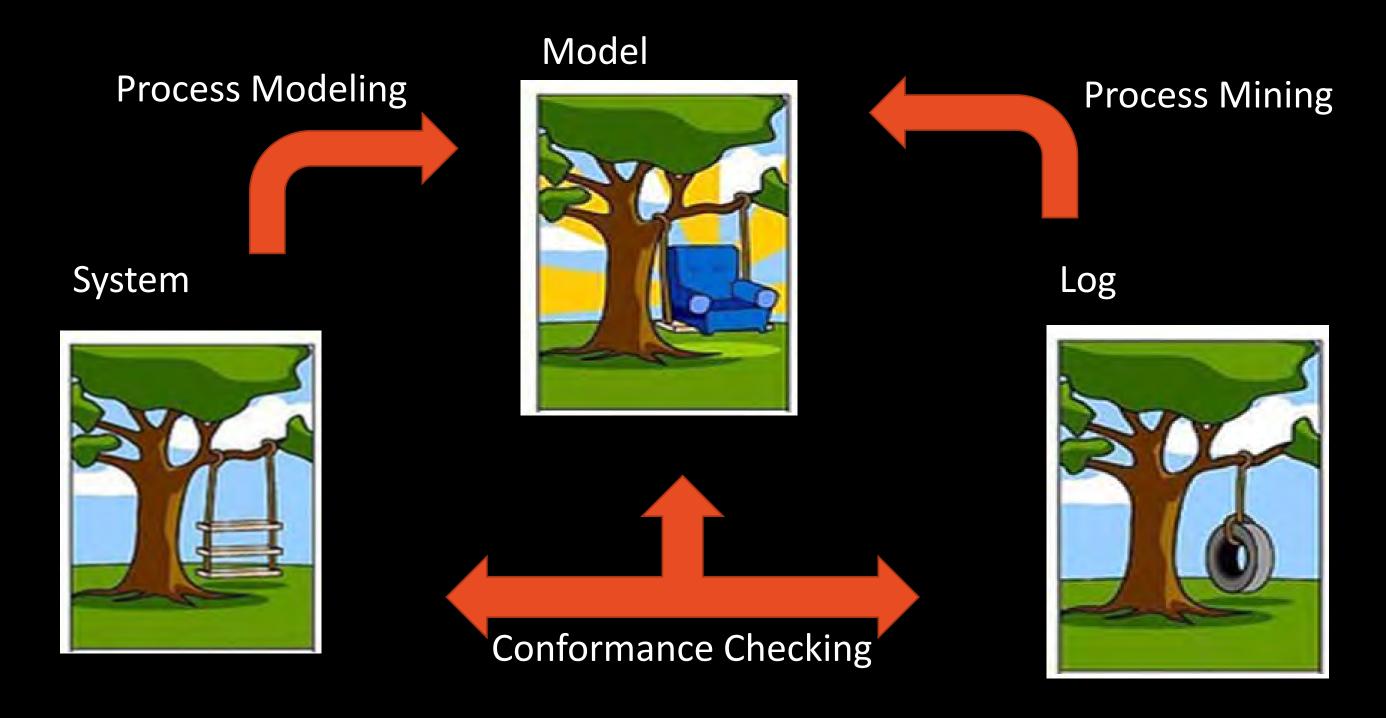
A Unified Approach for Measuring Precision and Generalization Based on Anti-Alignments

Boudewijn van Dongen

Josep Carmona

Thomas Chatain

Conformance in Process Mining



Alignments & Fitness

• Fitness is a measure for the amount of behavior shown in the log that fits the model

 Alignments provide the basis for computing fitness

• An *alignment* shows where deviations occurred and why these deviation are considered as such

Model







Anti-Alignments

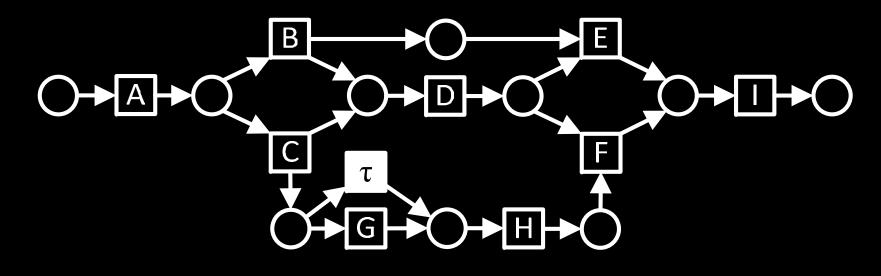
- Anti-alignments show how far the model allows you to deviate from observed behavior
- Given a model M, a finite $\log L$ and a distance function d, an (n,m) anti-alignment is a firing sequence s of the model of length n, such that for each trace t in the $\log holds$ that $d(s,t) \ge m$



Anti-Alignments - basics

- Given a model M, a finite log L and a distance function d, an (n,m) anti-alignment is a firing sequence s of the model of length n, such that for each trace t in the log holds that $d(s,t) \ge m$
- A maximal complete anti alignment of length n reaches the final marking and maximizes the distance m.

Trace	Frequency
<a,b,d,e,i></a,b,d,e,i>	1207
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56
<a,c,h,d,f,i></a,c,h,d,f,i>	23
<a,c,d,h,f,i></a,c,d,h,f,i>	28



Maximal complete AA:<A,C,G,H,D,F,I> with n=7 and $m=^{1}/_{7}$

Anti-Alignments - properties

- No anti alignments have to exist, if L is the language of M
- If M has a loop, infinitely many anti-alignments exist and their distances typically go to 1.
- Finding an anti-alignment with maximal m, given n can be translated into a SAT problem (when using hamming distances)
- Finding an anti-alignment with minimal *n*, given *m* can be translated into a SAT problem (when using hamming distances)

 No smart way exists yet for computing anti-alignments using editdistances.

Conformance Checking: Precision

 Precision is a measure for the fraction of the behavior of the model that is not in the log

 Simply comparing the (possibly infinite) behavior is infeasible and not very informative.

 Most precision metrics estimate the size of the "unseen" behavior by looking "one step ahead".

Model

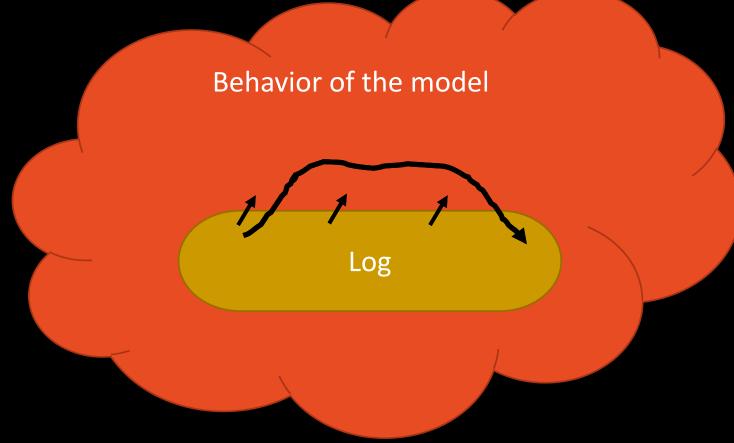


Log



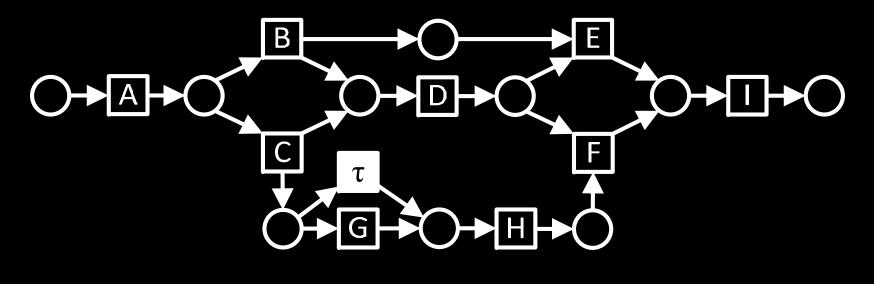
 Anti-alignments show behavior of the model as different as possible from behavior in the log

 With anti-alignments, you look at entire paths!



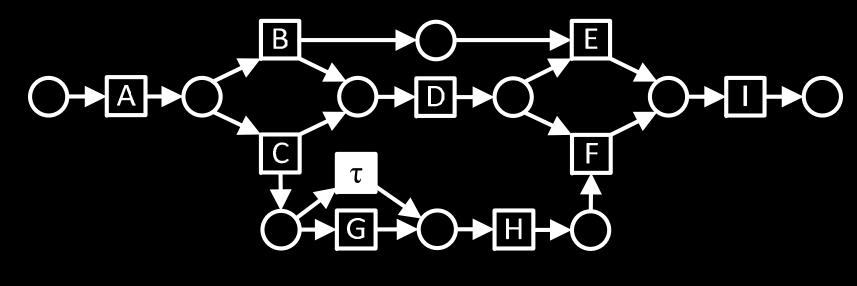
- Consider a model M and a log L.
- Now remove a trace t from the log to get L^t .
- Compute a maximal complete anti alignment s of length |t| for log L^t .
- In a very precise model, s = t, hence 1-d(s,t) is a precision measure.

Trace t	Freq.	AA for L ^t (s)	d(s,t)
<a,b,d,e,i></a,b,d,e,i>	1207		
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145		
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56		
<a,c,h,d,f,i></a,c,h,d,f,i>	23		
<a,c,d,h,f,i></a,c,d,h,f,i>	28		



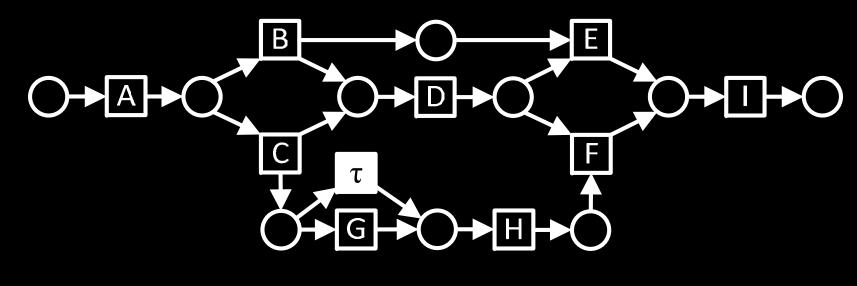
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Trace t	Freq.	AA for L ^t (s)	d(s,t)
<a,b,d,e,i></a,b,d,e,i>	1207	<a,b,d,e,i></a,b,d,e,i>	0
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145		
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56		
<a,c,h,d,f,i></a,c,h,d,f,i>	23		
<a,c,d,h,f,i></a,c,d,h,f,i>	28		



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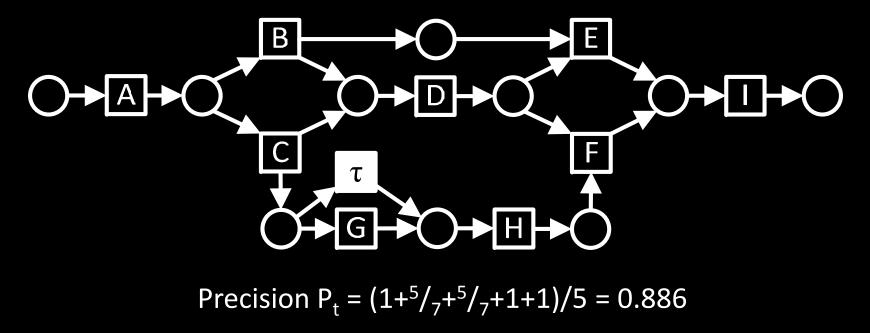
Trace t	Freq.	AA for L ^t (s)	d(s,t)
<a,b,d,e,i></a,b,d,e,i>	1207	<a,b,d,e,i></a,b,d,e,i>	0
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	$^{2}/_{7}$
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56		
<a,c,h,d,f,i></a,c,h,d,f,i>	23		
<a,c,d,h,f,i></a,c,d,h,f,i>	28		



Anti-Alignment Based Precision (trace based)

- Consider a model M and a log L.
- Now remove a trace t from the log to get L^t .
- Compute a maximal complete anti alignment s of length |t| for log L^t .
- In a very precise model, s = t, hence 1-d(s,t) is a precision measure.

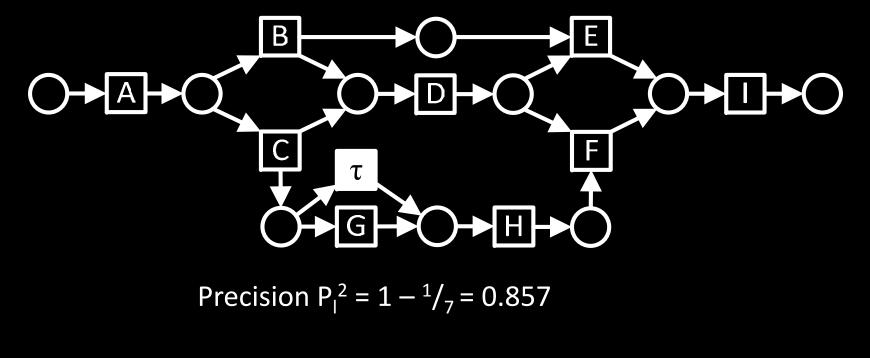
Trace t	Freq.	AA for L ^t : s	d(s,t)
<a,b,d,e,i></a,b,d,e,i>	1207	<a,b,d,e,i></a,b,d,e,i>	0
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	$^{2}/_{7}$
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	² / ₇
<a,c,h,d,f,i></a,c,h,d,f,i>	23	<a,c,h,d,f,i></a,c,h,d,f,i>	0
<a,c,d,h,f,i></a,c,d,h,f,i>	28	<a,c,d,h,f,i></a,c,d,h,f,i>	0



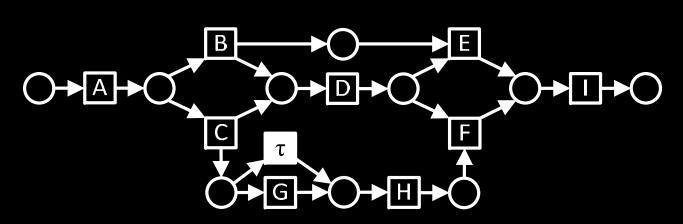
Anti-Alignment Based Precision (log based)

- Consider a model M and a log L.
- Compute a maximal complete anti alignment s of length $x \cdot |t|^{mx}$ for log L.
- In a very precise model, $s \in L$ and hence the minimal d(s,t) will be 0.

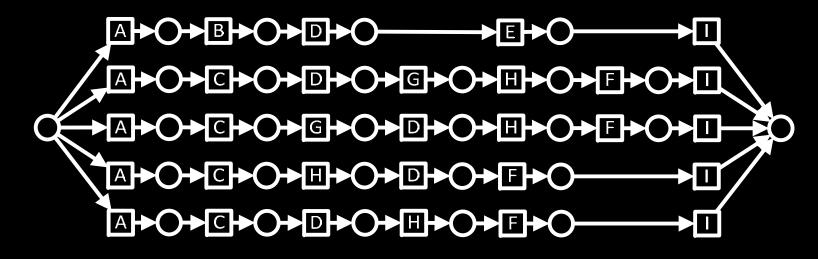
Trace t	Freq.	AA for L ^t : s	d(s,t)
<a,b,d,e,i></a,b,d,e,i>	1207	<a,b,d,e,i></a,b,d,e,i>	0
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	$^{2}/_{7}$
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	² / ₇
<a,c,h,d,f,i></a,c,h,d,f,i>	23	<a,c,h,d,f,i></a,c,h,d,f,i>	0
<a,c,d,h,f,i></a,c,d,h,f,i>	28	<a,c,d,h,f,i></a,c,d,h,f,i>	0
-	-	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	1/7



Precision

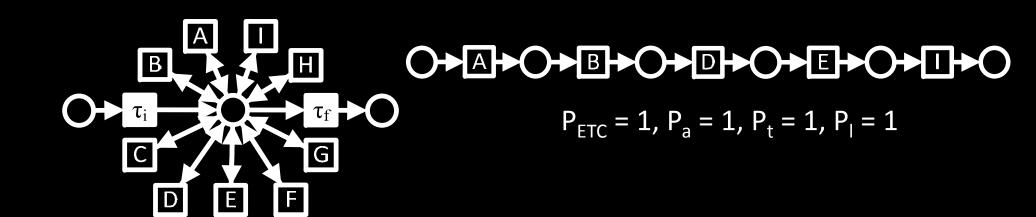


 $P_{ETC} = 0.994$, $P_a = 0.982$, $P_t = 0.886$, $P_l = 0.857$



$$P_{ETC} = 0.359$$
, $P_a = 1$, $P_t = 1$, $P_l = 1$

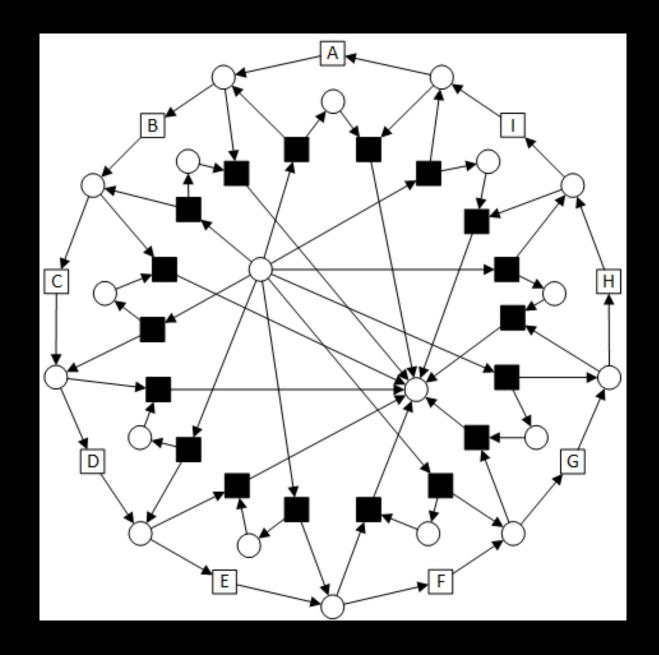
Trace	Frequency
<a,b,d,e,i></a,b,d,e,i>	1207
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56
<a,c,h,d,f,i></a,c,h,d,f,i>	23
<a,c,d,h,f,i></a,c,d,h,f,i>	28



$$P_{ETC} = 0.119$$
, $P_a = 0.142$, $P_t = 0$, $P_l = 0$

Precision

Trace	Frequency
<a,b,d,e,i></a,b,d,e,i>	1207
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56
<a,c,h,d,f,i></a,c,h,d,f,i>	23
<a,c,d,h,f,i></a,c,d,h,f,i>	28



$$P_{ETC} = 0.185$$
, $P_a = 0.889$, $P_t = 0$, $P_l = 0$

Conformance Checking: Generalization

 Generalization is a measure for the ability of a model to predict unseen, but correct behavior

 Behavior is correct if it is part of the unknown system

 Most generalization metrics look at frequencies of model elements

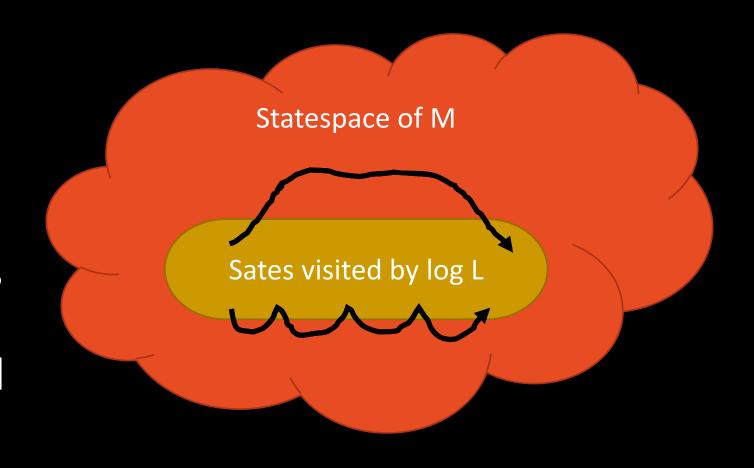


Generalization

 Assumption: A model generalizes if it allows for new sequences of behavior while not introducing too many new states.

Again, we use anti-alignments!

 Recovery distance is a measure for the maximal number of steps to get from the anti-alignment back into the statespace covered by the log.

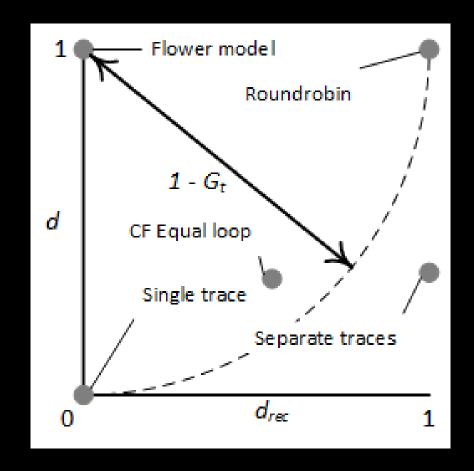


Anti-Alignment Based Generalization

Consider a model M and a log L

• Now remove a trace t from the log to get L^t and compute the corresponding anti-alignment s

 A model generalizes if s is very difference from the traces in L^t is high, and the recovery distance is low



Anti-Alignment Based Generalization

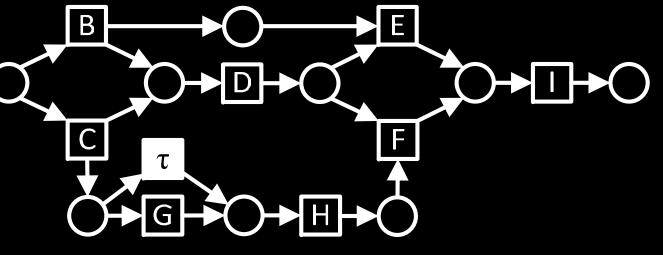
Same procedure is used as for precision

Distance to the log L^t is considered

Recovery distance is considered ○→A→C

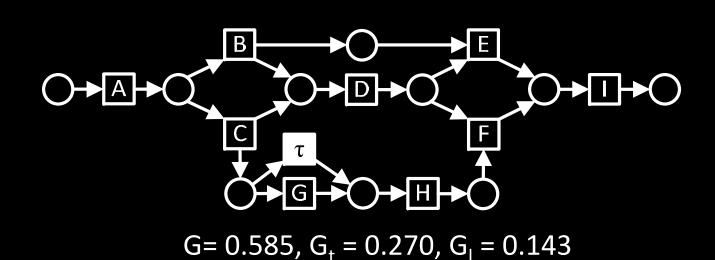
• Trace frequency is considered!

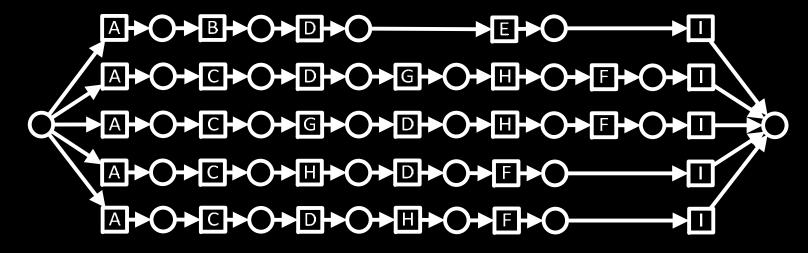
Trace t	Freq.	AA for <i>L^t</i> : s	d(s,t)	$d(s,L_t)$	d _{rec}
<a,b,d,e,i></a,b,d,e,i>	1207	<a,b,d,e,i></a,b,d,e,i>	0	$\frac{3}{6}$	2/4
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	$^{2}/_{7}$	1/7	0
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>	² / ₇	1/7	0
<a,c,h,d,f,i></a,c,h,d,f,i>	23	<a,c,h,d,f,i></a,c,h,d,f,i>	0	$^{2}/_{6}$	1/6
<a,c,d,h,f,i></a,c,d,h,f,i>	28	<a,c,d,h,f,i></a,c,d,h,f,i>	0	1/6	0
-	-	<a,c,g,h,d,f,i></a,c,g,h,d,f,i>		1/7	0



Precision $P_t = 0.886$ Precision $P_l = 0.857$ Generalization $G_t = 0.270$ Generalization $G_l = 0.143$

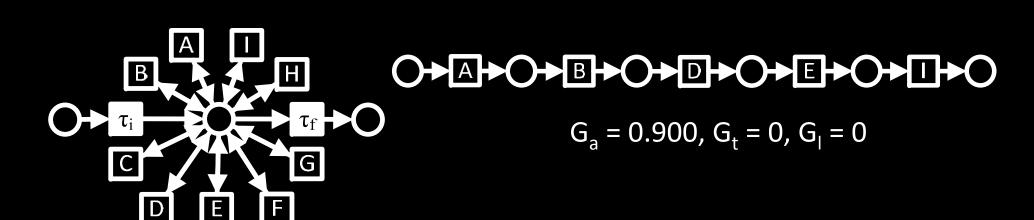
Generalization





$G_{\alpha} =$	0.145,	G ₊ =	0. ($G_1 = 0$
d	,	ι	,	

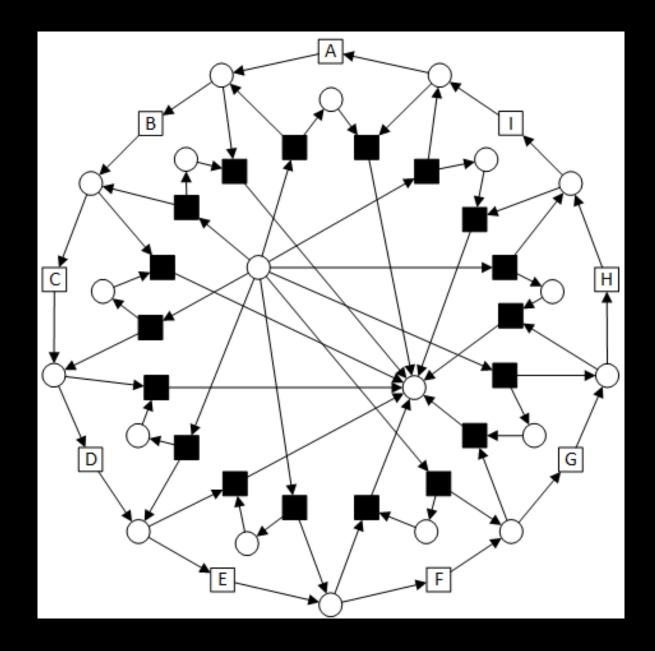
Trace	Frequency
<a,b,d,e,i></a,b,d,e,i>	1207
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56
<a,c,h,d,f,i></a,c,h,d,f,i>	23
<a,c,d,h,f,i></a,c,d,h,f,i>	28



$$G_a = 0.903$$
, $G_t = 1$, $G_l = 1$

Generalization

Trace	Frequency
<a,b,d,e,i></a,b,d,e,i>	1207
<a,c,d,g,h,f,i></a,c,d,g,h,f,i>	145
<a,c,g,d,h,f,i></a,c,g,d,h,f,i>	56
<a,c,h,d,f,i></a,c,h,d,f,i>	23
<a,c,d,h,f,i></a,c,d,h,f,i>	28



$$G_a = 0.4$$
, $G_t = 0$, $G_l = 0$

Conclusions & Future Work

- Anti-alignments provide insights into the behavior of a model outside of the log
- Using anti-alignments, we provide metrics for precision and generalization
- Our precision metric consistently ranks models with more traces as less precise as opposed to other metrics
- Efficient implementations are underway:
 - For various distance functions (hamming, edit, etc.)
 - For various model types (Petri nets / process trees)