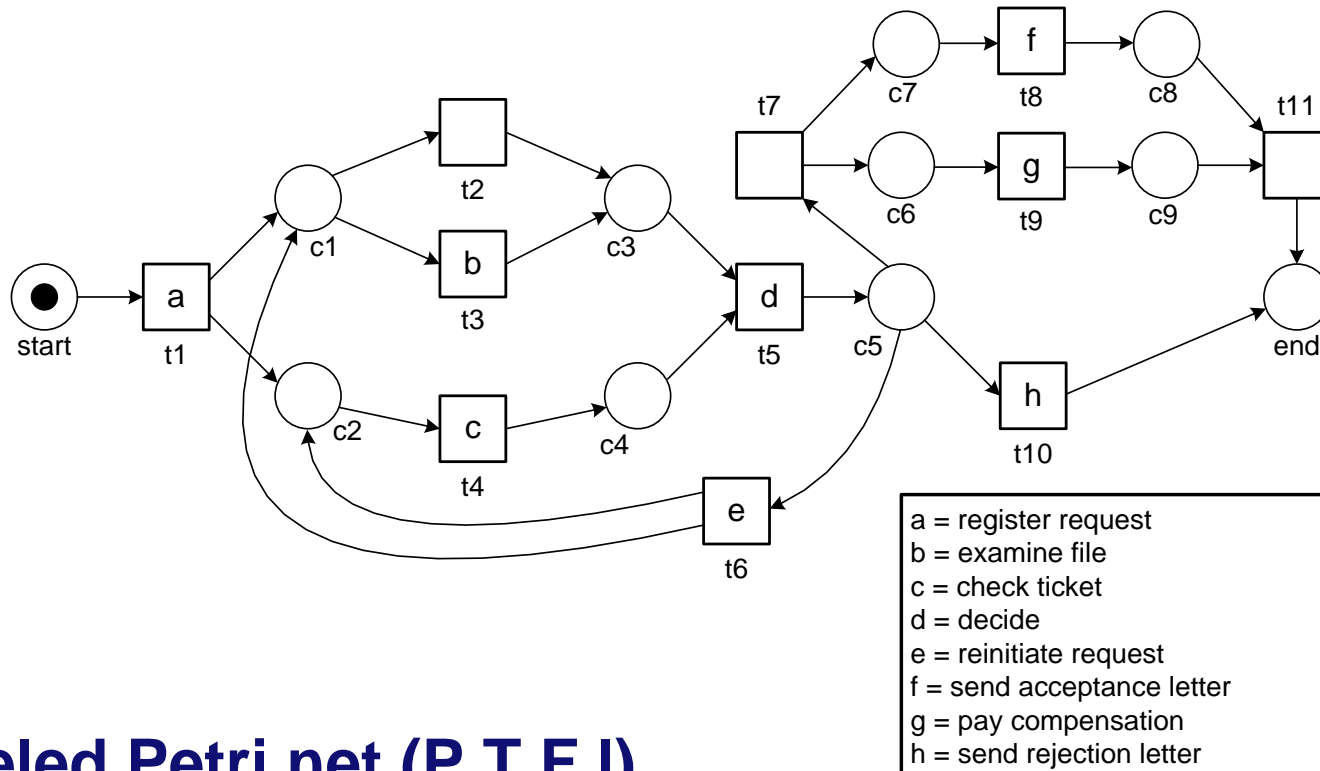
Decomposing Process Mining Problems

Joint work with Eric Verbeek, Jorge Munoz , and Josep Carmona.

Big Data: Opportunities and Challenges



System Net

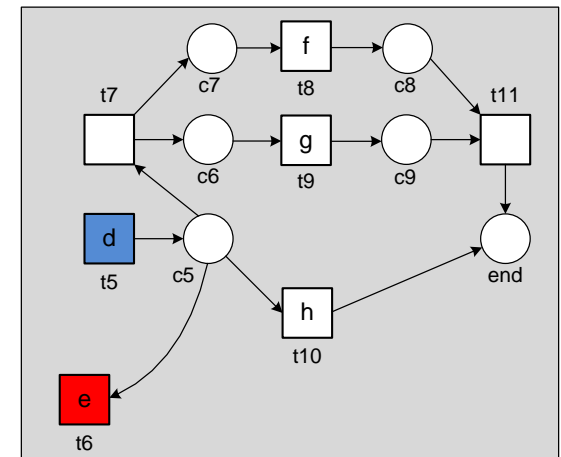
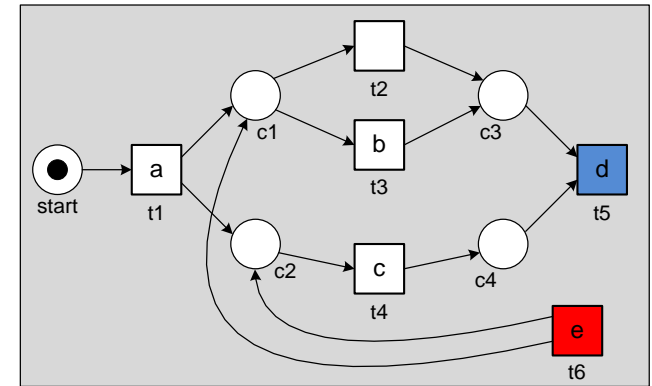
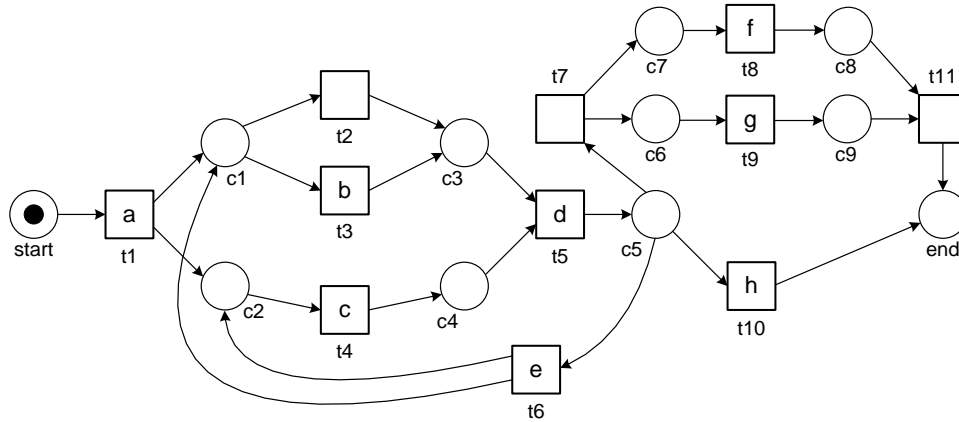


- **Labeled Petri net (P,T,F,I)**
- **Silent transitions and visible transitions (unique or not),**
- **One initial marking M_{init} , one final marking M_{final}**

Traces and Logs

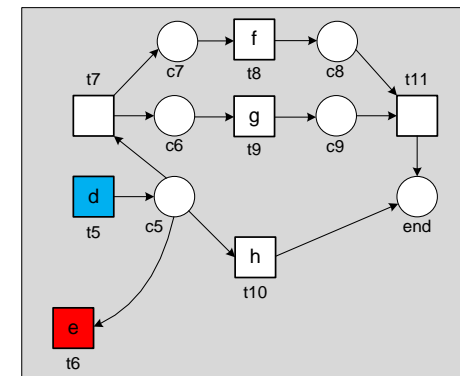
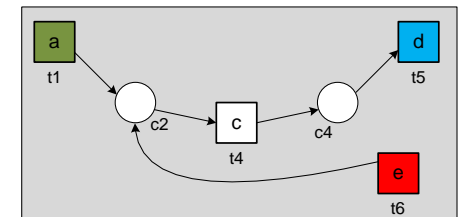
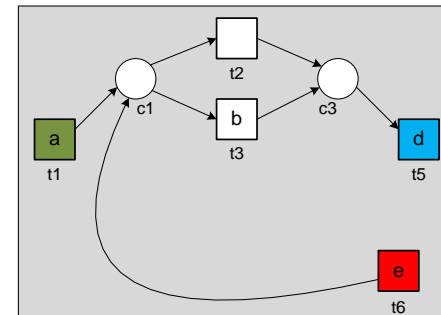
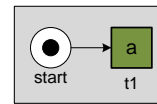
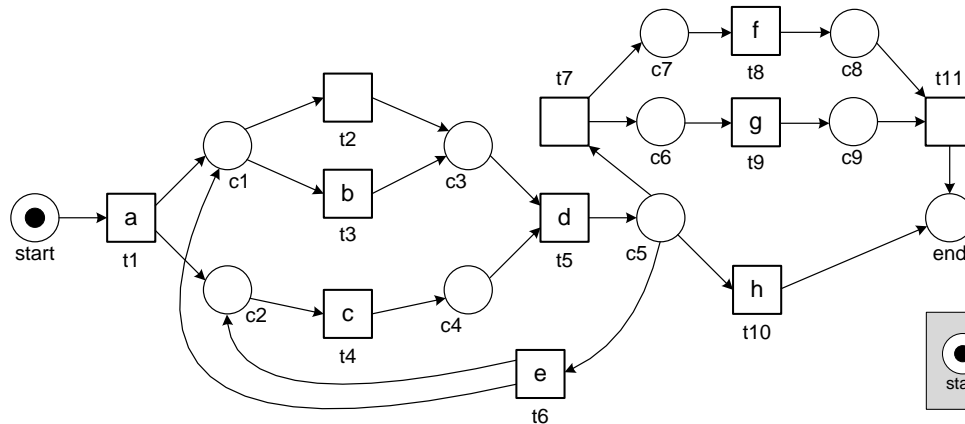
- A system net SN has a set of **possible visible traces** $\phi(\text{SN})$ starting in M_{init} and ending M_{final} only showing the visible steps.
- An **event log L** is a multiset of traces.
- Two main process mining problems:
 1. **Conformance checking**: Given L and SN, evaluate the "conformance" (e.g., fitness, precision, generalization, etc.) of L and $\phi(\text{SN})$
 2. **Process discovery**: Given L, create SN such that the conformance of L and $\phi(\text{SN})$ is "as good as possible"

Valid Decomposition



- **Union of subnets is original net**
- **No shared places**
- **Shared transitions are visible and have unique label**

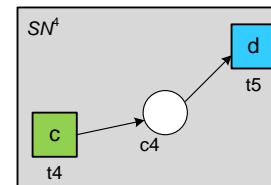
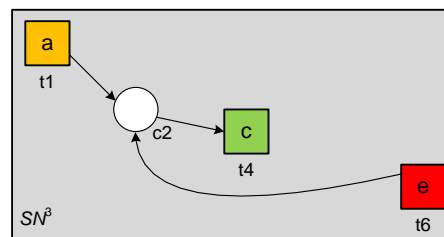
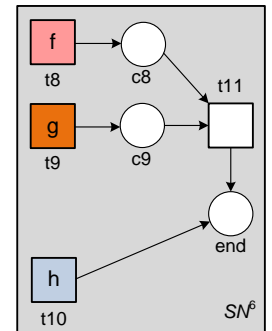
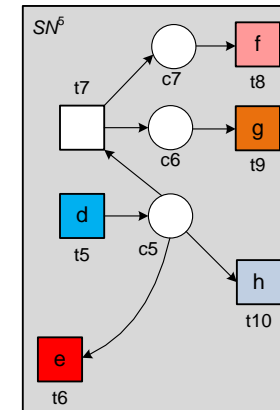
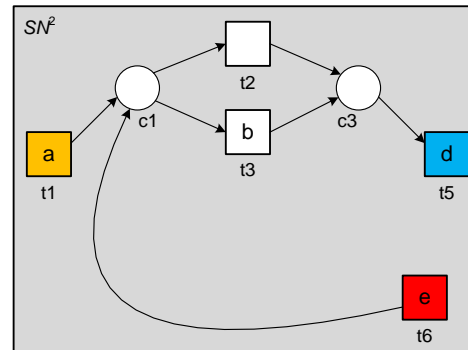
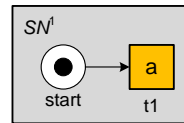
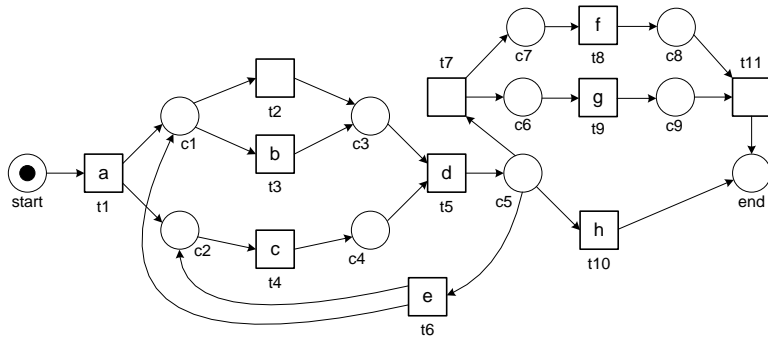
Another Decomposition



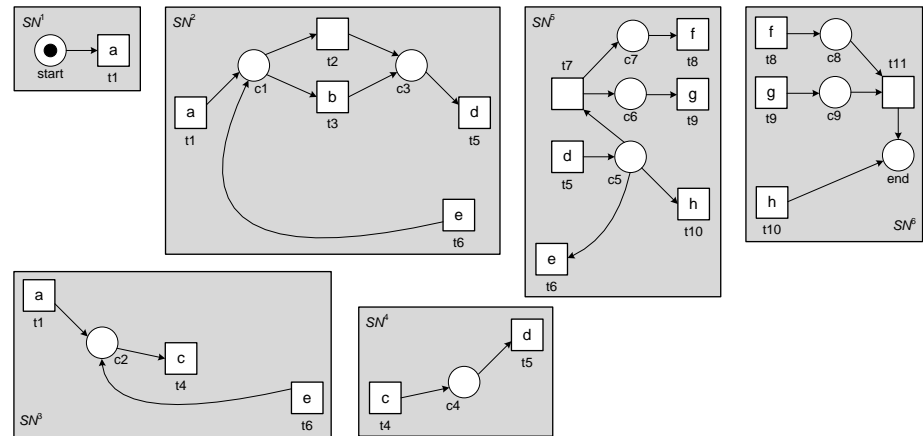
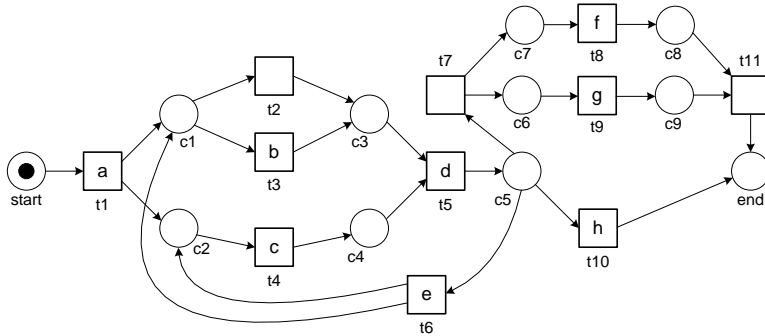
Requirement

- Union of subnets is original net
- No shared places
- Shared transitions are visible and unique

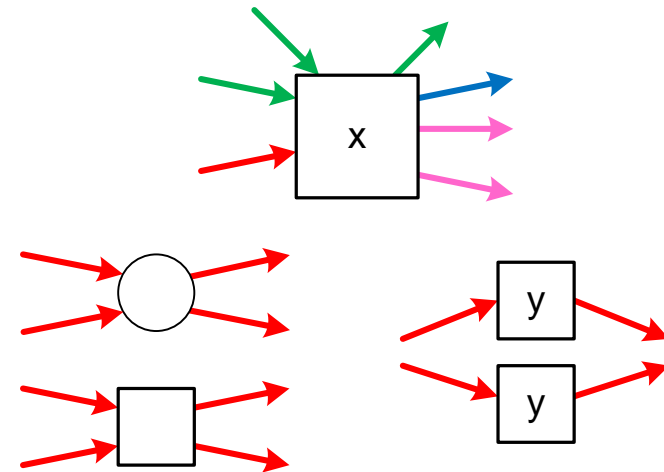
Maximal Valid Decomposition



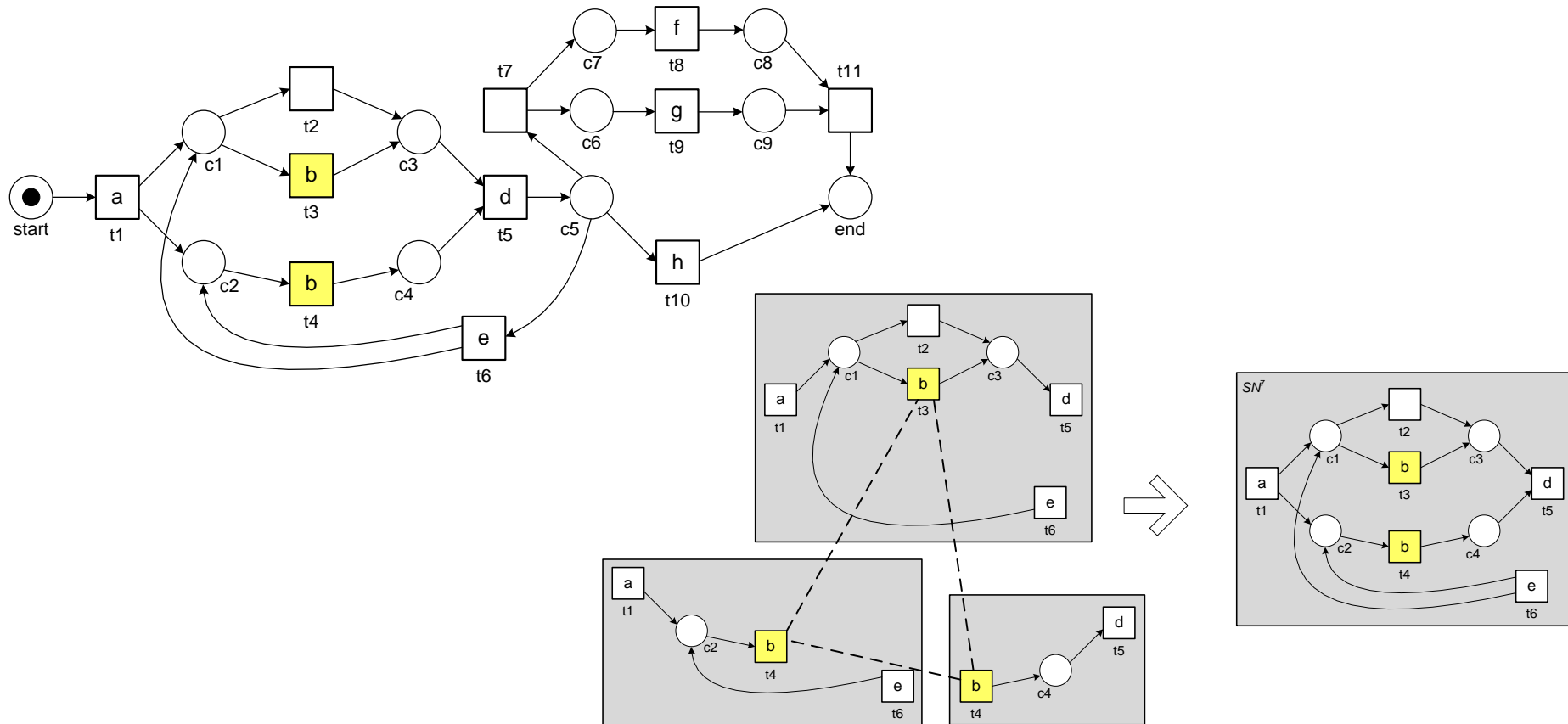
Maximal Decomposition



- **Construction: group arcs iteratively**
- **Maximal decomposition is unique**
- **There is always a valid decomposition**



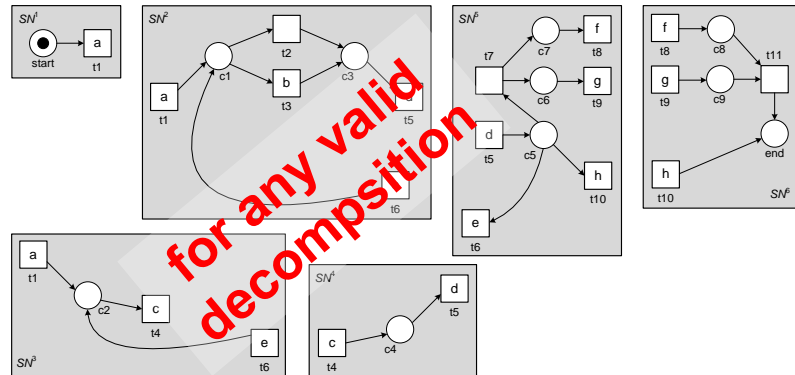
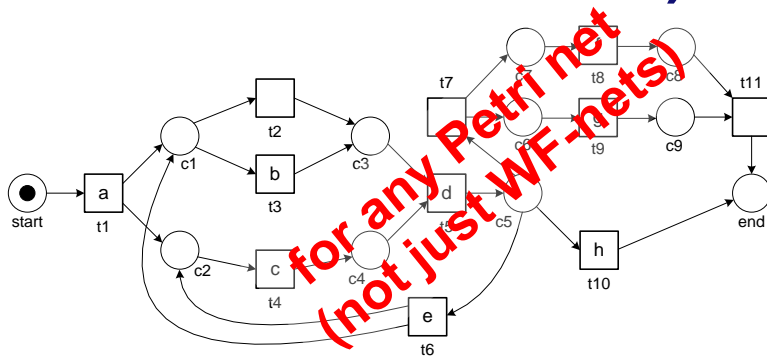
Non-unique visible labels



- Union of subnets is original net
- No shared places
- Shared transitions are visible and unique

Conformance checking can be decomposed !!!

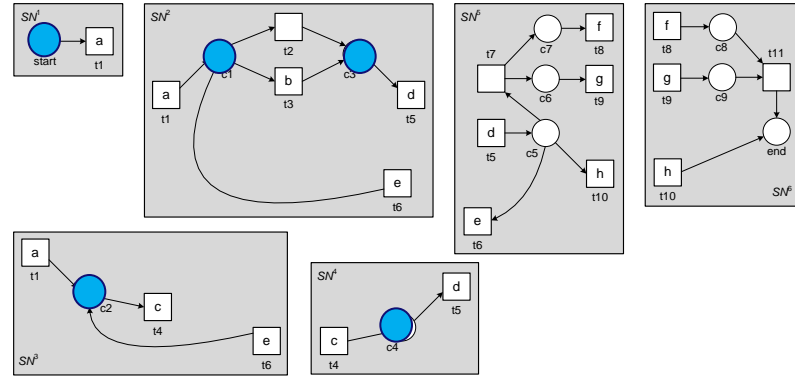
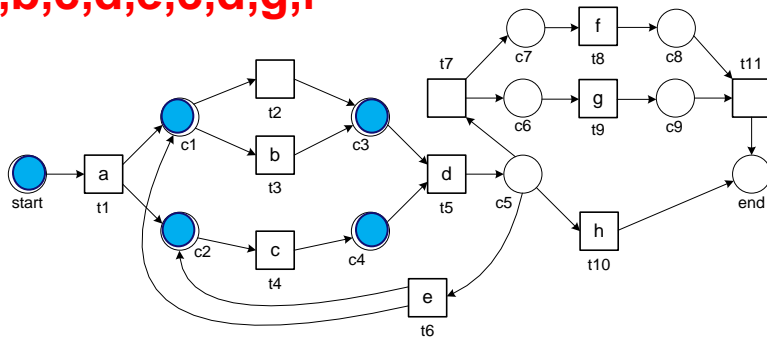
- Let L be an event log, SN a system net, and $D=\{SN^1, SN^2, \dots, SN^n\}$ a valid decomposition
- L^i is the sublog of SN^i (L projected onto visible transitions of SN^i)



**L is perfectly fitting SN
if and only if
each projected log is L^i is perfectly fitting SN^i**

Example of alignment for observed trace a,b,c,d,e,c,d,g,f

a,b,c,d,e,c,d,g,f



$\gamma_3 =$

1	2	3	4	5	6	7	8	9	10	11	12
a	b	c	d	e	c	\gg	d	\gg	g	f	\gg
a	b	c	d	e	c	τ	d	τ	g	f	τ
t1	t3	t4	t5	t6	t4	t2	t5	t7	t9	t8	t11

Etc.

$\gamma_3^1 =$

1
a
a
t1

$\gamma_3^2 =$

1	2	4	5	7	8
a	b	d	e	\gg	d
a	b	d	e	τ	d
t1	t3	t5	t6	t2	t5

$\gamma_3^3 =$

1	3	5	6
a	c	e	c
a	c	e	c
t1	t4	t6	t4

$\gamma_3^4 =$

3	4	6	8
c	d	c	d
c	d	c	d
t4	t5	t4	t5

$\gamma_3^5 =$

4	5	8	9	10	11
d	e	d	\gg	g	f
d	e	d	τ	g	f
t5	t6	t5	t7	t9	t8

$\gamma_3^6 =$

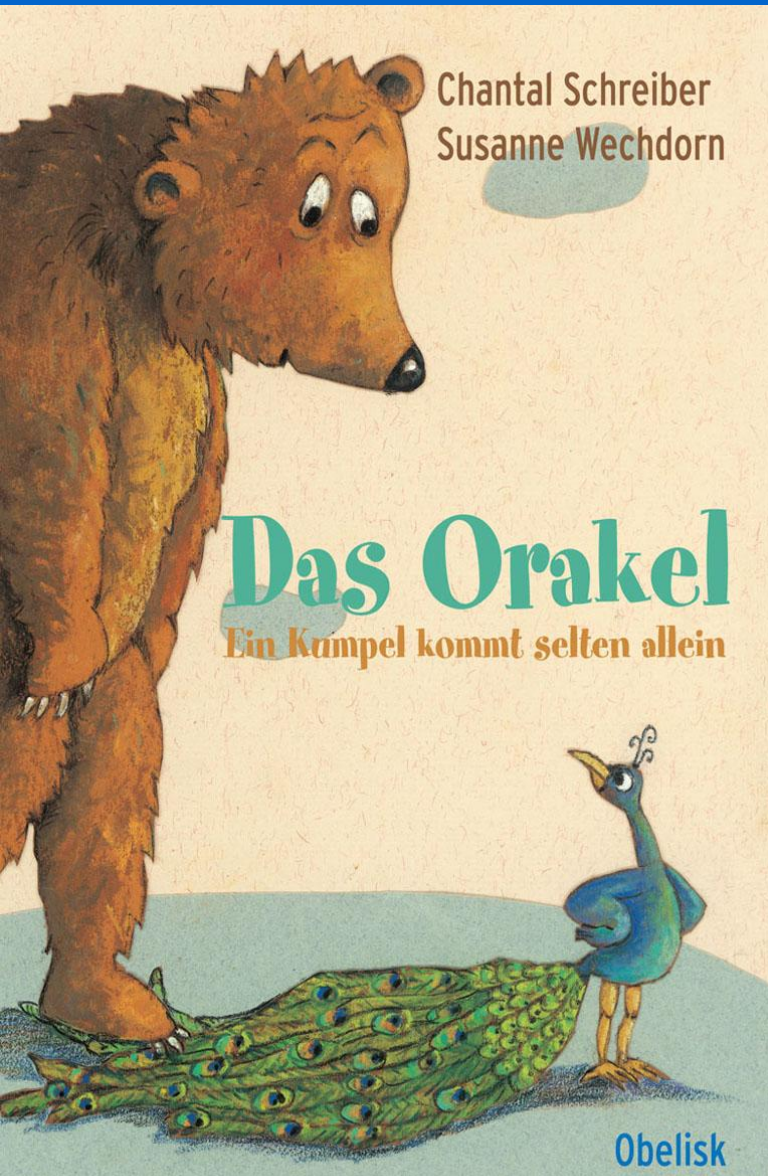
10	11	12
g	f	\gg
g	f	τ
t9	t8	t11

So What?

Quantifying Conformance

- **Exact result:** Fraction of cases perfectly fitting SN **equals** the fraction of cases for which each projected log is L^i is perfectly fitting SN^i .
- **Bound:** For fitness at the event level (costs based alignment) it is possible to compute an **optimistic** value.

Discovery can also be distributed!



1. **Assume the set of activities is split in overlapping sets.**
2. **Split log L in sublogs L^i based on these sets.**
3. **Discover a model SN^i per sublog.**
4. **Merge the models SN^i into SN and return result.**

All the earlier guarantees hold, e.g., L is perfectly fitting SN if and only if each projected log is L^i is perfectly fitting SN^i

Example

Das Orakel

$L = [\langle a, b, c, d, h \rangle^{30}, \langle a, c, b, d, e, b, c, d, j, g, f, k \rangle^{28}, \langle a, c, b, d, e, c, b, d, h \rangle^{28}, \langle a, c, b, d, e, c, b, d, j, f, g, k \rangle^{27}, \langle a, b, c, d, e, c, i, d, j, g, f, k \rangle^{26}, \langle a, b, c, d, e, i, c, d, h \rangle^{26}, \langle a, i, c, d, e, c, b, d, j, g, f, k \rangle^{25}, \langle a, i, c, d, j, f, g, k \rangle^{24}, \langle a, c, b, d, e, b, c, d, h \rangle^{24}, \langle a, b, c, d, e, b, c, d, j, g, f, k \rangle^{24}, \langle a, c, b, d, e, c, i, d, h \rangle^{22}, \langle a, b, c, d, e, c, i, d, h \rangle^{22}, \langle a, c, i, d, j, f, g, k \rangle^{21}, \langle a, c, i, d, j, g, f, k \rangle^{20}, \langle a, c, i, d, e, b, c, d, h \rangle^{18}, \langle a, c, i, d, e, c, i, d, h \rangle^{17}, \langle a, i, c, d, h \rangle^{17}, \langle a, c, b, d, j, g, f, k \rangle^{17}, \langle a, c, b, d, h \rangle^{15}, \langle a, i, c, d, e, i, c, d, j, f, g, k \rangle^{14}, \langle a, c, i, d, e, c, b, d, h \rangle^{14}, \langle a, c, i, d, e, c, b, d, j, f, g, k \rangle^{12}, \langle a, b, c, d, e, i, c, d, j, f, g, k \rangle^{12}, \langle a, b, c, d, e, c, b, d, h \rangle^{11}, \langle a, c, b, d, j, f, g, k \rangle^{10}, \langle a, i, c, d, j, g, f, k \rangle^9, \langle a, i, c, d, e, b, c, d, h \rangle^9, \langle a, i, c, d, e, c, b, d, h \rangle^9, \langle a, i, c, d, e, c, b, d, j, f, g, k \rangle^8, \langle a, c, b, d, e, b, c, d, j, f, g, k \rangle^8, \langle a, b, c, d, e, b, c, d, h \rangle^7, \langle a, c, b, d, e, i, c, d, j, g, f, k \rangle^7, \langle a, i, c, d, e, c, i, d, j, g, f, k \rangle^6, \langle a, c, i, d, h \rangle^6, \langle a, c, b, d, e, i, c, d, h \rangle^6, \langle a, i, c, d, e, b, c, d, j, g, f, k \rangle^6, \langle a, b, c, d, j, f, g, k \rangle^5, \langle a, i, c, d, e, i, c, d, h \rangle^5, \langle a, i, c, d, e, c, i, d, h \rangle^4, \langle a, c, i, d, e, i, c, d, h \rangle^4, \langle a, b, c, d, e, c, i, d, j, f, g, k \rangle^4, \langle a, b, c, d, e, c, b, d, j, g, f, k \rangle^4, \langle a, b, c, d, j, g, f, k \rangle^3, \langle a, c, i, d, e, b, c, d, j, f, g, k \rangle^3, \langle a, b, c, d, e, b, c, d, j, f, g, k \rangle^3, \langle a, i, c, d, e, b, c, d, j, f, g, k \rangle^3, \langle a, b, c, d, e, c, b, d, j, f, g, k \rangle^3, \langle a, c, i, d, e, i, c, d, j, f, g, k \rangle^2, \langle a, c, i, d, e, i, c, d, e, b, c, d, e, b, c, d, j, g, f, k \rangle^2, \langle a, b, c, d, e, i, c, d, j, g, f, k \rangle^2, \langle a, c, b, d, e, c, i, d, j, g, f, k \rangle^2, \langle a, c, i, d, e, c, i, d, j, f, g, k \rangle^2, \langle a, c, b, d, e, b, c, d, e, c, b, d, j, g, f, k \rangle^2, \langle a, c, i, d, e, c, b, d, j, g, f, k \rangle^2, \langle a, c, b, d, e, i, c, d, j, f, g, k \rangle^2, \langle a, c, i, d, e, i, c, d, e, i, c, d, j, g, f, k \rangle^1, \langle a, c, b, d, e, c, i, d, j, f, g, k \rangle^1, \langle a, i, c, d, e, c, i, d, e, c, i, d, e, i, c, d, e, i, c, d, j, g, f, k \rangle^1, \langle a, i, c, d, e, c, i, d, j, f, g, k \rangle^1, \langle a, c, i, d, e, c, i, d, j, g, f, k \rangle^1]$

$$A^1 = \{a, b, d, e, i\}$$

$$A^2 = \{a, c, d, e\}$$

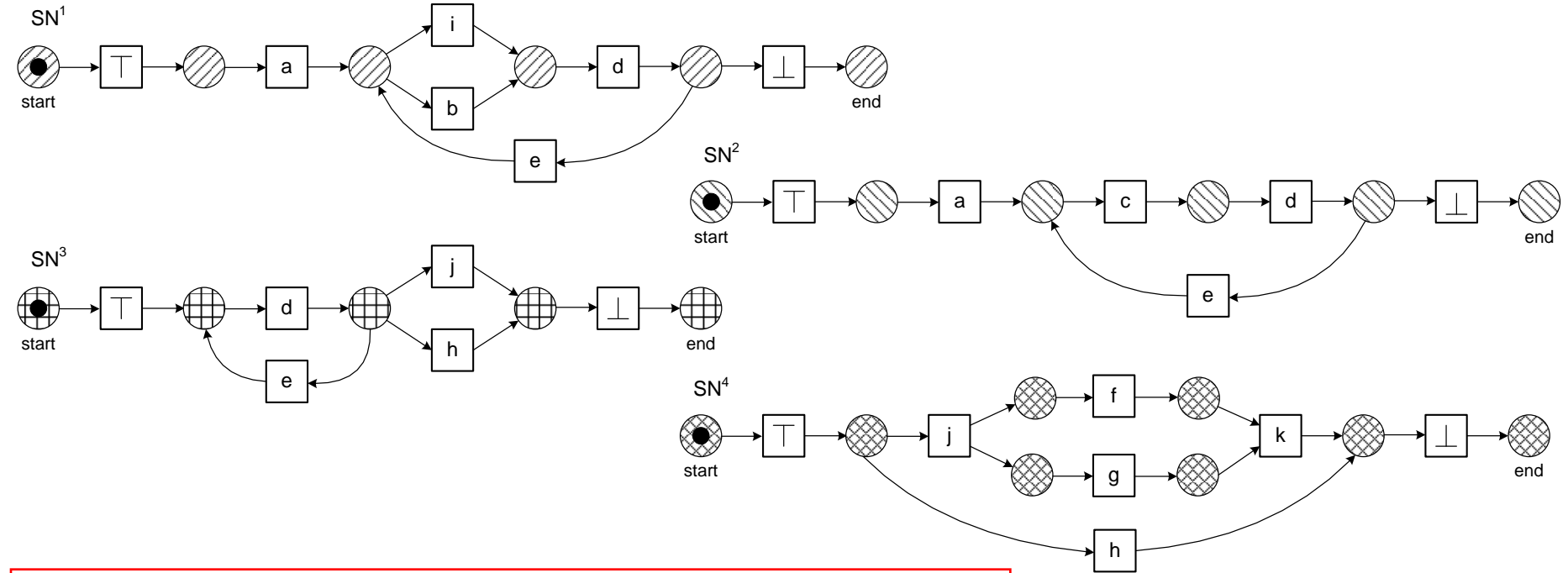
$$A^3 = \{d, e, h, j\}$$

$$A^4 = \{f, g, h, j, k\}$$

- Let's use the Alpha algorithm
- Alpha algorithm is not very suitable for discovering transition bordered subnets.
- By adding start and end activities we get (in this case) perfectly fitting subnets.

$$L' = [\langle \top \rangle \cdot \sigma \cdot \langle \perp \rangle \mid \sigma \in L_o] = [\langle \top, a, b, c, d, h, \perp \rangle^{30}, \langle \top, a, c, b, d, e, b, c, d, j, g, f, k, \perp \rangle^{28}, \langle \top, a, c, b, d, e, c, b, d, h, \perp \rangle^{28}, \langle \top, a, c, b, d, e, c, b, d, j, f, g, k, \perp \rangle^{27}, \langle \top, a, b, c, d, e, c, i, d, j, g, f, k, \perp \rangle^{26}, \dots]$$

Discover model per sublog (Alpha algorithm)



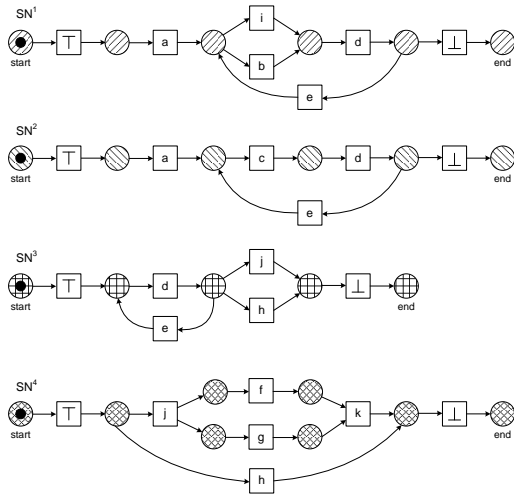
$$L^1 = [\langle \top, a, b, d, \perp \rangle^{30}, \langle \top, a, b, d, e, b, d, \perp \rangle^{28}, \langle \top, a, b, d, e, b, d, \perp \rangle^{28}, \langle \top, a, b, d, e, b, d, \perp \rangle^{27}, \langle \top, a, b, d, e, i, d, \perp \rangle^{26}, \dots]$$

$$L^2 = [\langle \top, a, c, d, \perp \rangle^{30}, \langle \top, a, c, d, e, c, d, \perp \rangle^{28}, \langle \top, a, c, d, e, c, d, \perp \rangle^{28}, \langle \top, a, c, d, e, c, d, \perp \rangle^{27}, \langle \top, a, c, d, e, c, d, \perp \rangle^{26}, \dots]$$

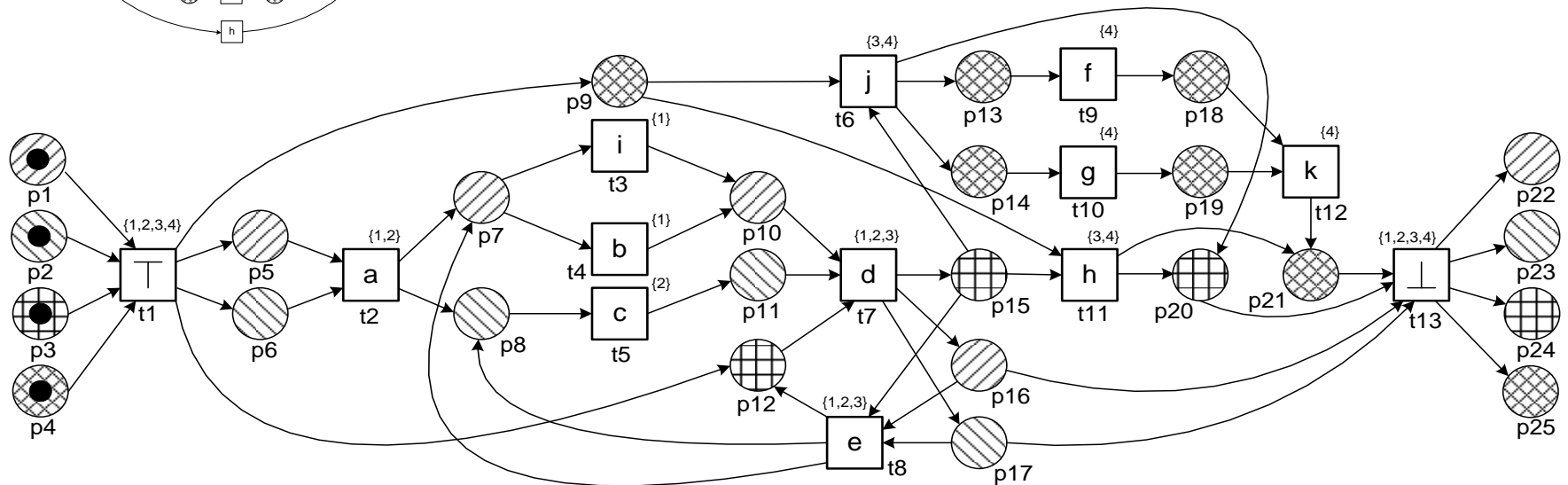
$$L_3 = [\langle \top, d, h, \perp \rangle^{30}, \langle \top, d, e, d, j, \perp \rangle^{28}, \langle \top, d, e, d, h, \perp \rangle^{28}, \langle \top, d, e, d, j, \perp \rangle^{27}, \langle \top, d, e, d, j, \perp \rangle^{26}, \dots]$$

$$L_4 = [\langle \top, h, \perp \rangle^{30}, \langle \top, j, g, f, k, \perp \rangle^{28}, \langle \top, h, \perp \rangle^{28}, \langle \top, j, f, g, k, \perp \rangle^{27}, \langle \top, j, g, f, k, \perp \rangle^{26}, \dots]$$

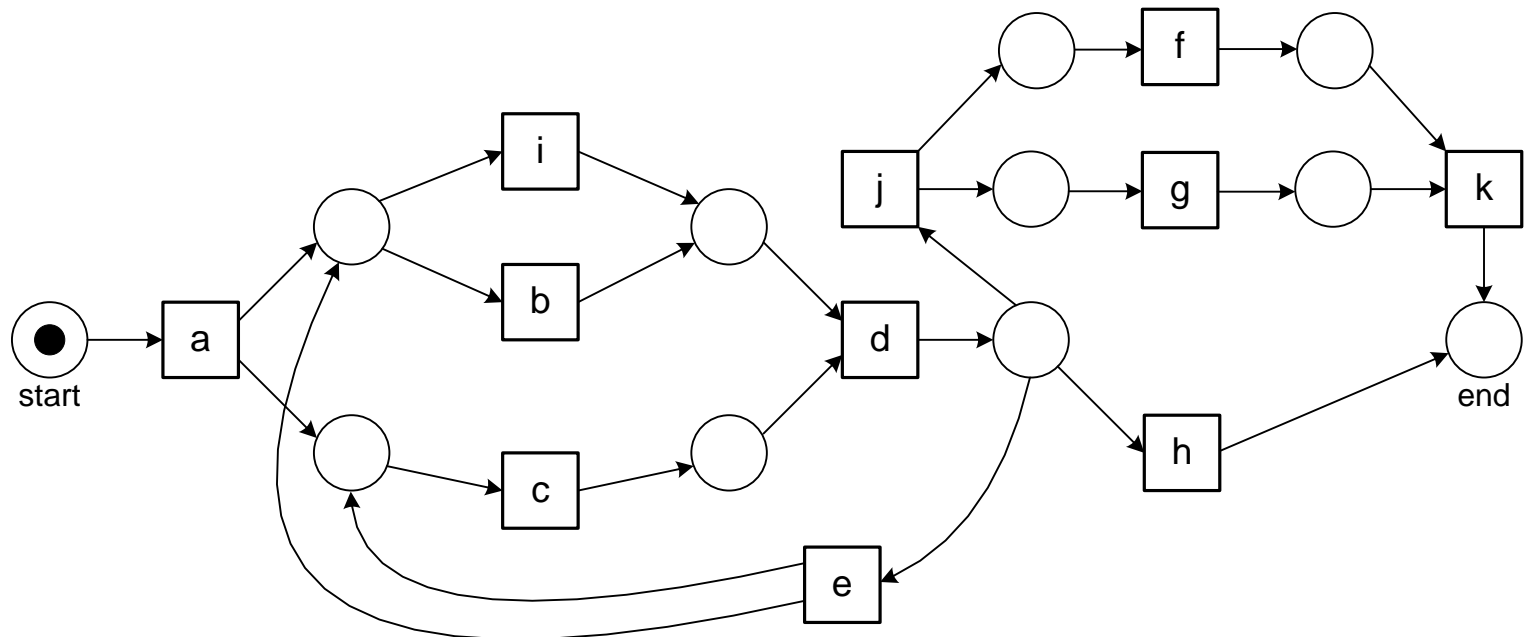
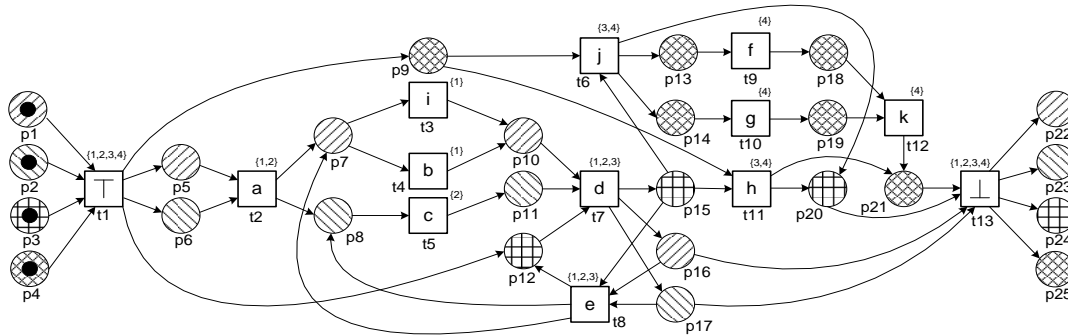
Merge models



L is perfectly fitting SN because each projected log is L^i is perfectly fitting SN^i



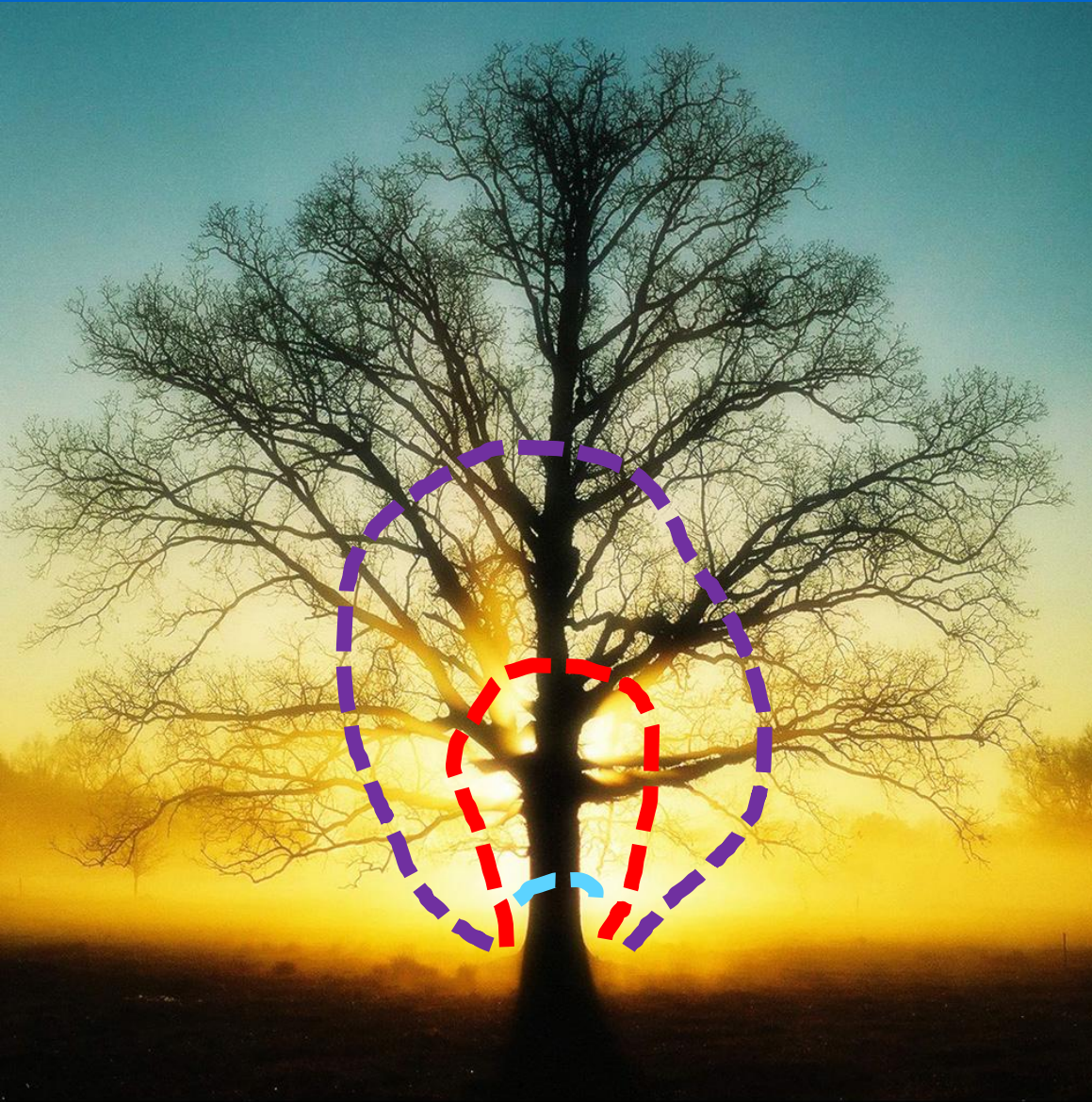
Simplify by removing redundant places and initialization



Log is perfectly fitting this model !

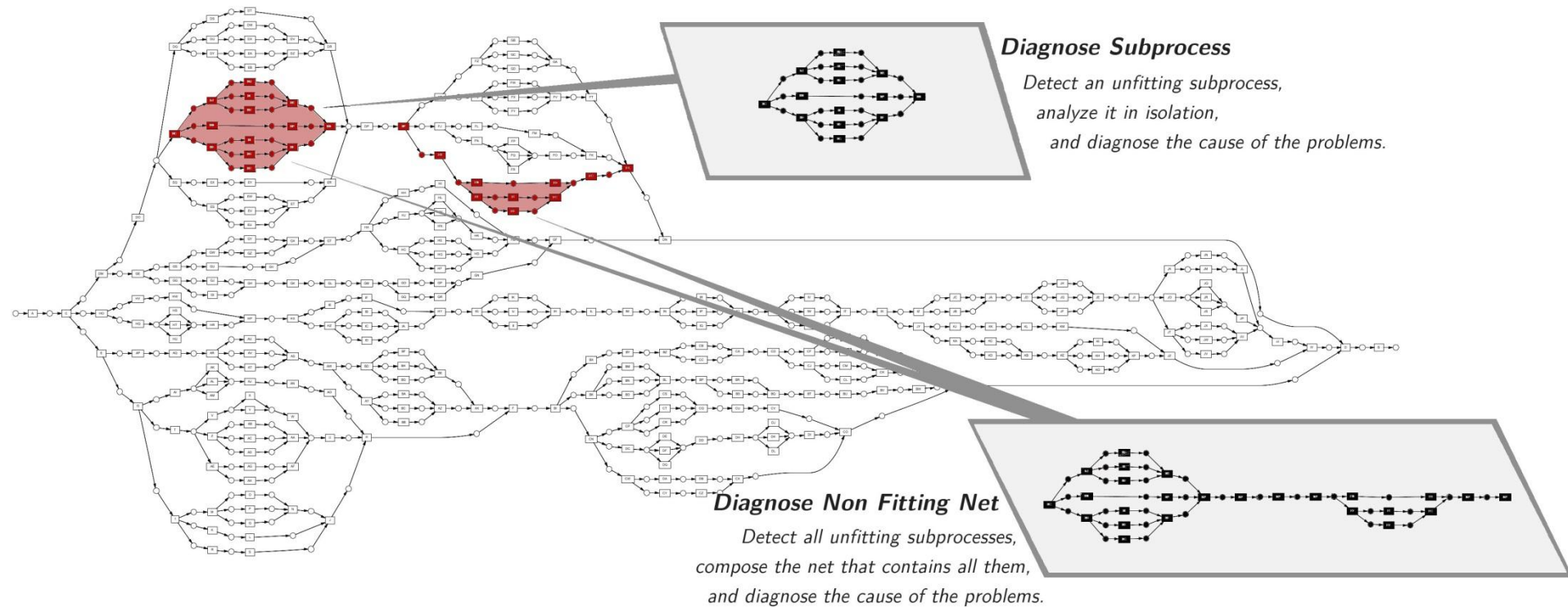


SESEs, Passages, and general result all define trees on process graph/event log



- Few large process mining tasks or many smaller process mining tasks.
- Choice of level is driven by computation time and desired diagnostics!
- All implemented in ProM.

Diagnosis



Example: Conformance Checking based on SESEs

[9,11]				k = 50				k = 100				k = 200			
P	T	f	t	S/B	>5	nf	t	S/B	>5	nf	t	S/B	>5	nf	t
prAm6	347	363	0.92 75	129/57	29	7(3%)	423	62/27	14	1(9%)	323	27/12	7	1(10%)	180
prBm6	317	317	1 88	93/38	22	0(0%)	608	66/29	14	0(0%)	318	36/16	8	0(0%)	114
prCm6	317	317	0.57 2743	93/38	22	58(92%)	189	66/29	14	41(94%)	185	36/16	8	22(96%)	502
prDm6	529	429	- -	105/34	33	5(8%)	1386	60/23	18	4(14%)	986	33/15	9	4(23%)	1284
prEm6	277	275	0.97 3566	82/35	20	2(5%)	529	35/13	11	2(5%)	313	15/7	5	2(6%)	211
prFm6	362	299	- -	108/43	28	2(6%)	1667	57/23	15	2(21%)	813	21/9	5	1(23%)	562

k=inf (no decomposition)

some overhead for easy problems

intractable problems become tractable

stopped after 10 hours

problems are often local

suitable k-value depends on model/log

k = maximal number of arcs in one SESE, P = # places, T = # transitions, f = fitness, t = time in seconds, S = # transition bounded SESEs, B = # bridges, >5 = # more than 5 arcs, nf = # non-fitting parts.

Some pointers

- **Wil M.P. van der Aalst. Decomposing Petri Nets for Process Mining: A Generic Approach. BPM Center Report BPM-12-20, BPMcenter.org, 2012**
- **Wil M. P. van der Aalst: Distributed Process Discovery and Conformance Checking. FASE 2012: 1-25**
- **Wil M. P. van der Aalst: Decomposing Process Mining Problems Using Passages. Petri Nets 2012: 72-91**
- **H. M. W. (Eric) Verbeek, Wil M. P. van der Aalst: An Experimental Evaluation of Passage-Based Process Discovery. Business Process Management Workshops 2012: 205-210**
- **Wil M.P. van der Aalst and Eric Verbeek. Process Discovery and Conformance Checking Using Passages. BPM Center Report BPM-12-21, BPMcenter.org, 2012**
- **J. Munoz-Gama, J. Carmona, W. van der Aalst: Hierarchical Conformance Checking of Process Models Based on Event Logs. In: Applications and Theory of Petri Nets, 2013**

Conclusion

Conclusion (1/2)

- **Alignments are essential for relating observed and modeled behavior!**
- **Conformance has (at least) four dimensions!**
- **Representational bias is important (and should not be confused with visualization)!**
- **New questions are emerging:**
 - mediating between a reference model and observed behavior
 - discovering configurable process models
- **Decomposing process mining problems to deal with Big Data.**

Conclusion (2/2)

Still many challenging and highly relevant open problems in process mining!



Data Scientist: The Sexiest Job of the 21st Century
by Thomas H. Davenport and D.J. Patil

